



# IQ Space Frequency Time Codes for MIMO-OFDM Systems

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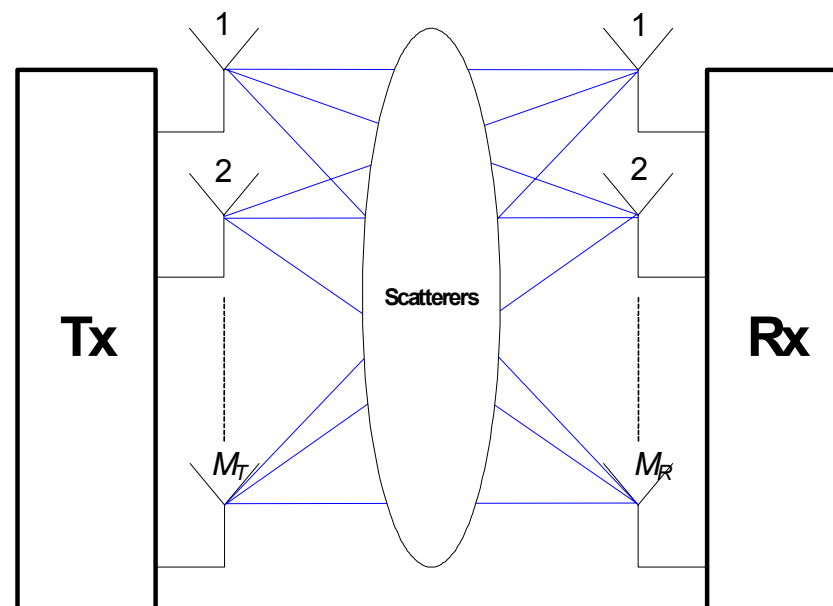


# Outline

- Background and motivation
- IQ-SFT code description and performance
- Effect of interleaving

# Introduction: Multiple Input Multiple Output (MIMO) Channels

- A MIMO channel is a wireless link between  $M_T$  transmit and  $M_R$  receive antennas.
- MIMO channels boost the information capacity of wireless systems by order of magnitude [Telatar95][Foschini98].



$$\mathbf{H}(t) = \begin{pmatrix} h_{11}(t) & \dots & h_{1M_T}(t) \\ \vdots & \ddots & \vdots \\ h_{M_R 1}(t) & \dots & h_{M_R M_T}(t) \end{pmatrix}$$

# OFDM

- Wide bandwidth and high data rates result in frequency selective channels (FSC) which cause ISI.
- OFDM is robust against FSC. It transforms FSC to parallel flat fading channels.
- WLANs such as IEEE 802.11a and Hyperlan2 are based on OFDM

# OFDM Channel Model in the Frequency Domain

$N_c$  subcarriers

$L$  taps (FSC length)

Let  $\mathbf{h}_{mn} = [h_0 \quad h_1 \quad \cdots \quad h_{L-1}]^T$

The OFDM channel in the frequency domain is  $\mathbf{h}_{mn}^f = \mathbf{F}\mathbf{h}_{mn}$

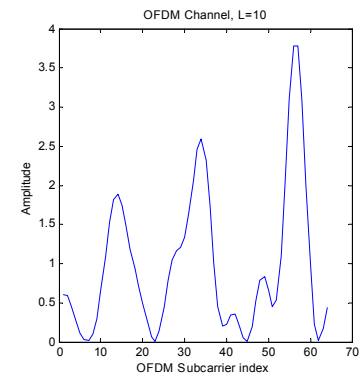
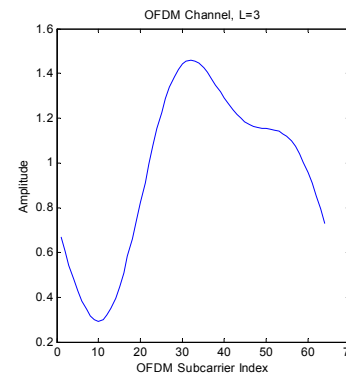
$$\mathbf{F}_{k,l} = \frac{1}{\sqrt{N_c}} \exp \left[ -i \frac{2\pi}{N_c} (k-1)(l-1) \right];$$

$$k = 0, 1, \dots, N_c - 1$$

$$l = 0, 1, \dots, L - 1$$

Let  $\mathbf{h} \sim N_c(\mathbf{0}, \mathbf{C}_h)$

The covariance matrix in the frequency domain is  $\mathbf{C}_{h^f} = \mathbf{F}\mathbf{C}_h\mathbf{F}^H$



# Background on Space Frequency Time (SFT) Codes

- SFT codes apply spatial coding across multiple antennas, frequency coding across OFDM subcarriers, and temporal coding across successive OFDM symbols.
- [Agrawal98]: STTC-OFDM, not optimized for OFDM channels, designed for quasi-static channels.

