

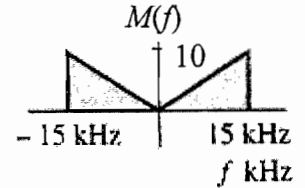
Serial #
 ○
 -2 points for not writing your serial #

Quiz 5

Name: KEY

Sec. 4

1. Given two signals $m(t)$ with the spectrum shown in the figure and $g(t)$ which is band limited to 10 kHz. Determine the minimum sampling (Nyquist) rate for the following signals.



$g(t)m(t)$, $5(g(t)+m(t))$, $dm(t)/dt$. Justify your answer

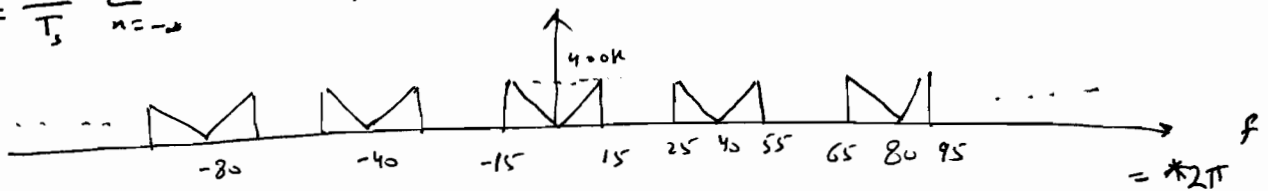
* Band width of $g(t)m(t)$ = $10K + 15K = 25K$ Hz
 because multiplication in time domain is equivalent to convolution in the frequency domain.
 Sampling rate = $2 * 25K = \underline{50KHz}$

* $5(g(t)+m(t))$
 Scaling by constant does not change the width of the spectrum.
 BW of $g(t)+m(t) = \max(BW(g(t)), BW(m(t)))$
 $= 15KHz \Rightarrow$ Sampling = $30KHz$

* $\frac{dm(t)}{dt}$: derivative does not change the BW of the signal (* jw). $BW = 15KHz$
 Sampling = $30KHz$

2. If the previous signal $m(t)$ is sampled at a rate of 40 kHz. Sketch the spectrum of the sampled signal. Show all details and show the final results. Can the signal be reconstructed?

$$\bar{G}(w) = \frac{1}{T_s} \sum_{n=-\infty}^{\infty} G(w - n\omega_s)$$



amplitude scaled by T_s

Yes, the signal can be reconstructed using a low pass filter
 "It is sampled above Nyquist rate"
 Please, see the quiz for the other section.