

Name: \_\_\_\_\_

Key

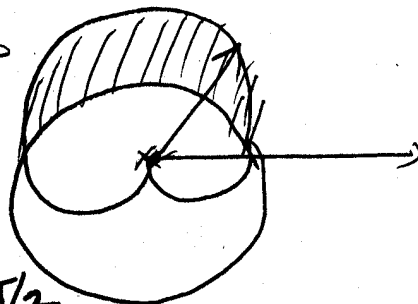
I.D.# \_\_\_\_\_

Serial # \_\_\_\_\_

Q1: Find the area inside the polar curve  $r = 1 + \sin \theta$  and outside the curve  $r = 1$ .

$$1 + \sin \theta = 1 \Rightarrow \sin \theta = 0$$

$$\sin \theta = 0, \pi$$



$$A = \frac{1}{2} \int_{\pi/2}^{\pi} [(1 + \sin \theta)^2 - 1^2] d\theta$$

$$= \frac{1}{2} \int_{\pi/2}^{\pi} [1 + 2\sin \theta + \sin^2 \theta - 1] d\theta = \int_{\pi/2}^{\pi} \left( 2\sin \theta + \frac{1}{2} - \frac{1}{2} \cos 2\theta \right) d\theta$$

$$= \left[ -2\cos \theta + \frac{\theta}{2} - \frac{1}{4} \sin 2\theta \right]_{\pi/2}^{\pi} = 0 + 2 + \frac{\pi}{4} = 2 + \frac{\pi}{4}$$

Q2: Find equation of the sphere that is centered at  $(2, 1, 0)$ , and tangent to the  $xz$ -plane.

$$r = |1| = 1$$

$$\text{The eq. is } (x-2)^2 + (y-1)^2 + z^2 = 1$$

Q3: Find the magnitude of  $\mathbf{u} + \mathbf{v}$  and  $\mathbf{u} - \mathbf{v}$ , where  $\mathbf{u} = \langle 1, 2, -1 \rangle$  and  $\mathbf{v} = \langle -2, 1, 0 \rangle$ .

$$\vec{u} + \vec{v} = \langle -1, 3, -1 \rangle,$$

$$\vec{u} - \vec{v} = \langle 3, 1, -1 \rangle$$

$$\|\vec{u} + \vec{v}\| = \sqrt{1+9+1} = \sqrt{11}$$

$$\|\vec{u} - \vec{v}\| = \sqrt{9+1+1} = \sqrt{11}$$