

P. 18.19  $g_{11} = \frac{I_1}{V_1} \Big|_{I_2=0}$      $g_{21} = \frac{I_2}{V_1} \Big|_{I_2=0}$

$V_1 = 200 I_1 + 800 I_1 = 1000 I_1 \Rightarrow g_{11} = 10^{-3} S$

$V_- = \frac{1000}{1500} V_2 = V_+ \quad V_+ = \frac{800}{1000} V_1$

$\therefore \frac{1000}{1500} V_2 = \frac{800}{1000} V_1 \quad \therefore g_{21} = 1.2$

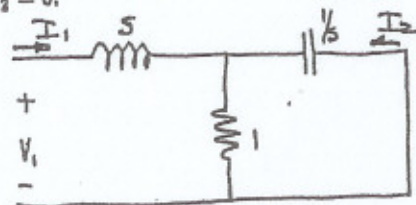
$g_{12} = \frac{I_1}{I_2} \Big|_{V_1=0} \quad g_{22} = \frac{I_2}{I_2} \Big|_{V_1=0}$

$I_1 = 0; \quad \therefore g_{12} = 0$

Also,  $V_+ = 0; \quad \therefore g_{22} = \frac{V_2}{I_2} = 40 \Omega$

P 18.20

$V_2 = 0;$



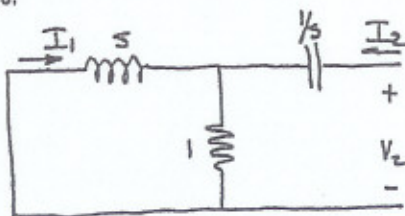
$\frac{V_1}{I_1} = s + 1 \parallel (1/s) = \frac{s^2 + s + 1}{s + 1}$

$\therefore y_{11} = \frac{I_1}{V_1} \Big|_{V_2=0} = \frac{s + 1}{s^2 + s + 1}$

$I_2 = \frac{-1}{1 + (1/s)} I_1 = \frac{-s}{s + 1} I_1 = \frac{-s}{s + 1} \left( \frac{s + 1}{s^2 + s + 1} \right) V_1$

$\therefore y_{21} = \frac{I_2}{V_1} \Big|_{V_2=0} = \frac{-s}{s^2 + s + 1}$

$V_1 = 0;$



$\frac{V_2}{I_2} = (1/s) + 1 \parallel s = \frac{1}{s} + \frac{s}{s + 1} = \frac{s^2 + s + 1}{s(s + 1)}$

$\therefore y_{22} = \frac{I_2}{V_2} \Big|_{V_1=0} = \frac{s(s + 1)}{s^2 + s + 1}$

$I_1 = \frac{-1}{s + 1} I_2 = \frac{-1}{s + 1} \left[ \frac{s(s + 1)}{s^2 + s + 1} \right] I_2$

$\therefore y_{12} = \frac{I_1}{V_2} \Big|_{V_1=0} = \frac{-s}{s^2 + s + 1}$

# 18.30 from Table 18.2

$I_2 = \frac{y_{21} V_1}{1 + y_{22} Z_L + y_{11} Z_g + \Delta y Z_g Z_L} = 0.0714 A$

$P_{R_L} = \frac{1}{2} I_2^2 R_L = 0.225 W$

$\frac{I_2}{I_1} = \frac{y_{21}}{y_{11} + \Delta y Z_L} = -14.294$

$\Rightarrow I_1 = -0.005 A$

$P_g = \frac{1}{2} I_1 V_1 = \frac{1}{2} (1) (-0.005) = -0.0025 W$

$\frac{P_o}{P_i} = 100$

HW 13

1/2

$$P 18.38 \quad a'_{11} = -\frac{\Delta h}{h_{21}} = \frac{-0.02}{-0.1} = 0.2$$

$$a'_{12} = -\frac{h_{11}}{h_{21}} = \frac{-150}{-0.1} = 1500$$

$$a'_{21} = -\frac{h_{22}}{h_{21}} = \frac{-10^{-4}}{-0.1} = 10^{-3}$$

$$a'_{22} = -\frac{1}{h_{21}} = \frac{-1}{-0.1} = 10$$

$$a''_{11} = \frac{1}{g_{21}} = \frac{1}{20} = 0.05$$

$$a''_{12} = \frac{g_{22}}{g_{21}} = \frac{24 \times 10^3}{20} = 1200$$

$$a''_{21} = \frac{g_{11}}{g_{21}} = \frac{0.01}{20} = 5 \times 10^{-4}$$

$$a''_{22} = \frac{\Delta g}{g_{21}} = \frac{320}{20} = 10$$

$$a_{11} = a'_{11}a''_{11} + a'_{12}a''_{21} = (0.2)(0.05) + (1500)(5 \times 10^{-4}) = 0.76$$

$$a_{12} = a'_{11}a''_{12} + a'_{12}a''_{22} = (0.2)(1200) + (1500)(10) = 24,240$$

$$a_{21} = a'_{21}a''_{11} + a'_{22}a''_{21} = (10^{-3})(0.05) + (10)(5 \times 10^{-4}) = 5.1 \times 10^{-3}$$

$$a_{22} = a'_{21}a''_{12} + a'_{22}a''_{22} = (10^{-3})(1200) + (10)(10) = 161.2$$

$$V_2 = \frac{Z_L V_g}{(a_{11} + a_{21} Z_g) Z_L + a_{12} + a_{22} Z_g}$$

$$= \frac{(1000)(109.5)}{[0.76 + (5.1 \times 10^{-3})(20)(1000)] + 24,240 + (161.2)(20)} = 3.87 \text{ V}$$

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