

7. (a) The force of the worker on the crate is constant, so the work it does is given by  $W_F = \vec{F} \cdot \vec{d} = Fd \cos \phi$ , where  $\vec{F}$  is the force,  $\vec{d}$  is the displacement of the crate, and  $\phi$  is the angle between the force and the displacement. Here  $F = 210 \text{ N}$ ,  $d = 3.0 \text{ m}$ , and  $\phi = 20^\circ$ . Thus  $W_F = (210 \text{ N})(3.0 \text{ m}) \cos 20^\circ = 590 \text{ J}$ .
- (b) The force of gravity is downward, perpendicular to the displacement of the crate. The angle between this force and the displacement is  $90^\circ$  and  $\cos 90^\circ = 0$ , so the work done by the force of gravity is zero.
- (c) The normal force of the floor on the crate is also perpendicular to the displacement, so the work done by this force is also zero.
- (d) These are the only forces acting on the crate, so the total work done on it is  $590 \text{ J}$ .

19. (a) We use  $F$  to denote the magnitude of the force of the cord on the block. This force is upward, opposite to the force of gravity (which has magnitude  $Mg$ ). The acceleration is  $\vec{a} = g/4$  downward. Taking the downward direction to be positive, then Newton's second law yields

$$\vec{F}_{\text{net}} = m\vec{a} \implies Mg - F = M\left(\frac{g}{4}\right)$$

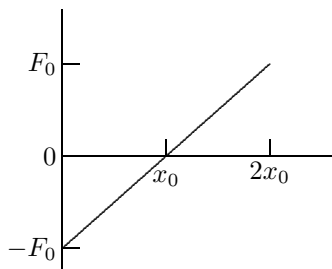
so  $F = 3Mg/4$ . The displacement is downward, so the work done by the cord's force is  $W_F = -Fd = -3Mgd/4$ , using Eq. 7-7.

- (b) The force of gravity is in the same direction as the displacement, so it does work  $W_g = Mgd$ .
- (c) The total work done on the block is  $-3Mgd/4 + Mgd = Mgd/4$ . Since the block starts from rest, we use Eq. 7-15 to conclude that this ( $Mgd/4$ ) is the block's kinetic energy  $K$  at the moment it has descended the distance  $d$ .
- (d) Since  $K = \frac{1}{2}Mv^2$ , the speed is

$$v = \sqrt{\frac{2K}{M}} = \sqrt{\frac{2(Mgd/4)}{M}} = \sqrt{\frac{gd}{2}}$$

at the moment the block has descended the distance  $d$ .

27. (a) The graph shows  $F$  as a function of  $x$  assuming  $x_0$  is positive. The work is negative as the object moves from  $x = 0$  to  $x = x_0$  and positive as it moves from  $x = x_0$  to  $x = 2x_0$ . Since the area of a triangle is  $\frac{1}{2}(\text{base})(\text{altitude})$ , the work done from  $x = 0$  to  $x = x_0$  is  $-\frac{1}{2}(x_0)(F_0)$  and the work done from  $x = x_0$  to  $x = 2x_0$  is  $\frac{1}{2}(2x_0 - x_0)(F_0) = \frac{1}{2}(x_0)(F_0)$ . The total work is the sum, which is zero.
- (b) The integral for the work is



$$W = \int_0^{2x_0} F_0 \left( \frac{x}{x_0} - 1 \right) dx = F_0 \left( \frac{x^2}{2x_0} - x \right) \Big|_0^{2x_0} = 0 .$$

40. The acceleration is constant, so we may use the equations in Table 2-1. We choose the direction of motion as  $+x$  and note that the displacement is the same as the distance traveled, in this problem. We designate the force (assumed singular) along the  $x$  direction acting on the  $m = 2.0$  kg object as  $F$ .

- (a) With  $v_0 = 0$ , Eq. 2-11 leads to  $a = v/t$ . And Eq. 2-17 gives  $\Delta x = \frac{1}{2}vt$  Newton's second law yields the force  $F = ma$ . Eq. 7-8, then, gives the work:

$$W = F\Delta x = m \left(\frac{v}{t}\right) \left(\frac{1}{2}vt\right) = \frac{1}{2}mv^2$$

as we expect from the work-kinetic energy theorem. With  $v = 10$  m/s, this yields  $W = 100$  J.

- (b) Instantaneous power is defined in Eq. 7-48. With  $t = 3.0$  s, we find

$$P = Fv = m \left(\frac{v}{t}\right) v = 67 \text{ W} .$$

- (c) The velocity at  $t' = 1.5$  s is  $v' = at' = 5.0$  m/s. Thus,

$$P' = Fv' = 33 \text{ W} .$$

44. Using Eq. 7-8, we find

$$W = \vec{F} \cdot \vec{d} = (F \cos \theta \hat{i} + F \sin \theta \hat{j}) \cdot (x \hat{i} + y \hat{j}) = Fx \cos \theta + Fy \sin \theta$$

where  $x = 2.0$  m,  $y = -4.0$  m,  $F = 10$  N, and  $\theta = 150^\circ$ . Thus, we obtain  $W = -37$  J. Note that the given mass value (2.0 kg) is not used in the computation.