

KING FAHD UNIVERSITY OF PETROLEUM & MINERALS
Department of Mathematical Sciences

Math 301 Method of Applied Mathematics

Major Exam # 1

Term 061

Time Allowed 60 minutes

Name _____ ID # _____ Section # _____

| Q # | Grade |
|-------|-------|
| 1 | / 5 |
| 2 | / 4 |
| 3 | / 5 |
| 4 | / 6 |
| Total | / 20 |

Important Note

Show all work.

Use of programmable calculator is not allowed.

Mobiles and paging devices should not be carried during examination.

Instructor: F. D. Zaman

Q # 1(a) Let $\underline{\mathbf{r}}$ be the position vector and $\underline{\mathbf{a}}$ a constant vector. Show the following
 $\nabla \cdot [(\underline{\mathbf{r}} \cdot \underline{\mathbf{r}})\underline{\mathbf{a}}] = 2(\underline{\mathbf{r}} \cdot \underline{\mathbf{a}}).$ (2)

Q1(b) Evaluate the integral

$\int_C 2xydx - 4ydy + e^{xy} dz$ where C is the curve $x = 2t, y = \sqrt{t}, z = 4, t = 0,1.$

(3)

Q2) Show that the integral is independent of path and hence evaluate it along any path

$$\int_{(2,1)}^{(3,4)} \frac{ydx - (x + y^3)dy}{y^2}. \quad (4)$$

Q 3) Use Green's theorem to evaluate the given line integral along the curve in the first quadrant formed by graphs of $y = 0, x = y^2, x = 8 - y^2$ **(5)**

$$\oint_C \frac{x^3 + y^3}{3} dx + (xy + xy^2) dy.$$

Q4) Find the integral giving flux of the vector field $\underline{\mathbf{F}}=z \underline{\mathbf{k}}$ through the surface S formed by the portion of the paraboloid $z = 5 - x^2 - y^2$ inside the cylinder $x^2 + y^2 = 4$. **(6)**