

King Fahd University of Petroleum and Minerals
Department of Mathematical Sciences
Math 301 Exam I
Semester I, 2006- (06I)
Dr. Faisal Fairag

Serial NO:	
ID:	
Name:	

FORM **A**

Q		Points
1		6
2		4
3		9
4		4
5		5
6		13
7		12
8		12
9		12
10		20
11		33
Total		130

Say a prayer & Good luck 😊

1) Find $L[f(t)]$ where

$$f(t) = t^2 - e^{-9t} + 5$$

2) Find the directional derivative of $f(x, y) = (xy + 1)^2$ at the point (3,2) in the direction of (5,3).

3) Given that $F(x, y, z) = xi + yj + zk$ and $G(x, y, z) = yi + xk$

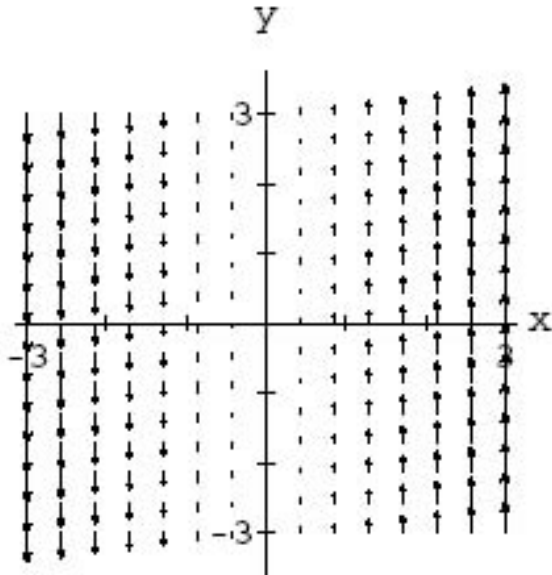
(a) Find $\text{div}(F \times G) =$

(b) Find $G \cdot \text{curl}F - F \cdot \text{curl}G =$

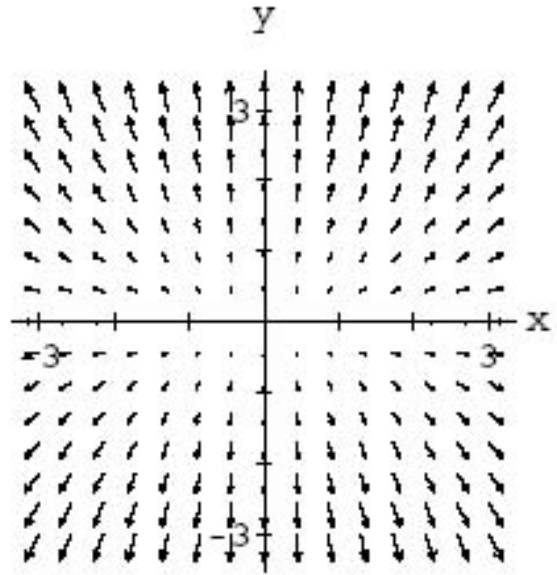
4) Find a vector that gives the direction in which the function $F(x, y, z) = x^2 + 4xz + 2yz^2$ increases most rapidly at the point (1,0,-1) .

5) The graph of the vector field $F(x, y) = -xi + yj$ is

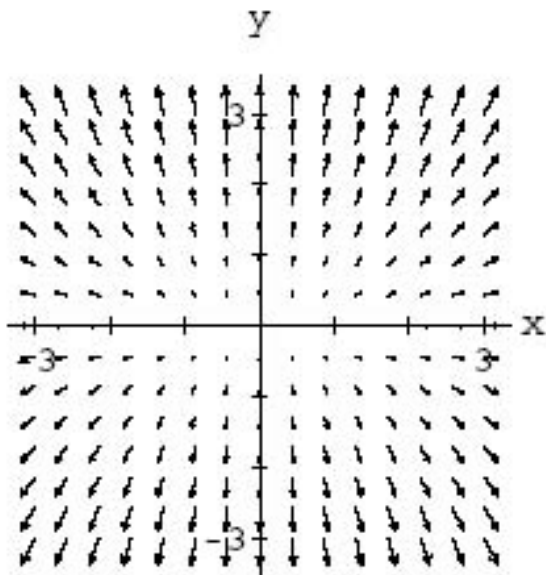
(a)



