

**King Fahd University of Petroleum and Minerals
College of Sciences, Prep-Year Math Program**

Code 001

Math 001, Exam I

(Term 012)

Sunday, March 17, 2002

6:00-7:50 p.m.

Code 001

Student's Name: _____

ID #: _____ Section #: _____

This exam consists of Three parts

Part I: True or False, write your answer in the assigned place on page 1.

Part II: Multiple Choice, write your answer in the assigned place on page 2.

Part III: Written Questions, you must show all necessary steps for full mark.

No Calculators, Pagers, or Mobiles are allowed during this exam.

| Question | Points | Student's Score |
|------------------|--------|-----------------|
| Part I: (a - g) | 14 | |
| Part II: (1 - 5) | 15 | |
| Part III: 1 | 5 | |
| 2 | 3 | |
| 3 | 4 | |
| 4 | 3 | |
| 5 (a), (b), (c) | 13 | |
| 6 | 5 | |
| 7 (a), (b) | 8 | |
| 8 | 5 | |
| 9 (a), (b) | 8 | |
| 10 | 5 | |
| 11 (a), (b) | 7 | |
| 12 | 5 | |

| | |
|--------------|------------|
| Total | |
| | 100 |

Math 001, Exam I, Term 012, Code 1

Part I: True or False Questions

(2 points each)

Write TRUE or FALSE for the following statement.

a. $5x + 5y = 5(x + y)$ because of **commutative** property -----b. The operation of **Division** by nonzero real numbers is **associative** -----c. Every **Natural** number is a **Rational** number -----d. The multiplicative inverse of $-4\frac{2}{5}$ is $\frac{5}{22}$ -----e. 23×10^{-3} is the scientific notation for the number 0.023 -----f. If R is a notation for the set of all real numbers, Q is a notation for the set of Rational numbers, and H is a notation for the set of Irrational numbers, the $Q \cap R = H$ -----g. $\pi = 3.14$ -----

Part II: Multiple Choice Questions

(3 points each)

1. If $(y^6 y^{3t})^{\frac{1}{3}} = y$ then t is equal to:

- a. -2
- b. 2
- c. 1
- d. -1

2. If $i = \sqrt{-1}$, then $(-i)^{47} + \sqrt{-9}\sqrt{-4}$ is equal to:

- a. $-6 + i$
- b. $-6 - i$
- c. $6 + i$
- d. $6 - i$

3. The set $\{0.34128\dots, 2, 0.\overline{35}, \sqrt{5}, -3, -\frac{1}{2}\}$ contains:

- a. Three natural numbers
- b. Four integers
- c. Two irrational numbers
- d. Five rational numbers

4. Determine which of the following equations is an **Identity**

- a. $2y + 7 = 3(y - 1)$
- b. $-3(x - 5) = -3x + 15$
- c. $(x + 3)^2 = x^2 + 9$
- d. $\frac{x}{x} = 1$ for any real number x

5. The **sum** of the solutions for the quadratic equation $\sqrt{3}x^2 + 3x + \sqrt{2} = 0$ is:

- a. $\frac{\sqrt{2}}{3}$
- b. $\frac{\sqrt{6}}{3}$
- c. -1
- d. $-\sqrt{3}$

Part III: Written (Solve the following Questions, show all necessary steps for full credit)

1. Find the value of $\frac{-3^2 + 6 + \sqrt{(-3)^2} - |-3|}{2 - \sqrt[3]{(-3)^3}}$ (5 pts)

2. Write without absolute value notation $\|x - 4| - |2x - 3|\|$ if $-3 < x < -2$ (3 pts)

3. Find the coefficient of a^2b in the expression $(a - 2b)^2(3a - b)$ (4 pts)

4. Rationalize the denominator of $\frac{\sqrt{3} + \sqrt{2}}{2\sqrt{3} - 3\sqrt{2}}$ (3 pts)

5. Simplify the following expressions:

(a) $\left(\frac{(ab)^{-1}c^2}{(ac^{-2})^{-1}b^2} \right)^{-2}$ (4 pts)

(b) $\frac{y^2+6y+9}{y^3+27} + \frac{y+3}{y^3-3y^2+9y}$ (5 pts)

(c) $\frac{1-(1-x)^{-1}}{x^{-1}+(1-x)^{-1}}$ (4 pts)

6. Find the Least Common Denominator (LCD) of the following expression (**Do not simplify**)

$$\frac{x+y}{x^2+2xy-3y^2} - \frac{2y}{x^2+xy-6y^2} + \frac{5}{3(x-y)} \quad (5 \text{ pts})$$

7. Factorize the following as completely as possible:

(a) $x^{4n} - 1$ (4 pts)

(b) $5xy + 20y - 15x - 60$ (4 pts)

8. Write the complex number $\frac{4+i}{3+i} - \frac{1}{3-i}$ in the standard form. (5 pts)

9. (a) Solve for x in the equation $z = y(1 + \frac{m}{x})$. (4 pts)

(b) Solve the quadratic equation $9x^2 - 12x - 1 = 0$ by completing the square method. (4 pts)

10. Find a positive real number that is 5 larger than its **reciprocal**.

(5 pts)

11. If -4 is a solution for the equation $kx^2 + 10x - 8 = 0$.

(a) Find k

(4 pts)

$$1 - \frac{20}{1 - 1} = \frac{1}{1} (x - 1)$$

(b) Using the value of k in (a), find the other solution of the equation.

(3 pts)

$$\frac{1}{2} \frac{1}{2} x = \frac{1}{2} (1 + x)$$

12. Find the solution set of $\frac{8}{2m+1} - \frac{1}{m-2} = \frac{5}{2m+1}$

(5 pts)