

Q.1: Find the value of $\csc\left(-\frac{7\pi}{3}\right) \cot\left(\frac{11\pi}{4}\right) + \cos\left(\frac{25\pi}{3}\right) \cos(810^\circ)$

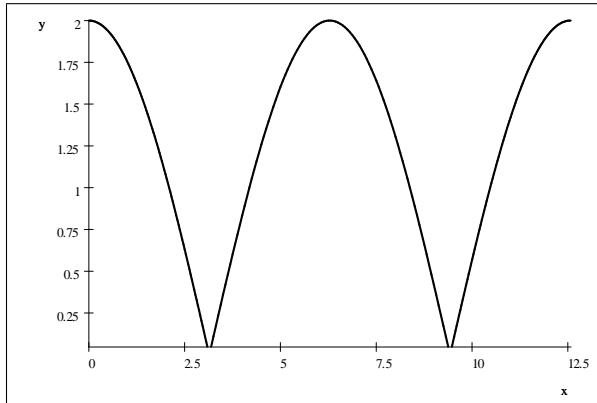
$$\begin{aligned} \text{Sol: } \csc\left(-\frac{7\pi}{3}\right) \cot\left(\frac{11\pi}{4}\right) + \cos\left(\frac{25\pi}{3}\right) \cos(810^\circ) &= \csc\left(-\frac{\pi}{3}\right) \cot\left(\frac{3\pi}{4}\right) + \cos\left(\frac{\pi}{3}\right) \cos(90^\circ) \\ &= \left(-\csc\left(\frac{\pi}{3}\right)\right) \left(-\cot\left(\frac{\pi}{4}\right)\right) + \cos\left(\frac{\pi}{3}\right) \cos(90^\circ) \\ &= -\frac{2}{\sqrt{3}}(-1) + \frac{1}{2}(0) = -\frac{2\sqrt{3}}{3}. \end{aligned}$$

Q.2: Evaluate $W\left(\frac{15\pi}{3}\right)$.

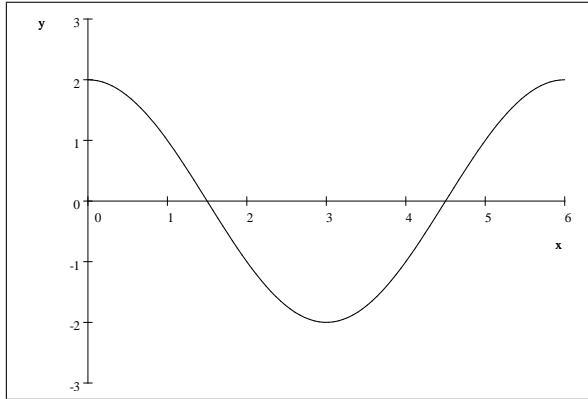
$$\begin{aligned} \text{Sol: } x &= \cos\left(\frac{15\pi}{3}\right) = \cos(5\pi) = \cos(\pi) = -1 \\ y &= \sin\left(\frac{15\pi}{3}\right) = \sin(5\pi) = \sin(\pi) = 0. \end{aligned}$$

Q.3: Sketch the graph of $y = |2 \cos\left(\frac{x}{2}\right)|$. Show all steps.

$$\text{Sol: } \text{Period } P = \frac{\pi}{\frac{1}{2}} = 2\pi, \text{ Amplitude } A = 2.$$



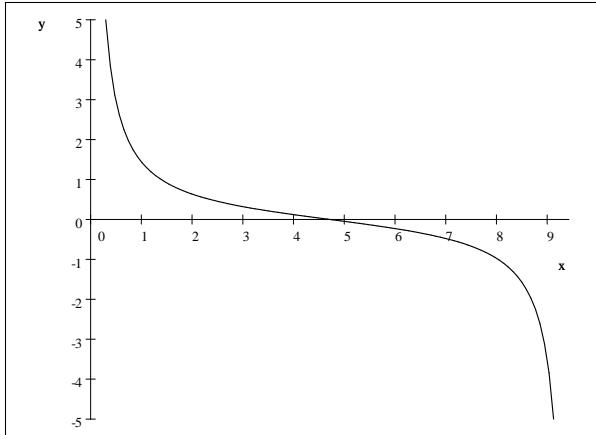
Q.4: Find the trigonometric function whose graph over one period is:



$$\begin{aligned} \text{Sol: } \text{Period } P &= 6 = \frac{2\pi}{b} \Rightarrow b = \frac{\pi}{3} \\ \text{Amplitude } A &= 2 \Rightarrow a = 2, \\ f(x) &= 2 \cos\left(\frac{\pi}{3}x\right). \end{aligned}$$

Q.5: Sketch the graph of $y = \frac{1}{2} \cot\left(\frac{x}{3}\right)$ over one period interval.

Sol: Period $P = \frac{\pi}{\frac{1}{3}} = 3\pi$,



Q.6: Write period, amplitude, phase-shift and sketch the graph of $y = 2 - 3 \sin\left(2x - \frac{\pi}{2}\right)$ over one full period of the function.

Sol: Period $P = \frac{2\pi}{2} = \pi$, Amplitude $A = 3$, Phase Shift $F = -\frac{-\frac{\pi}{2}}{2} = \frac{\pi}{4}$, Vertical Translation $V = 2$.