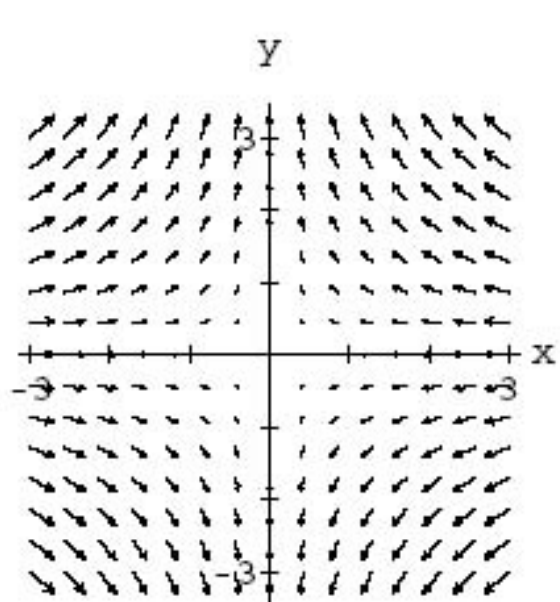
(b)



(c)



(d)



6) Given the force field F defined by $F(x, y, z) = (y - yz \sin x)i + (x + z \cos x)j + (y \cos x)k$

a) Show that F is a gradient field.

b) Find a potential function ϕ for F

c) Find the work done by F along the curve C traced by $r(t) = (2t)i + (1 + \cos t)^2 j + (4 \sin^3 t)k$ from $t = 0$ to $t = \pi/2$

7) Use Green's theorem to evaluate the line integral

$$\oint_C (x^4 - 2y^3)dx + (2x^3 - y^4)dy,$$

where C is the circle $x^2 + y^2 = 4$.

8) Use Green's theorem to evaluate the line integral

$$\oint_C xy dx + x^2 dy,$$

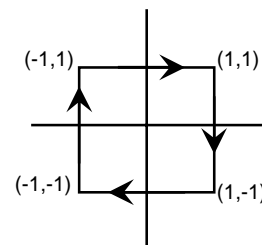
where C is the boundary of the region determined by the graph of $x = 0, x^2 + y^2 = 1, x \geq 0$.

[**Hint:** use polar coordinate to evaluate the double integral]

9) Evaluate

$$\oint_C x^2 y^3 dx - xy^2 dy,$$

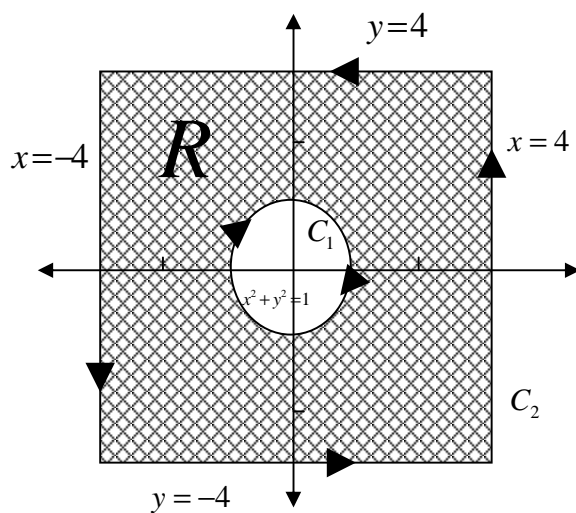
on the given curve C .



10) Evaluate

$$\oint_C \frac{x}{x^2 + y^2 - 4} dx + \frac{y}{x^2 + y^2 - 4} dy,$$

where $C = C_1 \cup C_2$ is the boundary of the shaded region R .



11) Read the statement and decide if it is (True) or (False) and circle your answer.

A	The graph on the curve traced by $r(t) = ti + 2tj + \cos tk$, $t \geq 0$ is a helix.	T	F
B	The curve C traced by $r(t) = (t^2 - 2t)i + (\frac{1}{3}t^3 - t)j$, $0 \leq t \leq 5$ is a <u>smooth</u> curve.	T	F
C	The length of the curve traced by $r(t) = (4t)i + 6j - (3t)k$, $0 \leq t \leq 1$ is equal 5 .	T	F
D	$\nabla F(-1,1,-1) = -i + j - k$ where $F(x, y, z) = xyz$.	T	F
E	The maximum value of the directional derivative is $\ \nabla F\ $ and it occurs when u has the same direction as ∇F .	T	F
F	$F(x, y, z) = xyz$. The minimum value of $D_u F(-1,1,-1)$ is $-\sqrt{3}$.	T	F
G	$F(x, y, z) = (2x)i + j + (3x)k$ is not a vector field.	T	F
H	The velocity vector field $F(x, y, z) = yi + xj + zk$ for a fluid is <u>irrotational</u> .	T	F
I	The velocity vector field $F(x, y, z) = yi + xj + zk$ for a fluid is <u>incompressible</u> .	T	F
J	The face field $F(x, y) = xi + yj$ is <u>conservative</u> .	T	F
K	The function $\phi(x, y) = x^2 - y$ is a <u>potential</u> function for $F(x, y) = (2x)i + j$.	T	F