

King Fahd University of Petroleum & Minerals
 Electrical Engineering Department
 EE418: Satellite Communications (101)
Quiz 2: Orbital Mechanics (Doppler Effects)

Serial #

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- 1 points for not writing your serial number

Name: KEY

A satellite, in a 500 km high circular orbit, carries a 3 GHz transmitter. Determine: $v = \sqrt{\frac{\mu}{r}}$

- The orbital velocity.
- The orbital period.
- The orbital angular velocity in radians per second;
- If an earth station on the surface of the earth at mean sea level, 6,370 km from the center of the earth, can receive the transmissions down to an elevation angle of 0° , calculate the maximum Doppler shift that this station will observe. Note: include the earth's rotation and be sure you consider the *maximum possible* Doppler shift (i.e. $2\Delta f$).

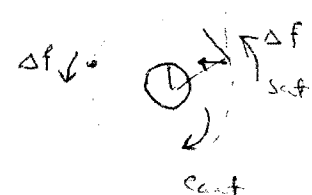
Note: assume the average radius of the earth is 6,370 km and Kepler's constant has the value $3.986004418 \times 10^5 \text{ km}^3/\text{s}^2$.

a) $v = \sqrt{\frac{\mu}{r}} = 7.6171 \text{ km/sec}$ (1)

b) $T = \frac{2\pi r}{v} = 5.687 \times 10^3 \text{ sec}$ (2)

c) $v_{\text{angular}} = \frac{2\pi}{T} = 0.0011 \text{ rad/sec}$ (2)

d) $v_{\text{in direction}} = v * \frac{r_e}{r_{\text{earth}}} = 7.0626 \text{ km/sec}$ (2)



Max when earth rotate in the opposite direction

Earth rotation (angular) = $\frac{2\pi}{\text{sidereal day}} = \frac{2\pi}{24 * 60 * 60}$ (1)

speed on Earth surface = $\frac{2\pi}{24 * 60 * 60} * r_e$

Total speed = $7062.6 + 463.23 = 7526 \text{ km/sec}$

$\Delta f = \frac{v_T}{\lambda}$ (1)

$2\Delta f = 150.5196 \text{ kHz}$

Because max increase is Δf
 & max decrease is Δf

without Earth Station
 $2\Delta f = 141.25 \text{ kHz}$

Good Luck, Dr. Ali Muqaibel