

1. (a) Select the **value of each expression** in List I, from the values listed in List II:

List I (The Expression)	The Value
1. $\cos\left(\frac{2n+1}{2}p\right), n=0,\pm 1,\pm 2, \dots$	
2. $\sec^2 20^\circ - \tan^2 20^\circ$	
3. $\sqrt{\frac{1-\cos 40^\circ}{2}}$	
4. $\frac{\tan 115^\circ + \tan 5^\circ}{1 - \tan 115^\circ \tan 5^\circ}$	
5. $\cot 20^\circ \sec 20^\circ$	

List II
a) 1
b) $-\sqrt{3}$
c) $\tan 120^\circ$
d) 0
e) $\cos 20^\circ$
f) $\csc 20^\circ$
g) $\cos 70^\circ$

1. (b) Find the **exact value** of

i.  $\cos\left(\frac{19p}{12}\right)$

ii.  $5\cot(150^\circ) - 6\tan(-300^\circ)$

2. (a) If  $\tan x = -\sqrt{8}$ ,  $\frac{3\pi}{2} < x < 2\pi$ , find the **value** of  $\cos\left(\frac{x}{2}\right)$ .

2 (b) Verify the identity:  $2\csc 2q = \tan q + \cot q$

3. (a) Using the **reduction identity**, rewrite  $f(x) = \frac{\sqrt{3}}{2} \sin 2x - \frac{1}{2} \cos 2x$ :

Also, find:

- i. **range** of  $f$ .
- ii. **period** of  $f$ .
- iii. **amplitude** of  $f$ .
- iv. **phase shift** of  $f$ .

3. (b) **Verify the identity**:  $\frac{1}{1-\sin q} + \frac{1}{1+\sin q} = 2\sec^2 q$

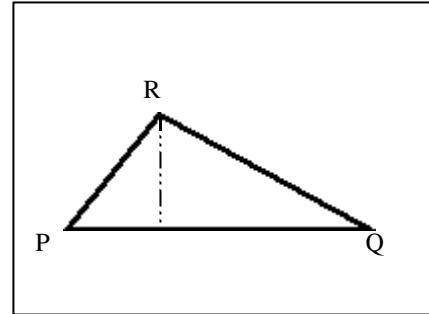
4. (a) i. If  $\mathbf{a} + \mathbf{b} = \mathbf{p}$ , find  $\cos \mathbf{a} + \cos \mathbf{b}$ .

ii. Use part (i) to find the value of

$$\cos\left(\frac{\mathbf{p}}{5}\right) + \cos\left(\frac{2\mathbf{p}}{5}\right) + \cos\left(\frac{3\mathbf{p}}{5}\right) + \cos\left(\frac{4\mathbf{p}}{5}\right) + \cos\left(\frac{5\mathbf{p}}{5}\right)$$

4. (b) Given  $\tan \mathbf{a} = -\frac{3}{4}$  for  $\mathbf{a}$  in Quadrant II and  $\csc \mathbf{b} = -\frac{5}{4}$  for  $\mathbf{b}$  in Quadrant IV, **find**  $\sec(\mathbf{a} - \mathbf{b})$

5. (a) The following figure shows that **two ships** are at points **P** and **Q** and also, an **airplane** is at **point R**. When the airplane is at the **height** of 3500 ft, the **angle of depression** from airplane to P is  $45^\circ$  and to Q is  $30^\circ$ . **Find the distance between the two ships.**



5. (b) Find the **solution set** of the equation  $\cos^2 2x - 2\cos 2x = 3$  in the interval  $p \leq x \leq 4p$ .

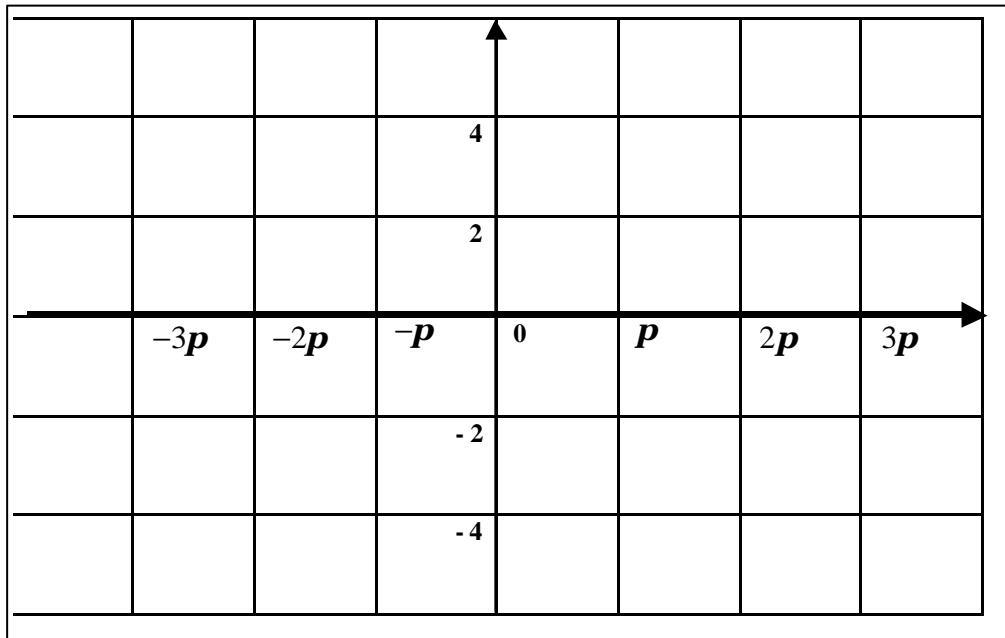
6. (a) If  $f(x) = 4\cos\left(\frac{1}{2}x + \frac{p}{4}\right)$ , then find its

i. **amplitude**

ii. **period**

iii. **phase shift**

Also, **draw the graph** of the function  $f$  over **one cycle**



6. (b) The **graph** of the function

$$f(x) = 2\cot(bx + c)$$

has **period**  $\frac{2p}{3}$  and **phase shift**  $\frac{p}{2}$  to the left. **Find**  $f(p)$ .

