

Name: KEY

In a certain digital voice communication system, there are 4 voice signals, each of bandwidth 4 kHz. Samples of these signals are time-division multiplexed, quantized and binary coded. The error in sample amplitudes cannot be greater than 3% of the peak amplitude.

a) Determine the number of bits for the quantizer, n .

① $\frac{\Delta v}{2} \leq 0.03 m_p$ — ① & $\Delta v = \frac{2 m_p}{L}$ — ② ①

Substitute ② in ①

4 ① $\frac{m_p}{L} \leq 0.03 m_p \Rightarrow L \geq \frac{100}{3} = 33.333$

$n=5 \Rightarrow L = 2^5 = 32$

① $n=6 \Rightarrow L = 2^6 = 64 \checkmark$

$n = 6$

b) Find the transmission bandwidth B_T if Nyquist criterion pulses with roll-off factor $r=0.3$ are used. The sampling rate must be at least 15% above the Nyquist rate.

① Nyquist rate = $2(4 \text{ kHz}) = 8 \text{ kHz}$ or $8 \text{ k } \frac{\text{samples}}{\text{sec}}$

① Sampling rate = $1.15(8 \text{ k}) = 9.2 \text{ kHz}$

① # of bits = $9.2 \text{ k } \frac{\text{samples}}{\text{sec}} * 6 \frac{\text{bits}}{\text{sample}} = 55.2 \text{ k } \frac{\text{bits}}{\text{sec}}$

① 4 users total rate $\Rightarrow 55.2 \text{ k} * 4 = 220.8 \text{ k } \frac{\text{bits}}{\text{sec}}$

① Binary Baseband $B_T = \frac{R}{2} + r \frac{R}{2} = \frac{(1+r)R}{2}$

$B_T = \frac{1.3}{2} (220.8 \text{ k}) = 1.3(110.4 \text{ k})$

$= 143.52 \text{ kHz}$

$$= \frac{3312}{11040} = 14352$$

①