

**King Fahd University of Petroleum & Minerals**  
 Electrical Engineering Department  
 EE205: Electric Circuits II (031)

**Quiz 7**

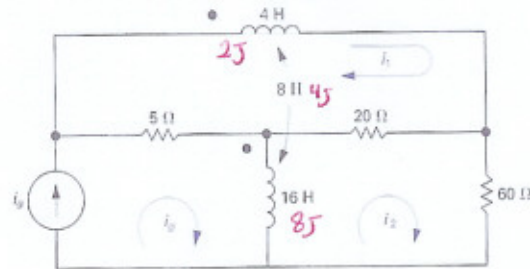
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Sec 01

a) What is the coefficient of coupling?

b) Assume that the physical structure of these coupled coils is such that  $\mathcal{P}_1 = \mathcal{P}_2$  (permeance 1 = permeance 2). What is the turns ratio  $N_1/N_2$ , if  $N_1$  is the number of turns on the 4H coil?



c) Write a set of mesh-current equations that describe the circuit in terms of the currents  $i_1$  and  $i_2$  in the frequency domain, where the source current is known and it has  $\omega = 0.5$  rad/s. (Hint: first represent in the  $j\omega$  domain)

$$a) \quad M = k\sqrt{L_1 L_2} \Rightarrow k = \frac{M}{\sqrt{L_1 L_2}} = \frac{8}{\sqrt{4 \cdot 16}} = 1$$

$$b) \quad L_1 = N_1^2 \mu, \quad L_2 = N_2^2 \mu$$

$$\frac{L_1}{L_2} = \frac{N_1^2 \mu}{N_2^2 \mu} \Rightarrow \frac{N_1}{N_2} = \sqrt{\frac{L_1}{L_2}} = \sqrt{\frac{4}{16}} = \sqrt{\frac{1}{4}} = \frac{1}{2}$$

$$c) \quad j\omega L_1 = j(0.5)(4) = 2j$$

$$j\omega L_2 = j(0.5)(16) = 8j$$

$$j\omega M = j(0.5)(8) = 4j$$

$$20(i_1 - i_2) + 5(i_1 - i_3) + 2j i_1 + 4j(i_3 - i_2) = 0$$

$$60 i_2 + 8j(i_2 - i_3) - 4j i_1 + 20(i_2 - i_1) = 0$$