

MATH 102
Bonus HW

Q1. Determine whether the following series converges, and if so find its sum

$$\frac{1}{1 \cdot 2} + \frac{3}{2 \cdot 5} + \frac{5}{5 \cdot 10} + \frac{7}{10 \cdot 17} + \cdots + \frac{2k-1}{[(k-1)^2+1](k^2+1)} + \cdots$$

Q2. Find all values of x for which the following series converges

$$\sum_{k=0}^{\infty} 2^k \sin^k x$$

Q3. Test for convergence:

$$\sum_{k=1}^{\infty} \frac{1 \cdot 3 \cdot 5 \cdots (2k-1)}{2 \cdot 5 \cdot 8 \cdots (3k-1)}$$

Q4. Determine whether the following series converges, and if so find its sum

$$\frac{1}{2} - \frac{1}{3} + \frac{1}{2^2} - \frac{1}{3^2} + \frac{1}{2^3} - \frac{1}{3^3} + \cdots$$

Q5. Test for convergence:

$$\sum_{k=1}^{\infty} \frac{\ln \sqrt{3k-1}}{\sqrt{k} \sqrt{k^3+5k+2}}$$