KING FAHD UNIVERSITY OF PETROLEUM & MINERALS DEPARTMENT OF MATHEMATICS & STATISTICS DHAHRAN, SAUDI ARABIA

STAT 212: BUSINESS STATISTICS | |
Semester 063
Second Exam & SOLUTIONS &
Saturday Aug 8, 2007

Please **circle** your:

Instructor's name

& section number

Mohammad F. Saleh

Sec 1: (9:20 – 10:20)

7:00 - 8:30PM

Sec 2:(10:30-11:30)

Marwan M. Almomani

Sec 3: (10:30-11:30)

Name:

Student ID#:

Serial #:

Directions:

1) You must show all work to obtain full credit for questions on this exam.

2) DO NOT round your answers at each step. Round answers only if necessary at **your final** step to 4 decimal places.

Question No	Full Marks	Marks Obtained
<i>Q1</i>	14	
<i>Q2</i>	14	
<i>Q3</i>	14	
Q4	23	
Total	65	

<u>Question One (2+1+6+1+2+1+1 = 14 pts)</u>:

Last rating period, the percentages of the viewers watching several channels between 11:00 P.M. and 11:30 PM in a major TV market were as follows:

	WDUX	WWTY	WACO	WTJW	Other
	(News)	(News)	(Cheers Reruns)	(News)	other
Pi	= 8%	28%	20%	6%	38%

And in the current rating period, a survey of 2,000 viewers gives the following:

WDUX WWTY WACO WTJW Other (News) (News) (Cheers Reruns) (News) 182

Pi=nPi 182 536 354 151 777 2.5 pts
Do you think that the viewing shares in the current rating period differ from those in the last rating period at 0.10 level of significance?

a. The test hypotheses are:

Ho: The viewing Shares in the current period are the Some as those in the last rating period. H_A :

The viewing shares in the current period one differ from those in on is:

the last voting period (2) pts b. The assumption is:

c. The test statistic is:

$$\chi_{c}^{2} = \sum \frac{(0i - 9i)^{1}}{ei} = \frac{(182 - 160)^{1}}{160} + \frac{(536 - 560)^{1}}{560} + \frac{(354 - 400)^{2}}{400} + \frac{(151 - 120)^{1}}{120} + \frac{(777 - 760)^{2}}{760}$$

$$= 3.625 + 1.0286 + 5.29 + 8.0683 + 0.3803$$

d. The critical value is: x2, k-1 = x2, 10, 4 = 7. 7794 } Opt

e. The decision rule and the decision are:

f. Your conclusion is:

The victing shares in the Current ruting period differ from those in the last roting g. Based on your decision, what type of error you might have committed?

Question Two (2+7+1+2+1+1 = 14 pts):

Marketers know that tastes differ in various regions of the country. In the rental car business, an industry expert has given the opinion that there are strong regional preferences of size of car and quotes the following data in support of the view:

			Region	3/02.		
		Northeast	Southeast	Northwest	Southwest	Total
Preferred Car Type	Full – size	105 (100)	120	105 (100)	70 (100)	400
	Intermediate	120 (25)	100 (25)	130 (25)	150 (25)	500
	All other	25 25	30 (25)	15 25	30 25	100
	Total	250	250	250	250	1000

Do the data support the expert's opinion at the 0.05 significance level?

a. The test hypotheses are:

b. The test statistic is:

$$\chi_{c}^{2} = \sum_{i=1}^{r} \frac{C}{j^{2}} \frac{(0.5 - 6i)^{2}}{6ij}$$

$$= \frac{(105 - 100)^{2} + (120 - 100)^{2} + (105 - 100)^{2} + (70 - 100)^{3} + (100 - 125)^{2}}{100} + \frac{(130 - 125)^{2} + (130 - 125)^{3} + (150 - 125)^{3} + (150 - 125)^{3}}{125} + \frac{(25 - 15)^{3} + (30 - 25)^{2}}{125} + \frac{(30 - 25)^{2}}{125} + \frac{(30 - 25)^{2}}{125} + \frac{(30 - 25)^{2}}{125}$$

$$= 0.25 + 4 + 0.25 + 9 + 0.2 + 5 + 0.2 + 5 + 0.1 + 4 + 1 = 29.9 \text{ Opt}$$

c. The critical value is:

$$\chi_{\kappa, (r-1)(c-1)}^{1} = \chi_{.05, 6}^{2} = 12.5916$$
 }) pt

d. The decision rule and the decision are:

