

Math 102 Sem II (052) Second Major Exam Wed 26 / 4 / 2006 Time $1\frac{1}{4}$ hours

Answer all the questions

Show all of your work

Question #	1	2	3	4	5	6	7	8	Total
Grade	/5	/5	/5	/5	/5	/5	/5	/5	/40

1. Find the arclength of the parametric curve $y = e^t \sin t$, $x = e^t \cos t$ from $t = 0$ to $t = 1$
2. $x \tan^{-1} x dx$
3. Find the surface area generated if the curve $y = \cosh x$, $0 \leq x \leq 2$ is revolving about the y axis.
4. $\int_{x=0}^{x=1} \frac{2}{1-x^2} dx$
5. Determine if the sequence $\frac{3-2n}{3n}^n$ is convergent or divergent, if convergent find the limit.

Math 102 Sem II (052) First Major Exam Wed 22 / 3 / 2006 Time $1\frac{1}{4}$ hours

Question #	1a	1b	1c	2	3	4	5	6	7	Total
Grade	/4	/4	/4	/4	/5	/5	/5	/4	/5	/40

1. Integrate each of the following:
 - a. $\int_{x=1}^{x=4} \frac{x^3 - 3x - 2}{\sqrt{x}} dx$
 - b. $\int_{x=0}^{x=\pi/2} \frac{\cos 2x}{\sqrt{4 - 3 \sin 2x}} dx$
 - c. $\int_{x=1}^{x=2} 3x^2 dx$
2. Find the derivative $\frac{d}{dx} \left[\int_{x=0}^{x=t} \frac{t^3 - 3}{t^2 - 1} dt \right]$
3. Find the area of the region bounded by $y = x^2$, $y = 4x - 4$, and $y = 0$
4. Find the volume generated if the region bounded by the curves $y = x^3$, $x = 1$, $y = 0$ is revolving about the x axis
5. Express the Riemann Sum $\lim_{n \rightarrow \infty} \sum_{k=1}^n \frac{n}{n^2 - k^2}$ over the interval $[0, 1]$ as a definite integral and solve it
6. Find the volume generated if the region bounded by the curves $y = x^2$, $y = x - 2$, is revolving about the line $x = 1$
7. $\int_{x=0}^{x=\ln 2} \frac{1}{1 - e^{-x}} dx$