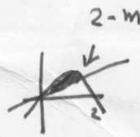


$$\boxed{1} \quad A = \int_0^2 (2x - x^2) dx = \frac{4}{3}$$

$$\frac{A}{2} = \int_0^{2-m} (2x - x^2 - mx) dx = \frac{1}{6} (2-m)^3 = \frac{A}{2} = \frac{4/3}{2} = \frac{4}{6}$$

$$\Rightarrow (2-m)^3 = 4 \Rightarrow 2-m = \sqrt[3]{4} \Rightarrow m = 2 - \sqrt[3]{4}.$$



$$\boxed{2} \text{ disks } V = \pi \int_{-1}^1 [1-y^2]^2 dy = \pi \int_{-1}^1 1 - 2y^2 + y^4 dy$$

$$= \pi \left[ y - \frac{2y^3}{3} + \frac{y^5}{5} \right]_{-1}^1 = \pi \frac{16}{15}$$

$$\text{Shells } V = 2\pi \int_0^1 x [\sqrt{1-x} - (-\sqrt{1-x})] dx$$

$$= 2\pi \int_0^1 x 2\sqrt{1-x} dx = 4\pi \int_0^1 x \sqrt{1-x} dx \quad u = 1-x \\ du = -dx$$

$$= 4\pi \int_1^0 (1-u) \sqrt{u} (-du) = 4\pi \int_0^1 (1-u) \sqrt{u} du \quad x = 1-u$$

$$= 4\pi \int_0^1 u^{1/2} - u^{3/2} du = 4\pi \left[ \frac{2u^{3/2}}{3} - \frac{2u^{5/2}}{5} \right]_0^1$$

$$= 4\pi \left[ \frac{2}{3} - \frac{2}{5} \right] = \pi \frac{16}{15}.$$

$$\boxed{3} \quad \int_1^2 2\pi x^3 \sqrt{1+9x^4} dx =$$

$$u = 1+9x^4 \quad u(1) = 10$$

$$du = 36x^3 dx \quad u(2) = 145$$

$$S = \frac{2\pi}{36} \int_{10}^{145} \sqrt{u} du = \frac{2\pi}{36} \left[ \frac{2u^{3/2}}{3} \right]_{10}^{145} = \frac{4\pi}{108} \left( 145^{\frac{3}{2}} - 10^{\frac{3}{2}} \right) \\ = \frac{\pi}{27} (145^3 - 10^3).$$

$$\boxed{4} \quad \int \coth^2 x \operatorname{csch}^2 x dx$$

$$u = \coth x \\ du = -\operatorname{csch}^2 x dx$$

$$= - \int u^2 du = -\frac{u^3}{3} + C$$

$$= -\frac{\coth^3 x}{3} + C.$$

$$\square \text{ Eq. of the line } y - \frac{1}{2} = \frac{3}{5\pi}(x - \frac{5\pi}{6}) = \frac{3}{5\pi}x - \frac{1}{2} \Rightarrow y = \frac{3}{5\pi}x$$

Solving the two

$$\Rightarrow \sin x = \frac{3}{5\pi}x \Rightarrow x = \frac{5\pi}{6}$$

$$y = \sin x$$

$$\frac{5\pi}{6}$$

$$A = \int_0^{\frac{5\pi}{6}} \sin x - \frac{3}{5\pi}x dx = \frac{\sqrt{3}}{2} - \frac{5\pi}{24} + 1.$$



$$\square \text{ disks } V = \pi \int_{-1}^1 [1-y^2]^2 dy = \pi \int_{-1}^1 1-2y^2+y^4 dy = \pi \left[ y - \frac{2y^3}{3} + \frac{y^5}{5} \right]_{-1}^1 = \pi \frac{16}{15}$$

Shells

$$V = 2\pi \int_0^1 x (\sqrt{1-x} - (-\sqrt{1-x})) dx$$

$$\Rightarrow 2\pi \int_0^1 x 2\sqrt{1-x} dx = 4\pi \int_0^1 x \sqrt{1-x} dx \quad u = 1-x \\ du = -dx$$

$$\Rightarrow 4\pi \int_1^0 (1-u)\sqrt{u} (-du) = 4\pi \int_0^1 (1-u)\sqrt{u} du \quad x = 1-u$$

$$\Rightarrow 4\pi \int_0^1 u^{1/2} - u^{3/2} du = \pi \frac{16}{15}$$

$$\textcircled{3} \quad S = \int_1^4 2\pi \sqrt{x} \sqrt{1 + \frac{1}{4x}} dx = 2\pi \int_1^4 \sqrt{x + \frac{1}{4}} dx = 2\pi \frac{2(x + \frac{1}{4})}{3} \Big|_1^4$$

$$= \frac{4\pi}{3} \left\{ \left[ 4 + \frac{1}{4} \right]^{\frac{3}{2}} - \left[ 1 + \frac{1}{4} \right]^{\frac{3}{2}} \right\} =$$

$$\textcircled{4} \quad \int \tanh^2 x \operatorname{sech}^2 x dx \quad u = \tanh x$$

$$du = \operatorname{sech}^2 x dx$$

$$\int u^2 du = \frac{u^3}{3} + C = \frac{\tanh^3 x}{3} + C.$$

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1 Find a formula for the general term of the sequence  $r, -r^3, r^5, -r^7, \dots$

$$\left\{ (-1)^n r^{2n+1} \right\}_{n=0}^{\infty}$$

2. Find the limit of the sequence  $\left\{ \frac{n}{n+2} \right\}_{n=1}^{\infty}$

$$\lim_{n \rightarrow \infty} \frac{n}{n+2} = 1$$

3. Is the sequence  $\left\{ \frac{2^n}{1+2^n} \right\}_{n=1}^{\infty}$  decreasing or increasing.

Increasing

$$\frac{a_{n+1}}{a_n} = \frac{\frac{2^{n+1}}{1+2^{n+1}}}{\frac{2^n}{1+2^n}} = \frac{2^{n+1}}{1+2^{n+1}} \cdot \frac{1+2^n}{2^n} = \frac{2 + 2^{2n}}{1 + 2^{2n}} > 1$$

3. Is the series  $\sum_{n=1}^{\infty} \frac{4^{k-3}}{7^{k-1}}$  converges or diverges if converges find its sum.

G. S. with  $r = \frac{4}{7}$   $a = \frac{1}{16}$

$$S = \frac{\frac{1}{16}}{1 - \frac{4}{7}}$$