

Hierarchy of (Elementary) Functions

1. POLYNOMIAL FUNCTION (OF DEGREE n):

$$p_n = a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x + a_0 \quad (a_n \neq 0);$$

2. RATIONAL FUNCTION: $Q(x) = \frac{p_n}{q_m} = \frac{a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x + a_0}{b_m x^m + b_{m-1} x^{m-1} + \dots + b_1 x + b_0}$;

3. EXPONENTIAL FUNCTION: $f(x) = a^x \quad (1 \neq a > 0)$;

4. (NATURAL) LOGARITHMIC FUNCTION: $f(x) = \ln x$;

5. TRIGONOMETRIC FUNCTIONS:

$$\sin x, \cos x, \tan x, \sec x, \csc x, \cot x;$$

6. HYPERBOLIC FUNCTIONS:

$$\sinh x, \cosh x, \tanh x, \operatorname{sech} x, \operatorname{cosech} x, \operatorname{coth} x;$$

7. INVERSE TRIGONOMETRIC FUNCTIONS;

8. INVERSE HYPERBOLIC FUNCTIONS.