# Design criteria of SFT codes

- The maximum diversity available in MIMO-OFDM systems is  $M_T M_R$  [Ben Lu 2000].
- The design criterion is to maximize the minimum effective length and break up channel correlation in frequency domain by interleaving.
- To achieve this diversity, the minimum effective length of the SFT code should be equal to at least  $M_T L$ , which needs large number of states for practical values.

# Design criteria of SFT codes

- Our goal in this work is to simplify the design and reduce the number of states required to achieve the full spatial and frequency diversity.
- Our approach is to concatenate trellis coded modulation (TCM) and STBC.
- Spatial diversity is guaranteed by STBC and frequency diversity is provided by TCM.
- We further reduce the number of states of TCM by using IQ-TCM [AlSemari 97].

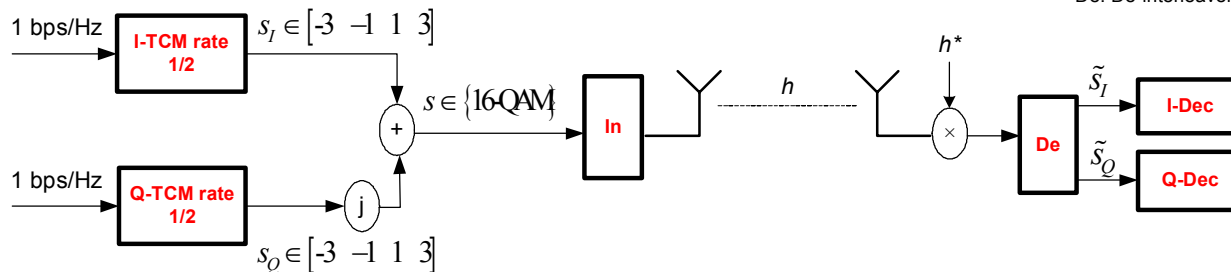


# IQ-TCM [AISemari97]

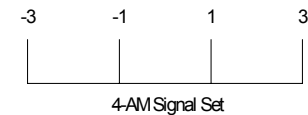
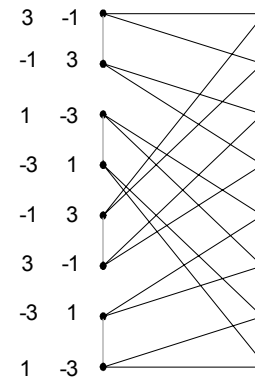
- The minimum effective length of TCM is upper bounded by:

