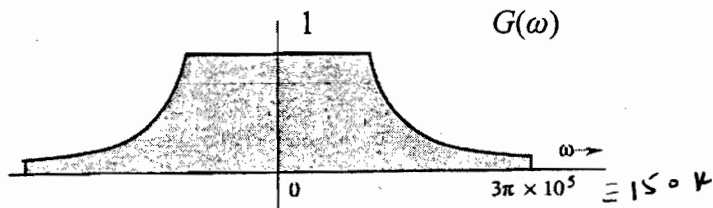


Name: KEY

The figure below shows the spectrum of a signal  $g(t)$



1. Determine the Nyquist interval and the sampling rate for  $g(t)$  (2 points)

$$\text{Max Freq} = \frac{3\pi \times 10^5}{2\pi} = 1.5 \times 10^5 \text{ Hz}$$

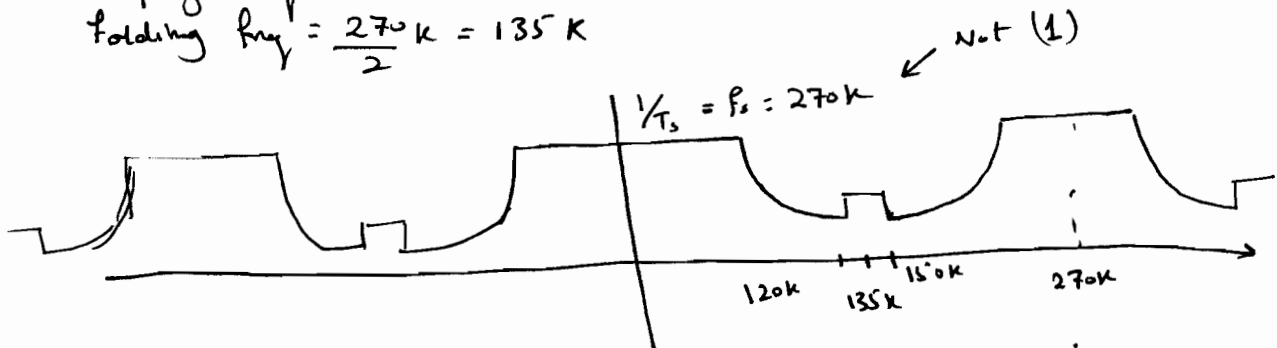
$$\Rightarrow \text{Nyquist Rate} = 2(\text{Max Freq}) = 3 \times 10^5 \text{ Hz (Samples/sec)}$$

$$\text{Nyquist Interval} = \frac{1}{\text{Nyquist Rate}} = \frac{1}{3 \times 10^5} = 3.33 \times 10^{-6} = 3.33 \mu\text{sec.}$$

2. Sketch the spectrum of the sampled signal, if  $g(t)$  is sampled (using uniformly spaced impulses) at  $0.9 \times$  Nyquist rate (4 points)

$$\text{Sampling Freq} = 0.9 * 3 \times 10^5 = 2.7 \times 10^5 \approx 270 \text{ K}$$

$$\text{Folding Freq} = \frac{270 \text{ K}}{2} = 135 \text{ K}$$



3. Explain whether you can recover the signal  $g(t)$  from the previous sampled signal. (2 points)

We cannot recover the signal  
 it is sampled at less than Nyquist rate  
 see the figure above.

4. Determine the Nyquist sampling rate for  $g^3(t)$ . (2 points)

multiplication in time  $\Rightarrow$  convolution in frequency

$$f_{s, \text{new}} = 3 * (300 \text{ kHz}) = 900 \text{ kHz}$$

because the [Bandwidth of  $g^3(t)$ ] =  $3 * \text{Bandwidth of } g(t)$