

17. All distances in this solution are understood to be in meters.

(a) $\vec{a} + \vec{b} = (4.0 + (-1.0))\hat{i} + ((-3.0) + 1.0)\hat{j} + (1.0 + 4.0)\hat{k} = 3.0\hat{i} - 2.0\hat{j} + 5.0\hat{k}.$

(b) $\vec{a} - \vec{b} = (4.0 - (-1.0))\hat{i} + ((-3.0) - 1.0)\hat{j} + (1.0 - 4.0)\hat{k} = 5.0\hat{i} - 4.0\hat{j} - 3.0\hat{k}.$

(c) The requirement $\vec{a} - \vec{b} + \vec{c} = 0$ leads to $\vec{c} = \vec{b} - \vec{a}$, which we note is the opposite of what we found in part (b). Thus, $\vec{c} = -5.0\hat{i} + 4.0\hat{j} + 3.0\hat{k}.$

26. The vector equation is $\vec{R} = \vec{A} + \vec{B} + \vec{C} + \vec{D}$. Expressing \vec{B} and \vec{D} in unit-vector notation, we have $1.69\hat{i} + 3.63\hat{j}$ and $-2.87\hat{i} + 4.10\hat{j}$, respectively. Where the length unit is not displayed in the solution below, the unit meter should be understood.

(a) Adding corresponding components, we obtain $\vec{R} = -3.18\hat{i} + 4.72\hat{j}$.

(b) and (c) Converting this result to polar coordinates (using Eq. 3-6 or functions on a vector-capable calculator), we obtain

$$(-3.18, 4.72) \longrightarrow (5.69 \angle 124^\circ)$$

which tells us the magnitude is 5.69 m and the angle (measured counterclockwise from $+x$ axis) is 124° .

37. From the figure, we note that $\vec{c} \perp \vec{b}$, which implies that the angle between \vec{c} and the $+x$ axis is 120° .

(a) Direct application of Eq. 3-5 yields the answers for this and the next few parts. $a_x = a \cos 0^\circ = a = 3.00 \text{ m}$.

(b) $a_y = a \sin 0^\circ = 0$.

(c) $b_x = b \cos 30^\circ = (4.00 \text{ m}) \cos 30^\circ = 3.46 \text{ m}$.

(d) $b_y = b \sin 30^\circ = (4.00 \text{ m}) \sin 30^\circ = 2.00 \text{ m}$.

(e) $c_x = c \cos 120^\circ = (10.0 \text{ m}) \cos 120^\circ = -5.00 \text{ m}$.

(f) $c_y = c \sin 120^\circ = (10.0 \text{ m}) \sin 120^\circ = 8.66 \text{ m}$.

(g) In terms of components (first x and then y), we must have

$$\begin{aligned} -5.00 \text{ m} &= p(3.00 \text{ m}) + q(3.46 \text{ m}) \\ 8.66 \text{ m} &= p(0) + q(2.00 \text{ m}) . \end{aligned}$$

Solving these equations, we find $p = -6.67$

(h) and $q = 4.33$ (note that it's easiest to solve for q first). The numbers p and q have no units.

53. (a) With $a = 17.0$ m and $\theta = 56.0^\circ$ we find $a_x = a \cos \theta = 9.51$ m.
- (b) And $a_y = a \sin \theta = 14.1$ m.
- (c) The angle relative to the new coordinate system is $\theta' = 56 - 18 = 38^\circ$. Thus, $a'_x = a \cos \theta' = 13.4$ m.
- (d) And $a'_y = a \sin \theta' = 10.5$ m.