$$l_{\min} \leq \lfloor v / k \rfloor + 1$$

## 2 bps/Hz IQ-16QAM-TCM



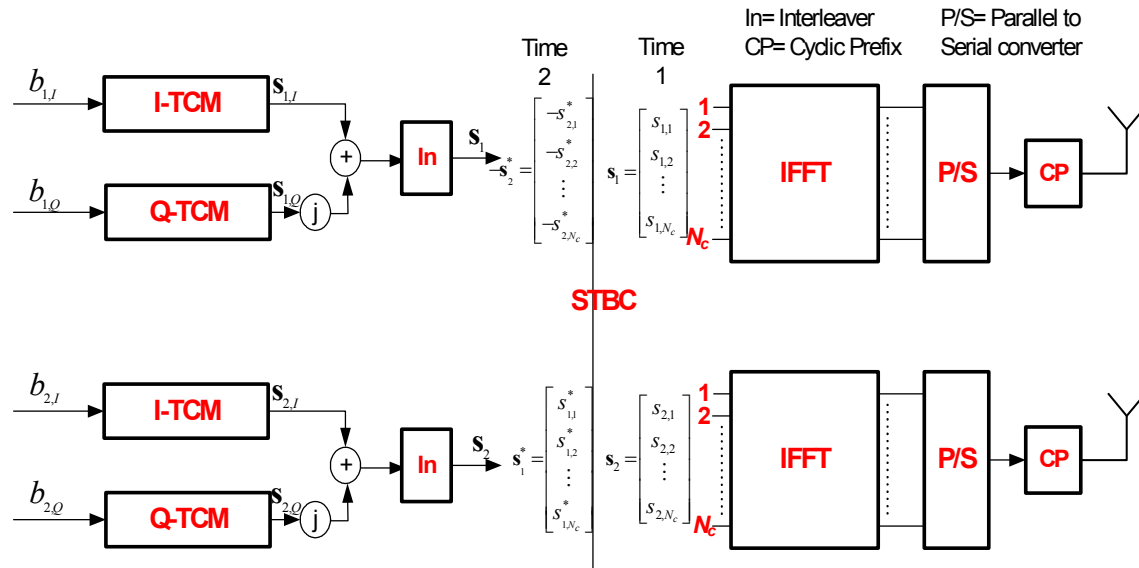
## 8-states 4AM-TCM



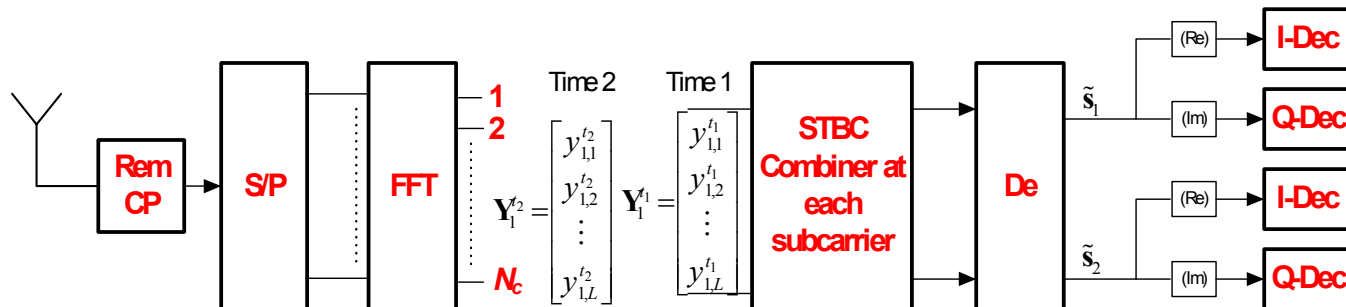
In: Interleaver  
De: De-interleaver

# IQ-SFT

## Encoder



## Decoder



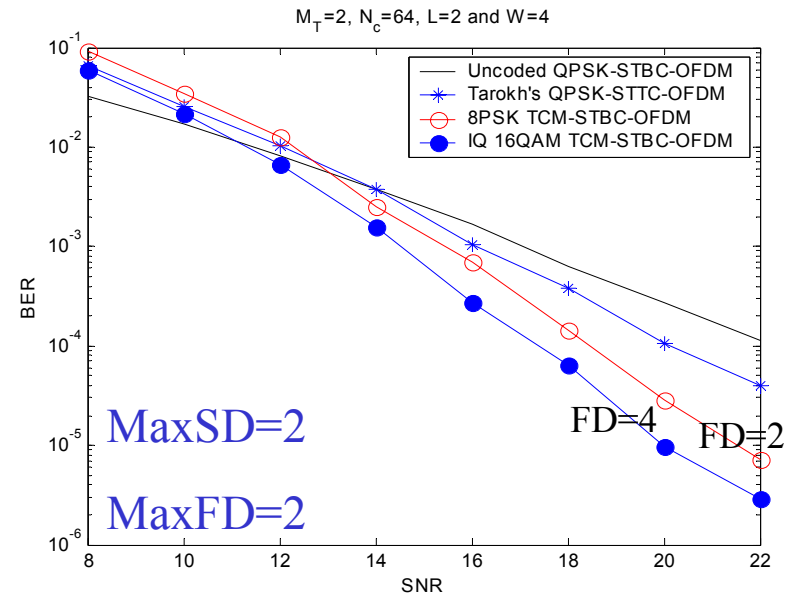
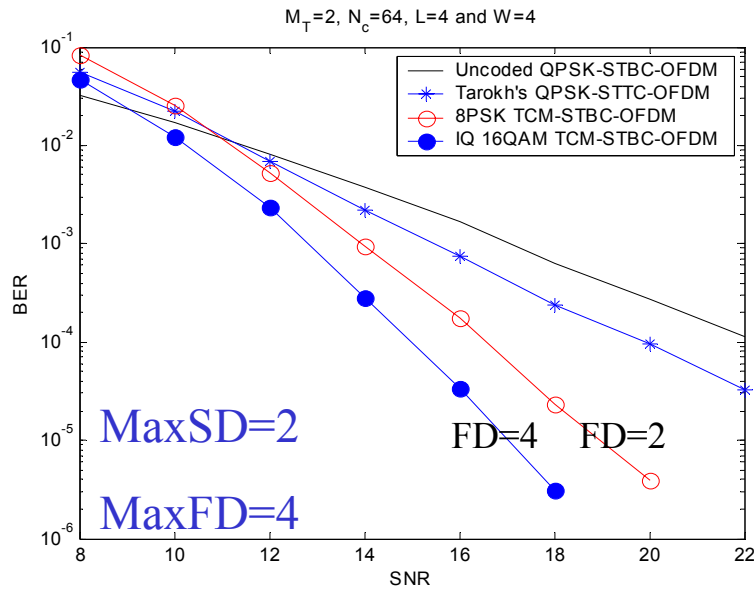
# Advantages of concatenated IQ-TCM-STBC at 2bps/Hz

