

(Credit will be given only for Correct Solution: Show All work)

**QI.** Consider the following matrix

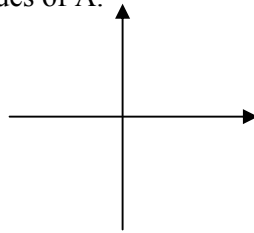
$$A = \begin{bmatrix} d_1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 3|d_3 - d_4| & 2|d_3 - d_4| \\ 0 & 0 & 2|d_3 - d_4| & 0 \end{bmatrix},$$

where  $d_i$  = i-th digit of your ID Number.

1) Rewrite the matrix A:  $A = \begin{bmatrix} \square & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & \square & \square \\ 0 & 0 & \square & 0 \end{bmatrix}$

(2) Describe and sketch the Gerschgorin's Circles C1, C2, C3, C4 for the eigenvalues of A.

	C1	C2	C3	C4
Center				
Radius				



(3) Find the eigenvalues of A.

4) Find a matrix Q such that  $Q^{-1}AQ = \text{Diag}(\lambda_i)$

[Diag  $(\lambda_i)$  is the diagonal matrix with eigen values of A as Diagonal entries] Solve this problem on the back of the paper. Show all necessary work.

**QII.** Find a set from the following vectors which forms a largest set of Linearly independent vectors:

$$v_1 = [0, d_3, d_4, 0], v_2 = [0, d_3, d_2, 0], v_3 = [1, d_3, d_5, 0]$$

$$v_4 = [1, d_3, d_4, 0], v_5 = [0, d_5, d_4, 1]$$