

**9.19.**

- a. The hypotheses are:  $H_0: \mu_1 = \mu_2$  vs.  $H_A: \mu_1 \neq \mu_2$

$$s_p = \sqrt{\frac{(16-1)32^2 + (25-1)30^2}{16+25-2}} = 30.785$$

Reject  $H_0$  if  $t < -2.0227$  or  $t > 2.0227$ .

- b.  $t = \frac{(2,456 - 2,460) - 0}{30.785 \sqrt{\frac{1}{16} + \frac{1}{25}}} = -.4058$ : Do not reject  $H_0$ .

**9.20.**

- a. The hypotheses are:  $H_0: \mu_1 = \mu_2$  vs.  $H_A: \mu_1 \neq \mu_2$

$$df = 25 + 20 - 2 = 43$$

If  $t > 2.0167$  or  $t < -2.0167$  reject  $H_0$ , otherwise do not reject  $H_0$ .

- b.  $s_p = \sqrt{\frac{(25-1)20^2 + (20-1)24^2}{25+20-2}} = 21.858$

$$t = \frac{(430 - 405) - 0}{21.858 \sqrt{\frac{1}{25} + \frac{1}{20}}} = 3.812$$

Since  $3.812 > 2.0167$  reject  $H_0$

**9.22.**

- a. The hypotheses are:  $H_0: \mu_1 - \mu_2 \leq 0$  vs.  $H_A: \mu_1 - \mu_2 > 0$   
 $df = 75 + 80 - 2 = 153$

The Decision Rule is: If  $z > 1.645$  reject  $H_0$ , otherwise do not reject  $H_0$

- b.  $z = \frac{(5.30 - 5.10) - 0}{\sqrt{\frac{2.20^2}{75} + \frac{2.644^2}{80}}} = 0.513$

Since  $.513 < 1.645$  do not reject  $H_0$

**9.25.**

- $H_0: \mu_F - \mu_M \leq 1$  vs.  $H_A: \mu_F - \mu_M > 1$

$$df = 60 + 60 - 2 = 118$$

$$z = \frac{(14.65 - 13.24) - 1}{\sqrt{\frac{1.2^2}{60} + \frac{1.56^2}{60}}} = 1.6136$$

Since  $1.6136 < 1.645$  do not reject  $H_0$  and conclude that the difference is not greater than 1.

**9.35.** Decision Rule:

If  $z > 1.645$  or  $z < -1.645$  reject  $H_0$ , otherwise do not reject  $H_0$

$$\bar{p} = (87+80)/(200+150) = 0.4771, \bar{p}_1 = 87/200 = 0.435 \text{ and } \bar{p}_2 = 80/150 = 0.5333$$

$$z = [(0.435 - 0.5333) - 0.05] / \sqrt{(0.435(1 - 0.435)/200) + (0.5333(1 - 0.5333)/150)} = -2.7594$$

Since  $z = -2.7594 < -1.645$  reject  $H_0$ , and conclude that the difference in the population proportions is not equal to 0.05.

**9.37.**

a. Decision Rule:

If  $z > 2.05$  reject  $H_0$ , otherwise do not reject  $H_0$

$$\bar{p} = (30+24)/(60+80) = 0.3857, \bar{p}_1 = 30/60 = 0.5 \text{ and } \bar{p}_2 = 24/80 = 0.3$$

$$z = [(0.5 - 0.3) - 0] / \sqrt{(0.3857)(1 - 0.3857)[(1/60) + (1/80)]} = 2.4059$$

Since  $z = 2.4059 > 2.05$  reject  $H_0$ , and conclude there is a difference in the population proportions.

b. Looking in the standard normal table we see area associated with  $z = 2.41$  is .4920. So the p-value is .00800 which is less than  $\alpha = .02$  and again reject  $H_0$ .

**9.40.**

a.  $H_0: p_p - p_g = 0$  vs.  $H_A: p_p - p_g \neq 0$

$$n_1 \bar{p}_1 = 22 > 5; n_1(1 - \bar{p}_1) = 48 > 5 \text{ and } n_2 \bar{p}_2 = 19 > 5; n_2(1 - \bar{p}_2) = 31 > 5$$

Decision Rule:

If  $z > 1.96$  or  $z < -1.96$  reject  $H_0$ , otherwise do not reject  $H_0$

$$\bar{p} = (22+19)/(70+50) = 0.3417, p_p = 22/70 = 0.3143 \text{ and } p_g = 19/50 = 0.38$$

$$z = [(0.3143 - 0.38) - 0] / \sqrt{(0.3417)(1 - 0.3417)[(1/70) + (1/50)]} = -0.7481$$

Since  $z = -0.7481 > -1.96$  do not reject  $H_0$ , and conclude that there is no difference in the proportion of employees who give to United Way depending on whether the employer is a private business or a government agency.