FCS Length	Minimum number of states to achieve full diversity ( $M_T L M_R$ )		
$L$	Tarokh STTC QPSK	8PSK-STBC	<b>IQ-16QAM-STBC</b>
2	64	4	2
3	1024	16	4
4	16384	64	8
5	262144	256	16
6	4194304	1024	32
7	67108864	4096	64

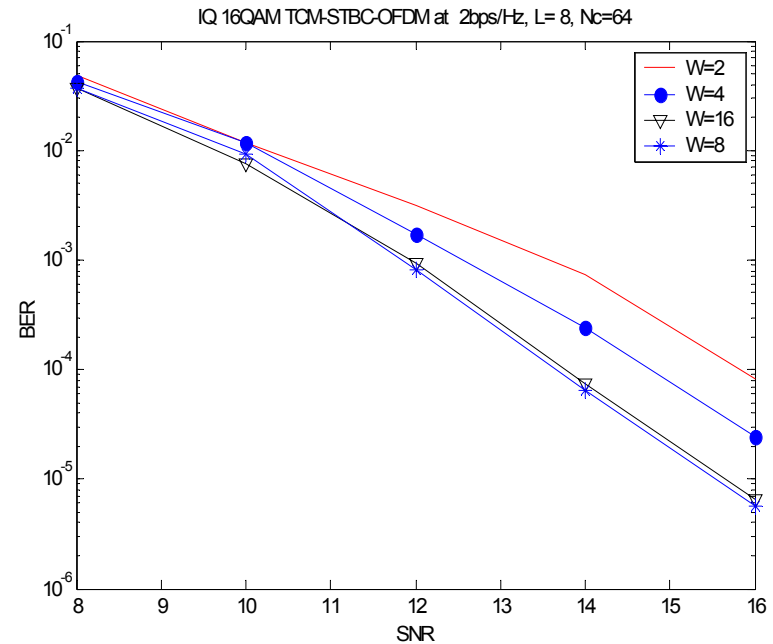
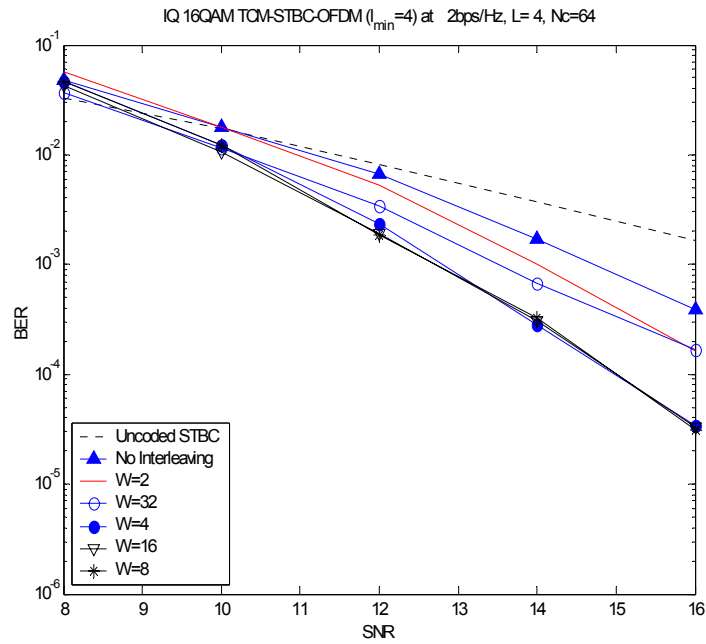
# Channel Model

