

**\*SOLUTIONS\***

King Fahd University of Petroleum & Minerals  
Department of Mathematical Science  
STAT-212-Term051-Quiz #6

Name:

ID:

Serial:

Question One (8-Points)

You are given the following MINITAB output for the estimated regression equation involving a dependent and two independent variables; Use this out put to answer the next questions:

Predictor	Coef.	SE Coef	T	P
Constant	-7.351	3.485	-2.11	0.061
X1	0.11273	0.02969	3.80	0.004
X2	0.34900	0.07131	4.89	0.001

S = 4.379      R-Sq = 94.8%      R-Sq(adj) = 93.8%

Analysis of Variance

Source	DF	SS	MS	F	P
Regression	2	3529.9	1765.0	92.03	0.000
Residual Error	10	191.8	19.2		
Total	12	3721.7			

a. The number of observations is:  $n-1=12 \Rightarrow n=13$  (1)

b. The regression equation is:

$$\hat{y} = -7.351 + 0.11273X_1 + 0.34900X_2$$
 (1)

c. Interpret the value of  $b_1$

Interpretation:

(1) AS  $X_1$  increases by one unit  $\rightarrow y$  increases by 0.11273 units holding  $x_2$  fixed.

d. Does the over all model significant? Why? Use  $\alpha = .05$

Answer (Yes/No):----- Yes (1)

Explanation:

$$p\text{-value} = 0.000 < \alpha \quad (\text{or } F_c = 92.03 \text{ large})$$
 (1)

e. Which, if any, of the independent variables is statistically significant? Use  $\alpha = .05$

All are significant, because for  $\beta_1 \rightarrow p\text{-value} = 0.004 < \alpha$

$\beta_2 \rightarrow p\text{-value} = 0.001 < \alpha$

(1)

So we reject  $H_0: \beta_1 = 0$  and  $H_0: \beta_2 = 0$

f. Find the values of SSR, and SSE

$$SSR = 3529.9$$

$$SSE = 191.8$$

(1)

(1)

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Question Two (6-Points)

Answer the following questions as true or false:

- a. If the R-square for a multiple regression model with two independent variables is .64, the correlation between the two independent variables will be .80. ---False
- b. A dummy variable is a dependent variable whose value is set at either zero or one. ---False
- c. If one independent variable affects the relationship between a second independent variable and the dependent variable, it is said that there is interaction between the two independent variables. -----True

Question Three (2+4 = 6-Points)

You are given the following MINITAB output of one dependent and three independent variables, the correlation matrix and two residual graphs.

