

- All possible zeros of the polynomial  $p(x) = 2x^5 - 2x^4 + 7x^3 - 8x^2 + 4x - 16$  are (Sec 3.3): 1)  $\pm 1, \pm \frac{1}{2}, \pm 2, \pm 4, \pm 8, \pm 16$  2)  $\pm 1, \pm 2, \pm 4, \pm 8, \pm 16$  3)  $\pm 1, \pm \frac{1}{2}, \pm \frac{1}{4}, \pm \frac{1}{8}, \pm \frac{1}{16}$  4)  $\pm 1, \pm \frac{1}{2}, \pm 2, \pm \frac{1}{4}, \pm \frac{1}{8}, \pm \frac{1}{16}$
- The horizontal asymptote(s) of  $f(x) = \frac{3(x-4)(2x+3)}{x^2-9}$  is (are) given by (Sec 3.5): 1)  $y = 8$  2)  $y = 3$  3)  $y = 0$  4)  $y = 6$
- The smallest positive integer detected by the "Bounds Theorem" as an upper bound for the real zeros of  $p(x) = 2x^3 + 4x^2 - 8x + 3$  is (Sec 3.3): 1) 2 2) 4 3) 3 4) 1
- Use the Descartes' Rule of Signs to discuss the nature of all zeros of  $p(x) = 4x^4 - 7x^3 + 3x + 2$ . Write all possibilities in a table. (Sec 3.3)
- Use the Descartes' Rule of Signs to discuss the nature of all zeros of  $p(x) = 2x^5 - 5x^4 - 12x^3 + 3x^2 - 14x + 8$ . Write all possibilities in a table. (Sec 3.3)
- Given that  $3i$  is a zero of multiplicity 2 of  $p(x) = x^5 - x^4 + 18x^3 - 18x^2 + 81x - 81$ . Find the other zeros. (Sec 3.4)
- Find the solution of the equation  $\frac{1}{2}x^3 + \frac{1}{6}x^2 - \frac{4}{3}x + \frac{2}{3} = 0$ . (Sec 3.3)
- Find a polynomial  $p(x)$  of degree 6 such that  $-3, 1,$  and  $2$  are its only zeros, its graph is above the x-axis between  $1$  and  $\infty$ , below the x-axis between  $-\infty$  and  $1$ , and  $p(0) = -9$ . [Hint, Draw a rough graph of  $p(x)$ ] (Sec 3.2)
- Consider the rational function  $f(x) = \frac{x^3 - 4x}{x^2 - 3x + 2}$ . a) Find all asymptotes, if any, of  $f(x)$ . b) Find the x-intercept(s), y-intercept and the hole(s), if any, of  $f(x)$ . c) Sketch the graph of  $f(x)$ . [Note: you must use all of the information obtained in (9a) and (9b)] (Sec 3.5)
- A monic polynomial has real coefficients and the lowest possible degree. Two of its zeros are  $3$  and  $2 + i$ . This polynomial must be one of the following: (Sec 3.4) 1)  $x^3 - 7x^2 + 15x - 9$  2)  $x^3 + x^2 - 13x + 3$  3)  $x^3 - 3x^2 + 5x - 15$  4)  $x^3 - 7x^2 + 17x - 15$  5)  $x^3 - 3x^2 + 4x - 12$
- The zeros of the polynomial  $x^3 - 23x^2 + 167x - 385$  are all positive integers. What is the sum of the zeros? (Sec 3.3) 1) 23 2) 6 3) 18 4) 12 5) 16
- The graph of  $y = \frac{x^2 + 1}{ax^2 + bx + c}$  has a horizontal asymptote  $y = 1$  and two vertical asymptotes given by  $x = -3$  and  $x = 1$ . What is the value of  $2d + b + c$ ? (Sec 3.5) 1)  $-6$  2)  $1$  3)  $6$  4)  $-7$  5)  $-3$
- To apply the Rational Zeros Theorem on a polynomial  $p(x)$ , all coefficients of  $p(x)$  should be (Sec 3.3) 1) Real numbers 2) Nonreal numbers 3) Real or nonreal numbers 4) Integers

