

**KING FAHD UNIVERSITY OF PETROLEUM &  
MINERALS  
DEPARTMENT OF MATHEMATICAL SCIENCES  
DHAHRAN, SAUDI ARABIA**

**STAT 212: BUSINESS STATISTICS II**

Major Exam I  
Sunday March 18, 2007  
6:00 pm – 7:15 pm

Please **circle** your instructor's name:

Instructor's name

**Rahimov I.**

**Anabosi R.**

**Al Sawi E.**

Section number

1      5

2      3      4

6

Name: **SOLUTION KEY**

ID#:

Serial:

Question No	Full Points	Points Obtained
1	10	
2	10	
3	12	
4	8	
5	10	
6	10	
<b>Total</b>	<b>60</b>	

**Q1. (10 pts)** Answer the following questions by indicating it as **True** or **False**.

1. When the decision maker has control over the null and alternative hypotheses, the alternative hypotheses should be the “research” hypothesis. ( **T** )
2. A conclusion to “not reject” the null hypothesis is the same as the decision to “accept” the null hypothesis. ( **F** )
3. If all other factors are held constant, an increase in sample size will result in decreased chance of committing a Type I statistical error. ( **F** )
4. Of the two types of statistical errors, the one that decision makers have most control of is the Type I error. ( **T** )
5. If a hypothesis test leads to incorrectly rejecting the null hypothesis, a Type II statistical error has been made. ( **F** )

**Q2. (10 pts)** Answer the following questions by choosing the right answer.

1. Which of the following would be an appropriate null hypothesis?
  - a. The mean of a population is equal to 55.
  - b. The mean of a sample is equal to 55.
  - c. The mean of a population is greater than 55.
  - d. Only (a) and (c) are true.
  
2. If the  $p$  value is less than  $\alpha$  in a two-tailed test,
  - a. The null hypothesis should not be rejected.
  - b. The null hypothesis should be rejected.
  - c. A one-tailed test should be used.
  - d. More information is needed to reach a conclusion about the null hypothesis.
  
3. In a two-tailed hypothesis test for a population mean, an increase in the sample size will:
  - a. Have no affect on whether the null hypothesis is true or false.
  - b. Have no affect on the significance level for the test.
  - c. Result in a sampling distribution that has less variability.
  - d. All of the above are true.
  
4. The reason for using the t-distribution in a hypothesis test about the population mean is:
  - a. The population standard deviation is unknown and the sample size is fairly small.
  - b. It results in a lower probability of a Type I error occurring.
  - c. It provides a smaller critical value than the standard normal distribution for a given sample size.
  - d. None of the above would be a reason for using the t-distribution.
  
5. When testing a two-tailed hypothesis using a significance level of 0.05, a sample size equal to  $n = 16$ , and with the population standard deviation unknown, which of the following is true?
  - a. The null hypothesis can be rejected if the sample mean gets too large or too small compared with the hypothesized mean.
  - b. The alpha probability must be split in half and a rejection region must be formed on both sides of the sampling distribution.
  - c. The test statistic will be a t-value.
  - d. All of the above are true.

**Q3. (12 pts)** A company makes a device that can be fitted to automobile engines to improve the mileage. The company claims that if the device is installed, owners will observe a mean increase of more than 3.0 mpg. Assuming that the population standard deviation of increase is known to be 0.75 mpg, and a sample of size 64 cars is selected with an  $\bar{x} = 3.25$  mpg.

- Based on these data for which significance levels you would reject company's claim?
- Do you have strong evidence to reject the company's claim using a significance level of 0.07?

The hypotheses are:  $H_0: \mu \leq 3.0$

$H_A: \mu > 3.0$  claim

The test statistic:

$$Z_0 = \frac{\bar{x} - \mu}{\frac{\sigma}{\sqrt{n}}} = \frac{3.25 - 3.0}{\frac{0.75}{\sqrt{64}}} = 2.67$$

The p-value:

$$\begin{aligned} P(Z > Z_0) &= P(Z > 2.67) = 0.5 - P(0 < Z < 2.67) \\ &= 0.5 - 0.4962 = 0.0038 \end{aligned}$$

Answer:

a) **The company's claim would be rejected for any significance level  $< 0.0038$**

b) **No, because p-value =  $0.0038 < 0.07 = \alpha$ .**

**Q4. (8 pts)** The following table shows the number of traffic citations given for speeding by two officers, Officer 1 and Officer 2, of the Dammam-Jubail Highway Patrol for the last six months.

