

Solution, HW #12

(7.3-1, 7.3-2, 7.3-4, 7.3-5)

7

7.3-1 A rate 6 kbps requires a bandwidth of at least 3 kHz for transmission using Nyquist Criterion Pulses. Since 4 kHz BW is available, we have an excess bandwidth of 1 kHz.

$$\therefore r = 1/3.$$

7.3-2 (a) Quantization error = $\frac{\Delta V}{2} = \frac{1}{2} \frac{2^m}{L} \leq 0.01$

$$\Rightarrow L \geq 100. \text{ Choose } L = 128 \text{ (} n = 7 \text{)}.$$

(b) Sampling rate = $4000 \times 1.25 = 5000$ Samples/sec.

Total transmission rate for 8 users =

$$= 5000 \times 7 \times 8 = 280 \text{ kbps.}$$

The minimum BW required for transmission with zero ISI is 140 kHz ($r=0$).

Using raised-cosine pulse with $r=0.2$, ~~the~~ we require a bandwidth of $140 \times 1.2 = 168$ kHz.

7.3-5 It is clear from Fig P7.3-5 that the minimum required bandwidth is 1 MHz.

$$\therefore \text{Transmission rate} = 2 \text{ Mbps.}$$

$$\text{Excess BW} = 0.2 \text{ MHz.}$$

$$\therefore r = \frac{0.2}{1} = 0.2.$$

7.3-4

(a) For the pulse to satisfy Nyquist Criterion of zero ISI, its spectrum must satisfy the equation:

$$\sum_{n=-\infty}^{\infty} P(\omega - n\omega_b) = \text{constant}.$$

Since the spectrum $P(\omega)$ has odd symmetry around $\omega = \pi \times 10^6$, it does satisfy the Nyquist Criterion.

(b) From FT tables

$$p(t) = \text{sinc}^2(10^6 t)$$

$p(t)$ goes to zero at $t = \pm 10^{-6}, \pm 2 \times 10^{-6}, \dots$

Hence pulse transmitted at a rate of 10^6 bps will have zero ISI.

(c) $R_b = 10^6$ bps = 1 Mbps.

Note that this rate requires a minimum of 0.5 MHz

bandwidth. The spectrum of the pulse extends to $2\pi \times 10^6$ rad/sec = 10^6 Hz = 1 MHz.

Therefore the excess BW over the minimum required BW is 0.5 MHz:

$$\therefore r = \frac{0.5}{0.5} = 1.$$

Solution HW# 13

(7.7-3, 7.8-1, ~~7.8-2~~)

7.7-3

- (a) In 8-ary signaling, each pulse represents $\log_2 8 = 3$ bits.

Therefore the bandwidth is reduced by a factor of 3 (i.e. from $B_{8\text{-ary}} = \frac{1}{3} B_{\text{binary}}$).

- (b) For the binary case, with $\pm A/2$ amplitudes
- $$\bar{P}_2 = \frac{1}{2} \left(\frac{A}{2}\right)^2 + \frac{1}{2} \left(\frac{A}{2}\right)^2 = \frac{A^2}{4} \text{ watts.}$$

For the 8-ary case, with $\pm A/2, \pm 3A/2, \pm 5A/2, \pm 7A/2$

$$\begin{aligned} \bar{P}_8 &= \frac{1}{8} \left[2\left(\frac{A}{2}\right)^2 + 2\left(\frac{3A}{2}\right)^2 + 2\left(\frac{5A}{2}\right)^2 + 2\left(\frac{7A}{2}\right)^2 \right] \\ &= \frac{1}{4} \left[\frac{A^2 + 9A^2 + 25A^2 + 49A^2}{4} \right] = \frac{21A^2}{4} \text{ watts.} \end{aligned}$$

\therefore Power is increased by a factor of 21.

- 7.8-1 (a) For full-width pulses, the ~~essential~~^{theoretical} bandwidth goes to infinity. However, the essential bandwidth for Polar signaling is R_b , that is 1 MHz.

(See Page 303 of your textbook).

- (b) For carrier modulated signal (PSK or ASK in this case are the same), the bandwidth is doubled, i.e. 2 MHz.

- (b) The spectrum of FSK looks like two spectra of ASK at f_{c0} & f_{c1} (spaced by 0.1 MHz).

The bandwidth is then 2.1 MHz.

