

Key

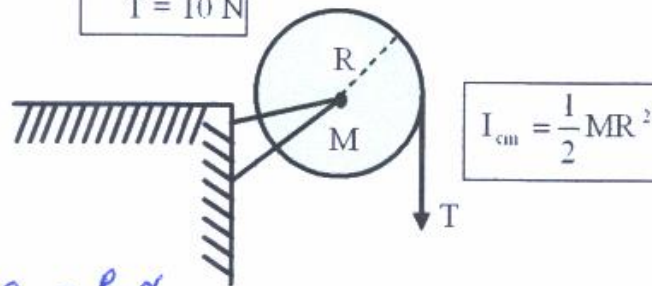
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1- A uniform disk of radius 50 cm and mass 4 kg is mounted on a frictionless axle, as shown. A light cord is wrapped around the rim of the disk and a steady downward pull of 10 N is exerted on the cord. Find the tangential acceleration of a point on the rim of the disk.

$M = 4 \text{ kg}$
 $R = 50 \text{ cm}$
 $T = 10 \text{ N}$



$$\tau = I \alpha$$

$$\alpha = \frac{\tau}{I} \quad \text{and} \quad a = R \alpha$$

$$\alpha = \frac{TR}{\frac{1}{2}MR^2}$$

$$\Rightarrow a = R \alpha = R \frac{T}{\frac{1}{2}MR} = \frac{T}{\frac{1}{2}M} = \frac{10}{\frac{1}{2} \times 4} = \boxed{5 \frac{\text{m}}{\text{s}^2}} \quad \downarrow \text{downward}$$

2- A torque of 0.8 Nm applied to a pulley increases its angular speed from 45 rev/min to 180 rev/min in 3 seconds. Find the moment of inertia of the pulley.

$$\tau = \hat{I} \alpha \Rightarrow \hat{I} = \frac{\tau}{\alpha}$$

apply: $\omega = \omega_0 + \alpha t$ to get $\alpha = \frac{\omega - \omega_0}{t} = 4.7 \frac{\text{rad}}{\text{s}^2}$

where $\omega_0 = \frac{45 \times 2\pi}{60} = 4.7 \frac{\text{rad}}{\text{s}}$

$\omega = 18.8 \frac{\text{rad}}{\text{s}}$

$$\Rightarrow \hat{I} = \frac{\tau}{\alpha} = \left(\frac{0.8}{4.7} \right) = \boxed{0.17 \text{ kg m}^2}$$