	Month					
	September	October	November	December	January	February
Officer 1	30	22	25	19	26	29
Officer 2	26	19	20	15	19	21

At the 2% significance level, is there a significant difference in the average number of citations given by the two officers?

The hypotheses are:  $H_0: p \leq 0.04$  claim

$H_A: p > 0.04$

Test Statistic:

$$\text{Test statistic} = Z_0 = \frac{p - p_0}{\sqrt{\frac{p_0(1-p_0)}{n}}} = \frac{0.06 - 0.04}{\sqrt{\frac{0.04(1-0.04)}{100}}} = 1.02$$

Critical value(s):  $\text{Critical value} = z_\alpha = z_{0.05} = 1.645$

The decision rule: **If  $Z_0$  (test statistic)  $> z_\alpha$  (critical value), reject  $H_0$ .**

The decision: **Since  $1.02 \not> 1.645$ , we do not reject  $H_0$ .**

The conclusion: **The proportion of defects in the shipment does NOT exceed 0.04.**

**Q5. (10 pts)** A department store study supplied the following data on customer ages from independent samples taken at two store locations.

	Inner-City Store	Suburban Store
Sample size	36	49
Sample mean	40	35
Sample standard deviation	9	10

If you allow 5% of type one error, do these data support the claim that the mean ages of the populations of customers at the two stores are different?

The hypotheses are:  $H_0: \mu_1 - \mu_2 = 0$   $H_A: \mu_1 - \mu_2 \neq 0$  claim

The test statistic:

$$Z_0 = \frac{\bar{X}_1 - \bar{X}_2 - 0}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}} = \frac{(40 - 35) - 0}{\sqrt{\frac{9^2}{36} + \frac{10^2}{49}}} = 2.41$$

Critical value(s):  $\pm z_{\frac{\alpha}{2}} = \pm z_{\frac{0.05}{2}} = \pm z_{0.025} = \pm 1.96$

Decision rule: **Reject  $H_0$  if  $Z_0 < -z_{\frac{\alpha}{2}}$  or if  $Z_0 > z_{\frac{\alpha}{2}}$ .**  
**Reject  $H_0$  if  $|Z_0| > z_{\frac{\alpha}{2}}$ .**

Decision: **Since  $2.41 > 1.96$ , Reject  $H_0$ .**

Conclusion: **Customers at the two stores are different in terms of mean ages.**

- Q6. (10 pts)** Company claims that its light bulbs are better than those of company B. A study showed that a sample of 20 bulbs from company A had mean lifetime of 647 hours with a standard deviation of 27 hours, while a sample of 20 bulbs from company B had mean lifetime of 638 hours with a standard deviation of 31 hours.
- Does this support the claim at the 0.05 level of significance?
  - What assumptions you need to answer this question?

The hypotheses are:  $H_0: \mu_A - \mu_B \leq 0$   $H_A: \mu_A - \mu_B > 0$  claim

The test statistic:

$$T_0 = \frac{\bar{X}_A - \bar{X}_B - 0}{s_p \sqrt{\frac{1}{n_A} + \frac{1}{n_B}}} = \frac{(647 - 638) - 0}{29.069 \sqrt{\frac{1}{20} + \frac{1}{20}}} = 0.979$$

$$s_p = \sqrt{\frac{(n_A - 1)s_A^2 + (n_B - 1)s_B^2}{n_A + n_B - 2}} = \sqrt{\frac{(20 - 1)27^2 + (20 - 1)31^2}{38}} = 29.069$$

Critical value(s):  $df = 38$ ,  $t_{0.05, 38} = 1.684$ ,

Decision rule : **Reject  $H_0$  if  $T_0 > t_{\alpha, df}$**

Decision and Conclusion: **Since  $T_0 = 0.979 < 1.684 = t_{0.05, 38}$ , Do NOT reject  $H_0$ .**

**That is, bulbs of company A are NOT better of those of company B**

Assumptions:

- Samples are INDEPENDENT.**
- Assume the two populations are NORMAL.**
- Population variances are EQUAL.**