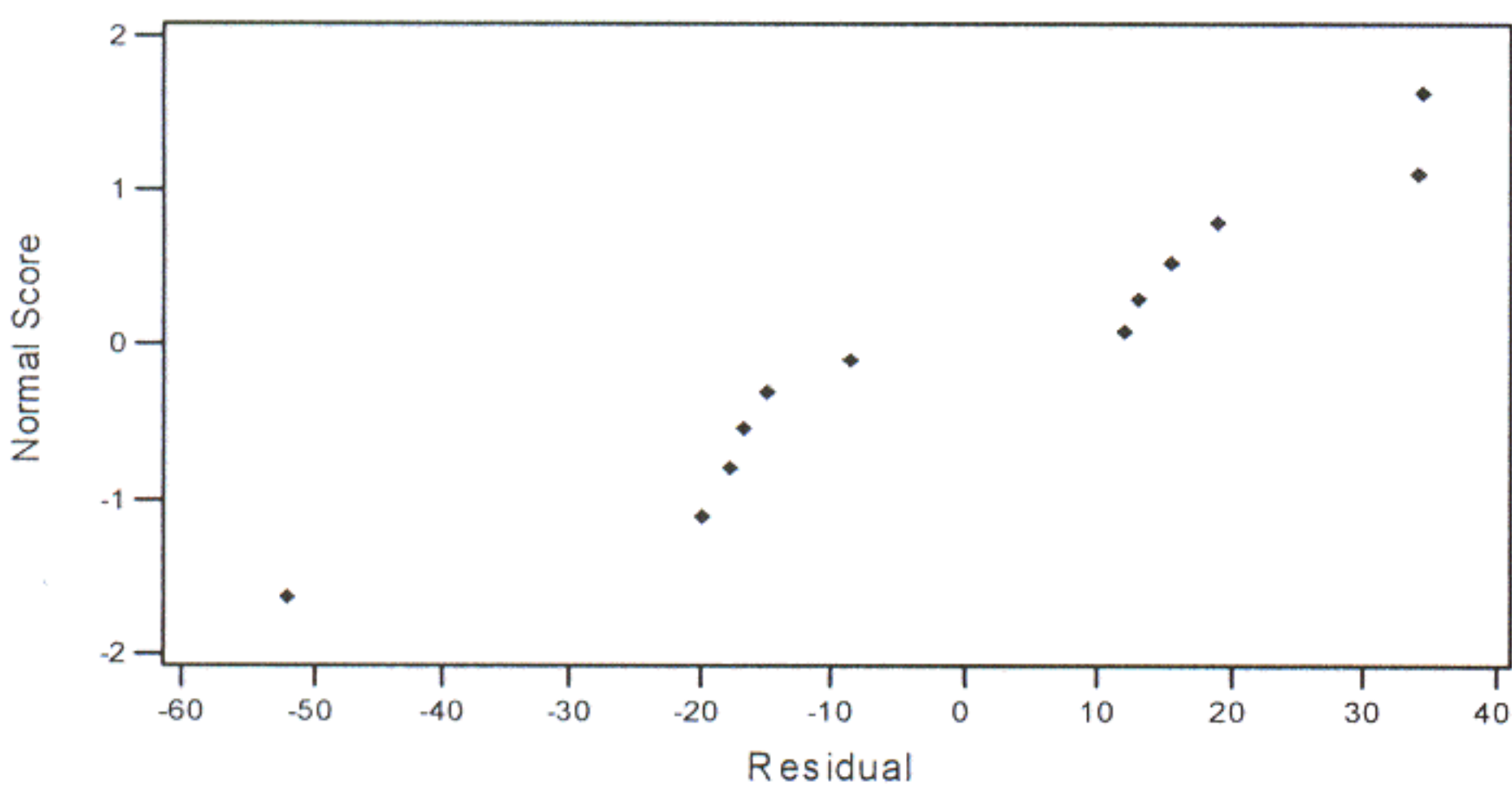
**Correlations: Y, X1, X2, X3**

	Y	X1	X2
X1	0.350 0.058		
X2	0.668 0.000	0.763 0.000	
X3	-0.179 0.345	-0.020 0.916	-0.125 0.512

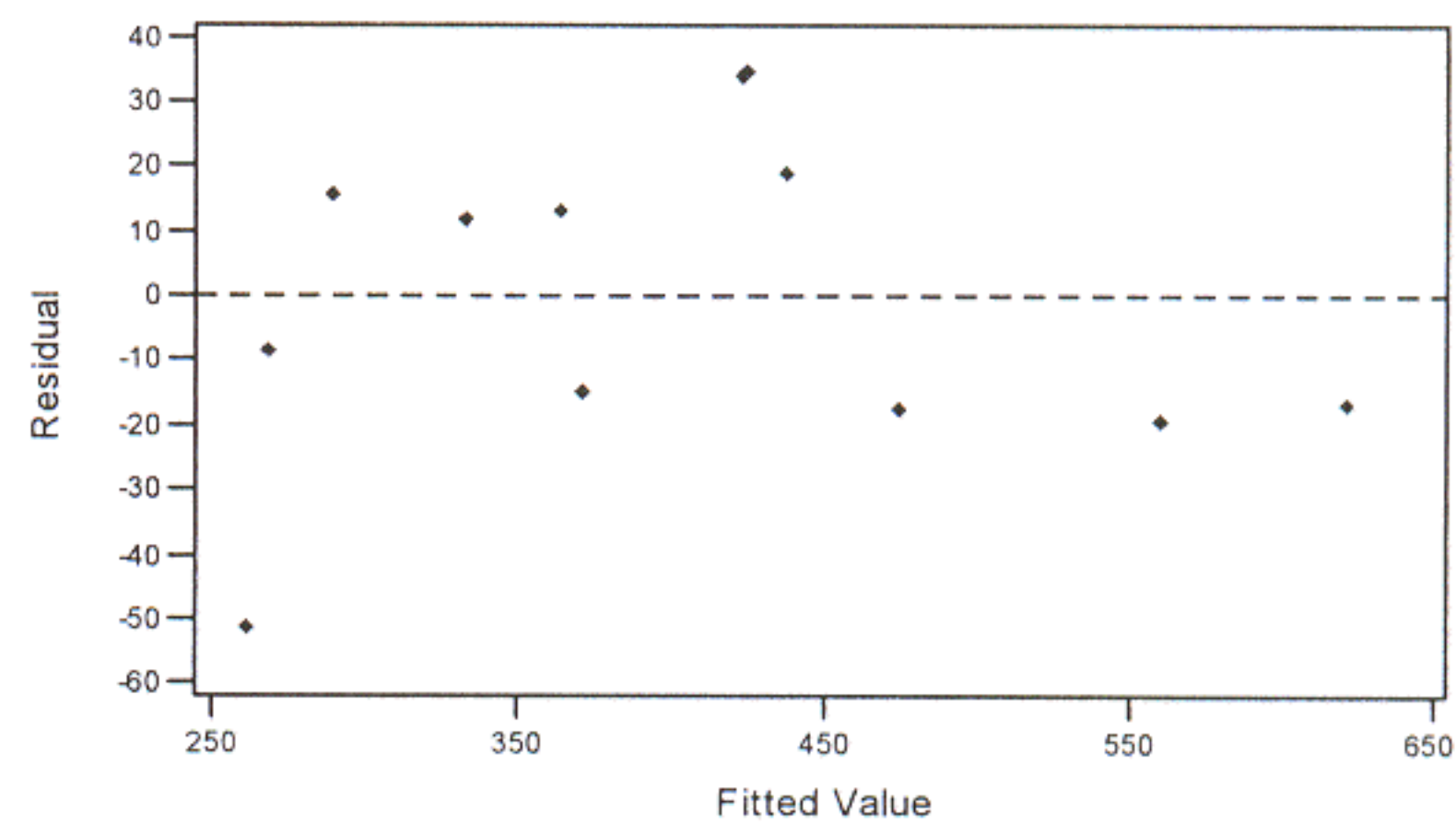
a. Which variable will enter the model-by forward selection method – and why?

*X<sub>2</sub> , because it has the highest value of correlation with Y  
r = .668 and it is significant. (2)*

Normal Probability Plot of the Residuals  
(response is Y)



Residuals Versus the Fitted Values  
(response is Y)



b. What can you conclude about the error assumptions ?

*None of the error assumptions is justified (4)*