

Name: Key

ID #

Problem #1 (7.5points)

Consider the amplifier circuit shown below, $R_{sig}=500\Omega$, $R_L=475\Omega$, and $\beta=100$ (ignore r_o).

i. Find expressions for R_{in} , R_{out} , voltage gain $A_v = v_o/v_{sig}$. **4 points**

ii. Design R_B and I to have $R_{in}=25K\Omega$ and $R_{out}=30\Omega$ then, **2 points**

a. Find the voltage gain v_o/v_{sig} . **0.75points**

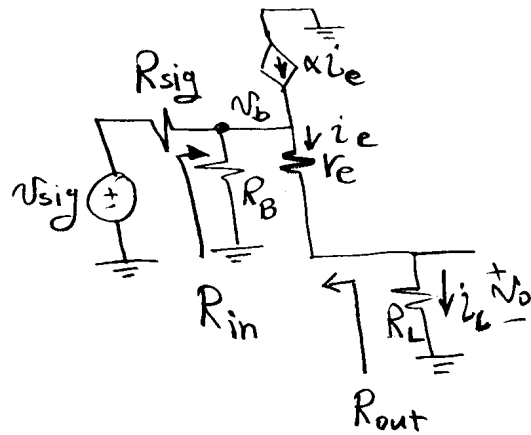
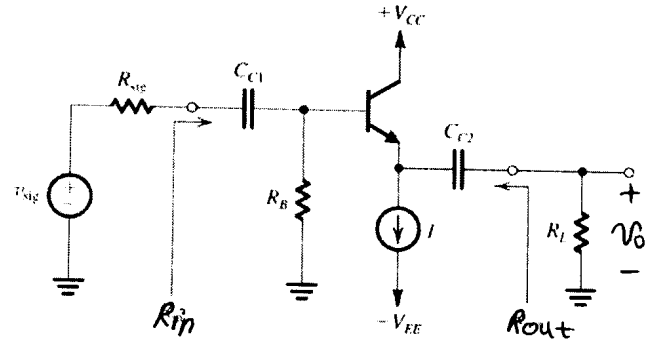
b. Find the maximum swing of $v_o(t)$ without distortion (Hint: based on the most negative current allowed on R_L). **0.75points**

i. **Small signal Analysis**

T-model

$$\frac{v_o}{v_{sig}} = \frac{v_b}{v_{sig}} \cdot \frac{v_o}{v_b}$$

$$A_v = \frac{v_o}{v_{sig}} = \frac{R_{in}}{R_{in} + R_{sig}} \cdot \frac{R_L}{R_L + r_e} \quad (*)$$



$$R_{in} = R_B \parallel [(\beta+1)(r_e + R_L)] \quad (**)$$

$$R_{out} = r_e + \frac{R_B \parallel R_{sig}}{(\beta+1)}$$

ii. $R_{out} = 30\Omega = r_e + \frac{R_B \parallel 500}{101}$ — very small $\leq 5\Omega$

$$\Rightarrow r_e = 25 = \frac{V_T}{I_E} = \frac{25m}{I} \Rightarrow \underline{I = 1mA} \quad (**)$$

$$R_{in} = R_B \parallel [101(25 + 475)] = R_B \parallel 50.5K$$

$$R_{in} = 25K\Omega \Rightarrow \underline{R_B = 50K\Omega} \quad (**)$$

a) $A_v = \frac{25K}{25K + 500} \cdot \frac{475}{500} = 0.93 \text{ V/V}$

b) i_c is limited by I in the negative cycle \Rightarrow
 maximum swing = $\pm I \times R_L = \pm 0.475 \text{ V}$

Consider the amplifier circuit shown below, (ignore r_o)

- i. Find expressions for R_{in} , R_{out} , voltage gain $A_v = v_o/v_{sig}$. 3.5 points
- ii. Given that $V_{DD}=10V$, $R_{sig}=500\Omega$, $R_L=10K\Omega$, $V_t=1V$, $k'_n(W/L)=1mA/V^2$
 - a. Design resistors R_D and I to have $g_m=1mA$ and $V_D=6V$. 2.5 points
 - b. Calculate voltage gain v_o/v_{sig} . 0.5 points
 - c. Find $v_o(t)$ and $v_D(t)$ for $v_{sig}(t)=0.2\sin 100t$. 1 point

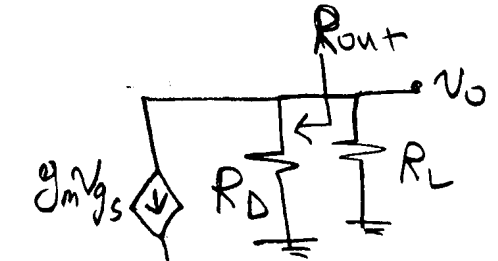
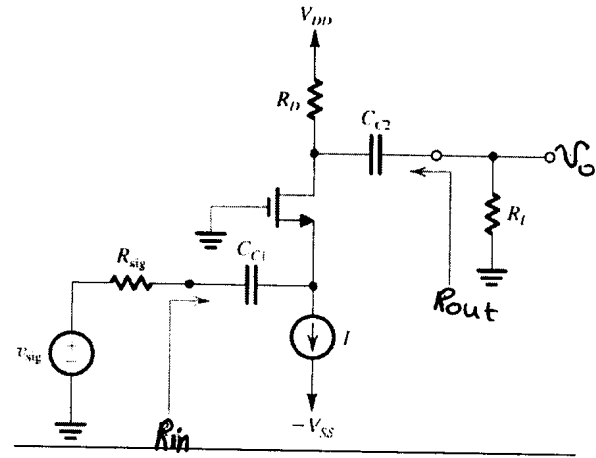
i. small signal Analysis

$$R_{in} = \frac{1}{g_m} \quad (*)$$

$$R_{out} = R_D \quad (**)$$

$$A_v = \frac{V_o}{V_{sig}} = \frac{-g_m V_{gs} (R_D || R_L)}{-g_m V_{gs} (\frac{1}{g_m} + R_{sig})}$$

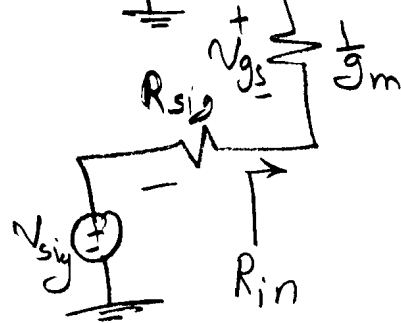
$$= \frac{R_D || R_L}{\frac{1}{g_m} + R_{sig}} \quad (***)$$



$$a) g_m = k'_n \frac{W}{L} (V_{GS} - V_t) = 1mA$$

$$\Rightarrow V_{GS} = 2V$$

$$I = I_D = \frac{1}{2} k'_n \frac{W}{L} (V_{GS} - V_t)^2 = 0.5mA \quad *$$



$$R_D = \frac{V_{DD} - V_D}{I_D} = \frac{10 - 6}{0.5m} = 8K\Omega$$

$$b) \frac{V_o}{V_{sig}} = \frac{8K || 10K}{\frac{1}{1m} + 500} = 2.96 \text{ V/V}$$

$$c) v_o(t) = 2.96 \times 0.2 \sin 100t = 0.59 \sin 100t \text{ V}$$

$$v_D(t) = V_D + v_d(t) = V_D + v_o(t) = 6 + 0.59 \sin 100t \text{ V}$$