

Name:	I.D.	Sec.	
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48/7.3 Evaluate  $\int \cot x dx$

$$\int \frac{\cos x}{\sin x} dx \quad u = \sin x \quad du = \cos x dx$$

$$= \int \frac{1}{u} du = \ln |u| + c = \ln |\sin x| + C$$

44/7.2 Find an equation of the curve that satisfies each point  $(x,y)$  on the curve the slope equals the square of the distance between the point and the y-axis the point  $(-1,2)$  is on the curve.

$$y' = x^2 \Rightarrow y = \frac{x^3}{3} + C \quad \text{at } (-1,2) \quad C = \frac{7}{3}$$

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30/7.4 Let  $S = \sum_{k=0}^n ar^k$ . Show that  $S - rS = a - ar^{n+1}$ .

$$\begin{aligned}
 S &= ar^0 + ar^1 + \dots + ar^n \\
 -rS &= -ar^1 - ar^2 - \dots - ar^{n+1} \\
 S - rS &= a - ar^{n+1}
 \end{aligned}$$

2. Find the maximum and minimum bounds of the integral  $\int_0^3 x^3 + 2 \, dx$

$$\begin{aligned}
 \max f(x) &= x^3 + 2 \\
 &\text{is } 29 \text{ at } x=3 \\
 \min &\text{ is } 2 \text{ at } x=0
 \end{aligned}$$

$$(3)(2) \leq \int_0^3 x^3 + 2 \, dx \leq (3)(29)$$

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40/7.4 Show that the sum of the first  $n$  consecutive positive odd integers is  $n^2$ .

$$1 + 3 + \dots + 2k-1$$

$$\sum_{k=1}^n 2k-1 = 2 \sum_{k=1}^n k - 1 = 2 \frac{n(n+1)}{2} - n = n^2 + n - n = n^2$$

2. Find the maximum and minimum bounds of the integral  $\int_0^{\pi} \sin x \, dx$



$$\text{#} \int_0^{\pi} \sin x \, dx \leq 1 \quad (\text{#})$$

$$0 \leq \int_0^{\pi} \sin x \, dx \leq 1 \quad (\pi)$$

