

# EXAMPLE

## Drilling Hydraulics

### Pressure losses Due to friction

You are drilling a 9½ inch hole at 7000 ft using 5½ inch OD drill pipe (ID = 4.778 inch) and 500 ft of 6.5” x 2.5” drill collars. The well has 10¾ in, 40.5 lb/ft (ID =10.05 in) casing set at 3500 ft. Mud is pumped down the drill pipe at the rate of 850 gal/min. Mud properties are:

density = 10 ppg, viscosity = 2- cp,  
yield point = 20 lb/1.00 sq. ft. The bit has three 0.343 in ID nozzles.

1. Calculate the pressure drop in the drill pipe

Solution:-

$$\bar{V} = \frac{q}{A} = 850 \frac{\text{gal}}{\text{min}} \times \frac{\text{ft}^3}{7.48 \text{ gal}} \times \frac{1 \text{ min}}{60 \text{ sec}} \times \frac{4 \times 144}{\pi(4.778)^2} = 15.21 \text{ ft / sec.}$$

$$N_{Re} = \frac{928 \rho \bar{V} d}{\mu} = \frac{928 \times 10 \times 15.21 \times 4.778}{20}$$

$$33729 > 2100$$

∴ Flow is turbulent

From chart (Fig. 4.31)

$$f = 0.005$$

$$\Delta P_F = \frac{f \rho \bar{V}^2 L}{25.8 d} = \frac{0.005 \times 10 \times (15.21)^2 \times 6500}{25.8 \times 4.778}$$

$$= 609.9 \text{ Psi}$$

2. Calculate the flowing pressure at the top of the drill pipe if the pump pressure is 8000 psi.

Solution:-

From eq. 4.29

$$P_1 + .052\rho(D_2 - D_1) - 8.074 \times 10^{-4} \rho(V_2^2 - V_1^2) + \Delta P_p - \Delta P_f = P_2$$

$$P_1 = 0 \quad V_1 = 0 \quad , \quad D_1 - D_2 = 0$$

$$\Delta P_p = 8000 \text{ psi}$$

$$\rho = 10 \text{ ppg} \quad V_2 = 15.21 \text{ ft/sec}$$

$$\Delta P_f = 0 \text{ (surface lines)}$$

$$P_2 = 8000 - 8.074 \times 10^{-4} (10) (15.71)^2$$

$$= 8000 - 2 = 7998 \text{ psi}$$

3. Calculate the flowing pressure at the bottom of the drill pipe if the pump pressure is 8000 psi.

Solution:-

Using Eq. 4.24

$$P_1 = 0 \quad , \quad V_1 = 0, \quad V_2 = 15.21 \text{ ft/sec} \quad D_1 = 0 \quad , \quad D_2 = 7000 \text{ ft}$$

$$\Delta P_p = 8000 \text{ psi}$$

$$\Delta P_f = \Delta P_s + \Delta P_{dp} = 0 + 609.9 = 609.9 \text{ psi}$$

$$P_2 = 0 + 0.052(10)(7000 - 0) - 8.074 \times 10^{-4} (10) (15.21)^2 + 8000 - 609.9$$

$$= 0 + 3640 - 2 + 8000 - 610$$

$$= 11,028 \text{ psi}$$