14. If  $f(x) = \frac{p(x)}{q(x)}$  is a rational function and  $a$  is a real number, then  $x = a$  is a vertical asymptote of the graph of  $f(x)$  if (Sec 3.5) 1)  $p(a) = 0$  and  $q(a) \neq 0$  2)  $p(a) = 0$  and  $q(a) = 0$  3)  $p(a) \neq 0$  and  $q(a) = 0$  4)  $p(a) \neq 0$  and  $q(a) \neq 0$
15. Let  $p(x)$  be a polynomial with real coefficients. If  $U$  is an upper bound for all real zeros of  $p(x)$ ,  $L$  is a lower bound for all real zeros of  $p(x)$ , and  $C$  is a real zero of  $p(x)$  such that  $U \neq L \neq C$ , then (Sec 3.3): 1)  $L < C < U$  2)  $U < C < L$  3)  $L < U < C$  4)  $U < L < C$
16. Find the solution set of the equation  $x^4 + x^3 - 2x^2 - 6x - 4 = 0$ . (Sec 3.3)
17. Graph the polynomial function  $p(x) = x^2(4x^2 - 1)$  (Showing all intercepts) (Sec 3.2)
18. If  $2 + i$  is a zero of  $p(x) = x^4 - 4x^3 + 6x^2 - 4x + 5$ , find the other zeros. (Sec 3.4)
19. Given the rational function  $f(x) = \frac{x^3 - 2x^2 - 3x}{x^3 - x}$  1) Find all asymptotes and missing points 2) Graph  $f(x)$  (Sec 3.5)
20. Let  $f(x) = \frac{ax^2 + 2x - 4}{x^2 - b}$ . If  $x = -1$  and  $y = 2$  are vertical and horizontal asymptotes of  $f(x)$ , then the graph has a hole or missing point at (Sec 3.5) 1)  $(-1, 0)$  2)  $(1, 0)$  3)  $(-2, 1)$  4)  $(3, 1)$  5)  $(1, 3)$
21. If  $2 - i$  is a zero with multiplicity two of  $p(x) = x^5 - 9x^4 + 34x^3 - 66x^2 + 65x - 25$ , then the sum of the non real zeros is: (Sec 3.4) 1)  $-9$  2)  $8$  3)  $8 - 4i$  4)  $8 + 4i$  5)  $4i$
22. The sum of all real zeros of  $6x^4 - x^3 + 5x^2 - x - 1$  is (Sec 3.3) 1)  $0$  2)  $\frac{1}{6}$  3)  $1$  4)  $-\frac{1}{6}$  5)  $\frac{5}{6}$
23. The graph of the polynomial  $p(x) = (1 - x)(x^2 - 3x + 2)$  is above the x-axis on (Sec 3.2) 1)  $(-\infty, -1) \cup (1, 2)$  2)  $(1, 2)$  3)  $(-\infty, 2)$  4)  $(-\infty, -1) \cup (1, 2)$  5)  $(2, \infty)$
24. The degree of a polynomial of lowest degree with real coefficients and has zeros 3 (of multiplicity 2),  $2 - i$  (of multiplicity 4), and  $1 + \sqrt{2}$  is (Sec 3.4): 1) 6 2) 11 3) 8 4) 12 5) 5
25. The sum of all integer zeros of the polynomial  $f(x) = x^3 - \frac{4}{3}x^2 + \frac{5}{3}x + \frac{2}{3}$  is (Sec 3.3): 1) 0 2) 3 3)  $-3$  4)  $-1$  5) 1
26. A polynomial  $p(x)$  of least degree such that the graph of  $p(x)$  crosses the x-axis at  $x = 3$ , touches x-axis at  $x = 1$ , and has y-intercept 6 is: 1)  $-2x^3 + 10x^2 - 14x + 6$  2)  $-2x^3 + 2x^2 + 10x + 6$  3)  $-2x^3 - 5x^2 + 7x + 6$  4)  $2x^2 - 8x + 6$  5)  $\frac{2}{3}(x^3 - 7x^2 + 15x + 9)$