

Name: KEY

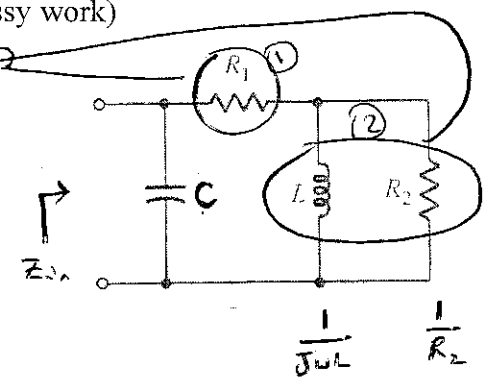
ver 1 ~~A~~ ver 2

For the shown circuit, design the value of C to get a resonance frequency equals to 20 kHz (30kHz)

Let  $R_1=3$  Ohms,  $L=1$  H,  $R_2=2$  Ohms.

(Be clear and organized. No credit will be given for messy work)

$$Z_{in} = \frac{1}{j\omega C} \parallel \left( R_1 + \frac{j\omega L R_2}{j\omega L + R_2} \right)$$



$$Z_{in} = \frac{1}{j\omega C} \parallel \frac{R_1 R_2 + j\omega L R_1 + j\omega L R_2}{j\omega L + R_2}$$

Substitute  $R_1, R_2$  &  $L$

$$Z_{in} = \frac{1}{j\omega C} \parallel \frac{6 + j\omega 3 + j\omega 2}{j\omega + 2}$$

(2) simplify

$$Z_{in} = \frac{1}{j\omega C} \parallel \frac{6 + j\omega 5}{2 + j\omega}$$

multiply by conjugate

$$Y_{in} = j\omega C + \frac{25\omega}{6 + j\omega 5} \cdot \frac{6 - j\omega 5}{6 - j\omega 5}$$

(1)

$$= j\omega C + \frac{12 - 45\omega + 5\omega^2}{36 + 25\omega^2}$$

$$\text{imag}(Y_{in}) = 0$$

$$\left( \frac{4\omega}{36 + 25\omega^2} \right) = 0 \Rightarrow C = \frac{4}{36 + 25\omega^2}$$

for 20kHz  $\Rightarrow \omega = (2\pi \times 20k) \Rightarrow C = 1.01 \times 10^{-11} = 10.1$  pF

for 30kHz  $\Rightarrow \omega = (2\pi \times 30k) \Rightarrow C = 4.5$  pF

(1)