Reject the 18
$$\chi_c^2 > \chi_{\kappa, (r-1)(c-1)}^2$$

$$29.9 > 12.5916 \qquad Peject th$$

e. The conclusion is:

f. What are other assumptions required to perform the test?

<u>Question Three (3+3+8 = 14pts):</u>

The following table shows how many weeks a sample of 6 persons have worked at an automobile inspection station and the number of cars each one inspected between noon and 2 P.M. on a given day:

Number of cars inspected (y)	14	13	15	21	23	21
Number of weeks employed (x)	1	2	5	7	9	12

You have calculated some of the necessary summary information to carry out the analyses as follows:

$$\sum x = 36$$
, $\sum x^2 = 304$, $\sum y = 107$, $\sum y^2 = 2001$ and $\sum xy = 721$

a. Obtain the correlation coefficient

$$\Gamma = \frac{(6)(721) - (36)(107)}{\left[(6)(304) - (36)^{2} \right] \left[(6)(2001) - (107)^{2} \right]} = \frac{474}{\sqrt{(528)(557)}} = 0.8740$$

$$\text{Opt}$$

- b. Interpret the value of the linear correlation coefficient in terms of the linear relationship between the two variables. There is a positive strong linear relationship between number of Cors inspected (Y) and number of weeks employed (X)
- c. (2+2+1+2+1 = 8 pts) At 1% level of significance, do the data provide sufficient evidence to conclude that the number of weeks employed (x) and the number of cars inspected (y) are negatively linear correlated?
 - I. State the hypotheses: vs. H_A: ρ< ο } ② p^{Ls} H₀: P ≥o
 - II. The test statistic is:

$$t_{c} = \frac{r}{\sqrt{\frac{1-r^{2}}{n-1}}} = \frac{0.8740}{\sqrt{\frac{1-(.8746)^{2}}{6-2}}} = 3.5973$$

III. The critical value is:

IV. The decision rule and the decision are:

Reject Ho if
$$E_{c} < -E_{c}, n-2$$
3.5973 & -3.7469

The conclusion is:

$$\begin{array}{c}
0 & \text{Pts} \\
0 & \text{Pts}
\end{array}$$

The date do NOT provide asufficient evidence that the number of weeks employed (X) and number of care inspected (Y) are negatively linearly correlated.

Question Four (2+6+1+4+1+3+1+1+4 = 23 pts):

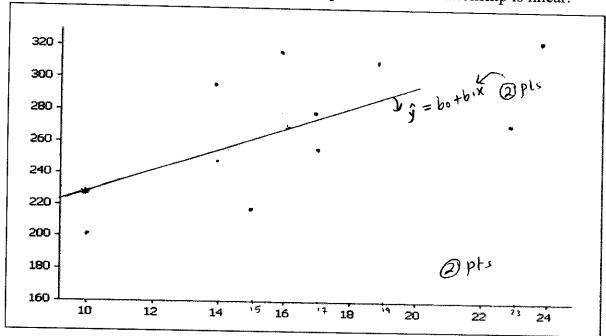
A manufacturing company is interested in predicting the cost of certain product. The manager believes that there is a relationship between the cost (in Dollars) of the product and the size (in millimeter) of the product. The manager believes that he can use production size to predict the cost of the product. The following data were collected randomly.