- The channel is a MIMO-FSC of length  $L$  with equal power paths and each path experience an independent Rayleigh fading.
- We assume that the channel is constant over two OFDM symbols.

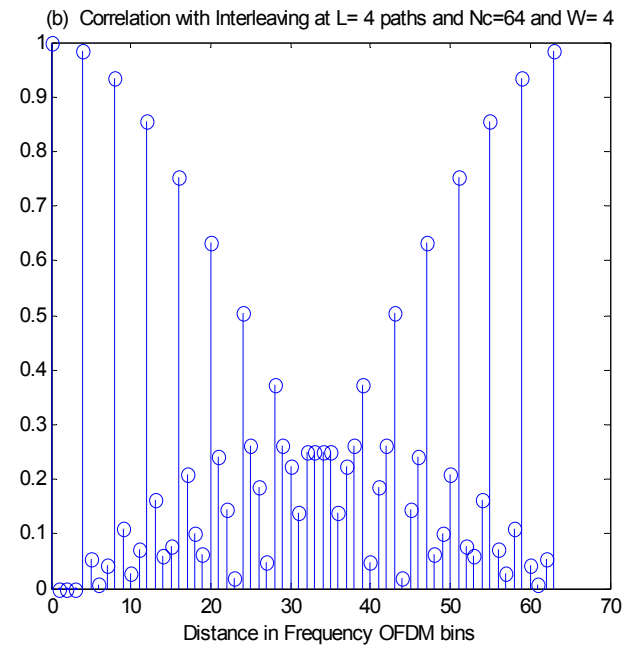
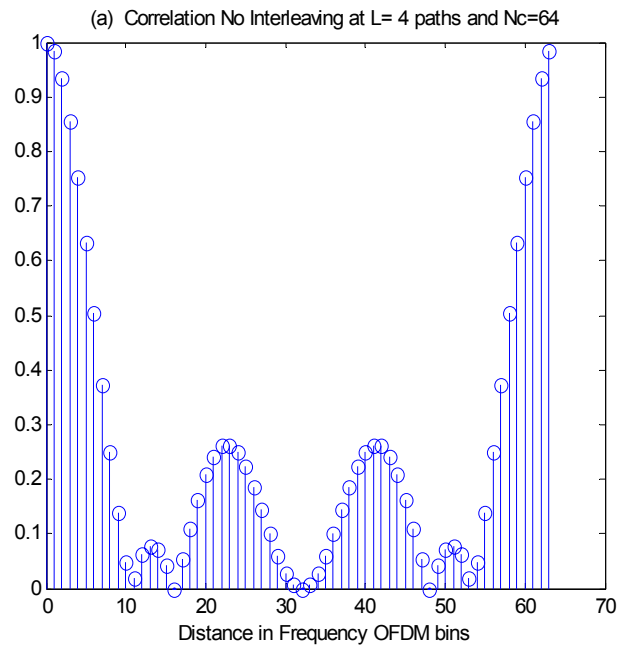
# Performance results over 2x1 MIMO-OFDM channels at 2 bps/Hz 8-state TCM, $N_c=64$ , $W=4$



# Interleaving effect over 2x1 MIMO-OFDM channels at 2bps/Hz 8-state TCM



# Effect of interleaving on subcarrier correlation



# SFT coding conclusions

- Concatenated IQ-TCM-STBC-OFDM achieves full spatial and frequency diversity at much lower complexity than other codes.
- Appropriate block interleaver design is essential to maintain the performance and diversity of the code. Best performance is at  $W=L$  and  $W=2L$ .





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