

Name:

Key

ID #

1- A rock is released from rest from a 100-m cliff. How long does it take to fall:

a- the first 50 m?

$$v_0 = 0, \quad \Delta y = -50 \text{ m}, \quad a = -g$$

$$\Delta y = v_0 t - \frac{1}{2} g t^2$$

$$-50 = 0 - 4.9 t^2 \Rightarrow t_1 = \sqrt{10.2} \approx \boxed{3.2 \text{ s}}$$

b- the second 50 m?

we find the total time needed to fall 100m first.

$$v_0 = 0, \quad \Delta y = -100 \text{ m}, \quad a = -g$$

$$\Delta y = v_0 t - \frac{1}{2} g t^2$$

$$-100 = -4.9 t^2$$

$$\Rightarrow t = \sqrt{20.4} = 4.5 \text{ s}$$

then

the time needed for the second 50-m is

$$t_2 = t - t_1 = 4.5 - 3.2 = \boxed{1.3}$$

2- A proton moving along the x axis has a position given by

$$x = 50 t + 10 t^2$$

Where t is measured in seconds and x is in meters.

Calculate the average speed of the proton during the first 3.0 seconds of its motion.

Method 1

$$\text{average speed} = \frac{\Delta x}{\Delta t} = \frac{x_3 - x_0}{3 - 0}$$

$$= \frac{(50(3) + 10(3)^2) - 0}{3 - 0}$$

$$= \frac{150 + 90}{3} = \frac{240}{3}$$

$$= \boxed{80 \frac{\text{m}}{\text{s}}}$$

Method 2

$$\text{average speed} = \frac{v_2 + v_0}{2}$$

$$\text{where } v = \frac{dx}{dt} = 50 + 20(t)$$

$$\text{average speed} = \frac{[50 + 20(3)] + 50}{2}$$

$$= \frac{50 + 60 + 50}{2} = \frac{160}{2}$$

$$= \boxed{80 \frac{\text{m}}{\text{s}}}$$