Cost (Dollars) (y)	245	312	279	308	201	219	270	324	300	255
Lot Size (x)	14	16	17	19	10	15	23	24	14	17

Also, the following summary statistics is obtained by the manager to predict the cost of the product using production size.

$$\sum x = 169$$
, $\sum x^2 = 3017$, $\sum y = 2713$, $\sum y^2 = 751337$, $\sum xy = 46833$, and $SSE = 9291$

a. Draw a scatter diagram to verify the assumption that the relationship is linear.



b. Fit a straight line to these data by the method of least squares, and draw its graph on the diagram obtained in part (a).

$$b_1 = \frac{46833 - \frac{(169)(2713)}{10}}{3017 - \frac{(169)^2}{10}} = \frac{983.3}{160.9} = 6.1112$$

 $b_0 = \bar{y} - b_1 \bar{x} = 271.3 - (6.1112)(16.9) = 168.0207 } \mathbb{O}P^{k}$

$$\hat{Y} = 168.0207 + 6.1112$$

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When X=10 , y = 229.1327

- c. Interpret the slope of the regression line.
- As the lot size (x) increases by 1 millimeter, the Cost (Y) increases 6446.11

d. What is the percentage of the variation of the cost that explained by the variation of the size?

$$R^{2} = \frac{55R}{55T}, \quad 5ST = \Sigma(y-\bar{y})^{2} = \Sigma y^{2} - (\Sigma y)^{2} = 751337 - (2713)^{2} = 15300 - 1$$

$$SSR = SST - SSE = 15300 - 1 - 9291 = 6009 - 1 \quad \text{Opt}$$

$$R^{2} = \frac{6009 - 1}{15300 - 1} = 0.3927 \text{ Opt}$$

e. The percentage = 39.27). Pt

$$5_{\xi} = \sqrt{\frac{55E}{n-7}} = \sqrt{\frac{9291}{8}} = 34.0790$$
 } (1) Pt

$$Sb_1 = \frac{S_{\xi}}{\sqrt{\sum_{x'} - (\sum_{x})^{5}}} = \frac{34.0796}{\sqrt{3017} - \frac{(164)^{5}}{10}} = \frac{34.0790}{\sqrt{160.9}} = 2.6866 \text{ } \text{Opt}$$

f. Construct a 95% confidence interval for the true regression slope and interpret this interval estimate.

1-x= 195 => x=105 : tw, n-2 = £1025, 8 = 2.3060 → OPt A 95% C.I. for B1 is: b1 + tokin-2. Sb1 => 6.1112 + (2.3060)(2.6866) Introprehabition: As the Size (X) increases by 1 millimeter 6.1112 ± 6.1953 [-0.0841, 12.3065] than the cost (Y) increases by on average between - 0841

and 12.3065 dollars (1) pt g. Based on the C.I that you obtained in part (f), do you think that there is a significant

relationship between the size and the cost of the product? Explain. Zero value belongs to the C.I., then the linear relationship

between the lot sizeward the cost (Y) is not significant at d=.05 (Ppt

h. Use the regression equation that you obtained in part (b) to predict the cost of a product if the size of the lot is 19 millimeter.

$$\hat{\mathcal{G}}^{(19)} = 168.0207 + 6.1112(19)$$

$$= 284.1335$$

i. Find the 95% confidence interval for the average of a lot of size of 19 millimeter.

A 95% C.1.
$$\frac{1}{4x}$$
 $\frac{E(Y|X_{P}=19)}{\hat{y}}$ is:
 $\hat{y} \pm t_{W_{P},N-2}$. $\frac{5}{5} \sqrt{\frac{1}{17} + \frac{(X_{P}-\bar{X})^{2}}{\Sigma(X-\bar{X})^{2}}}$
 $284.1335 \pm (2.3060)(34.0790\sqrt{\frac{1}{10} + \frac{(19-16.9)^{2}}{160.9}})$] Opt
 284.1335 ± 28.0508
[256.0827, 312.1843]] @pts