

Electrical Power and Energy Systems 25 (2003) 695-704

ELECTRICAL POWER & ENERGY SYSTEMS

www.elsevier.com/locate/ijepes

# Coordinated design of a PSS and an SVC-based controller to enhance power system stability

## M.A. Abido\*, Y.L. Abdel-Magid

Department of Electric Engineering, King Fahd University of Petroleum and Minerals, KFUMP Box No. 183, Dhahran 31261, Saudi Arabia

## Abstract

Power system stability enhancement via robust coordinated design of a power system stabilizer and a static VAR compensator-based stabilizer is thoroughly investigated in this paper. The coordinated design problem of robust excitation and SVC-based controllers over a wide range of loading conditions and system configurations are formulated as an optimization problem with an eigenvalue-based objective function. The real-coded genetic algorithm is employed to search for optimal controller parameters. This study also presents a singular value decomposition-based approach to assess and measure the controllability of the poorly damped electromechanical modes by different control inputs. The damping characteristics of the proposed schemes are also evaluated in terms of the damping torque coefficient over a wide range of loading conditions. The proposed stabilizers are tested on a weakly connected power system. The non-linear simulation results and eigenvalue analysis show the effectiveness and robustness of the proposed approach over a wide range of loading conditions. © 2003 Published by Elsevier Science Ltd.

Keywords: Power system stabilizer; Flexible alternating current transmission systems devices; Static VAR compensator; Genetic algorithms

## 1. Introduction

Since 1960s, low frequency oscillations have been observed when large power systems are interconnected by relatively weak tie lines. These oscillations may sustain and grow to cause system separation if no adequate damping is available [1,2]. Nowadays, the conventional power system stabilizer (CPSS) is widely used by power system utilities.

Generally, it is important to recognize that machine parameters change with loading make the machine behavior quite different at different operating conditions. Since these parameters change in a rather complex manner, a set of stabilizer parameters, which stabilizes the system under a certain operating condition, may no longer yield satisfactory results when there is a drastic change in power system operating conditions and configurations. Hence, power system stabilizers (PSSs) should provide some degree of robustness to the variations in system parameters, loading conditions, and configurations.

 $H_{\infty}$  optimization techniques [3,4] have been applied to robust PSS design problem. However, the importance and difficulties in the selection of weighting functions of  $H_{\infty}$  optimization problem have been reported. In addition, the additive and/or multiplicative uncertainty representation cannot treat situations, where a nominal stable system becomes unstable after being perturbed [5]. Moreover, the pole-zero cancellation phenomenon associated with this approach produces closed loop poles whose damping is directly dependent on the open loop system (nominal system) [6]. On the other hand, the order of the  $H_{\infty}$ -based stabilizer is as high as that of the plant. This gives rise to complex structure of such stabilizers and reduces their applicability.

Kundur et al. [7] have presented a comprehensive analysis of the effects of the different CPSS parameters on the overall dynamic performance of the power system. It is shown that the appropriate selection of CPSS parameters results in satisfactory performance during system upsets. In addition, Gibbard [8] demonstrated that the CPSS provide satisfactory damping performance over a wide range of system loading conditions. Robust design of CPSSs in multi-machine power systems using genetic algorithm is presented in Ref. [9], where several loading conditions are considered in the design process.

Although PSSs provide supplementary feedback stabilizing signals, they suffer a drawback of being liable to cause great variations in the voltage profile and they may even

<sup>\*</sup> Corresponding author. Tel.: +966-3-860-4379; fax: +966-3-860-3535. *E-mail address:* mabido@kfopm.edu.sa (M.A. Abido).

<sup>0142-0615/03/\$ -</sup> see front matter @ 2003 Published by Elsevier Science Ltd. PII: \$0142-0615(02)00124-2

result in leading power factor operation under severe disturbances. The recent advances in power electronics have led to the development of the flexible alternating current transmission systems (FACTS). Generally, a potential motivation for the accelerated use of FACTS devices is the deregulation environment in contemporary utility business. Along with primary function of the FACTS devices, the real power flow can be regulated to mitigate the low frequency oscillations and enhance power system stability.

Recently, several FACTS devices have been implemented and installed in practical power systems [10, 11]. In the literature, a little work has been done on the coordination problem investigation of excitation and FACTS-based stabilizers. Mahran et al. [12] presented a coordinated PSS and SVC control for a synchronous generator. However, the proposed approach uses recursive least squares identification, which reduces its effectiveness for on-line applications. Rahim and Nassimi [13] presented optimum feedback strategies for both SVC and exciter controls. However, the proposed controller requires some or all states to be measurable or estimated. Moreover, it leads to a centralized controller for multi-machine power systems, which reduces its applicability and reliability. Noroozian and Anderson [14] presented a comprehensive analysis of damping of power system electromechanical oscillations using FACTS, where the impact of transmission line loading and load characteristics on the damping effect of these devices have been discussed. Wang and Swift [15] have discussed the damping torque contributed by FACTS devices, where several important points have been analyzed and confirmed through simulations. However, all controllers were assumed proportional and no efforts have been done towards the controller design. On the other hand, it is necessary to measure the electromechanical mode controllability in order to assess the effectiveness of different controllers and form a clear inspiration about the coordination problem requirements. A comprehensive study of the coordination problem requirements among PSSs and different FACTS devices has been presented in Ref. [16]. However, no efforts have been done towards the coordinated design of the stabilizers investigated.

In this paper, a comprehensive assessment of the effects of the excitation and SVC control when applied independently and also through coordinated application has been carried out. The design problem is transformed into an optimization problem, where the real-coded genetic algorithm (RCGA) is employed to search for the optimal settings of stabilizer parameters. A controllability measure-based on singular value decomposition (SVD) is used to identify the effectiveness of each control input. In addition, the damping torque coefficient is evaluated with the proposed stabilizers over a wide range of loading conditions. For completeness, the eigenvalue analysis and non-linear simulation results are carried out to demonstrate the effectiveness and robustness of the proposed stabilizers to enhance system dynamic stability.

## 2. Power system model

#### 2.1. Generator

In this study, a single machine infinite bus system as shown in Fig. 1 is considered. The generator is equipped with PSS and the system has an SVC at the midpoint of the line as shown in Fig. 1. The line impedance is Z = R + jXand the generator has a local load of admittance  $Y_L = g + jb$ . The generator is represented by the third-order model comprising of the electromechanical swing equation and the generator internal voltage equation [1,2]. The swing equation is divided into the following equations

$$\rho\delta = \omega_b(\omega - 1) \tag{1}$$

$$\rho\omega = (P_{\rm m} - P_{\rm e} - D(\omega - 1))/M \tag{2}$$

where  $P_{\rm m}$  and  $P_{\rm e}$  are the input and output powers of the generator, respectively; *M* and *D* are the inertia constant and damping coefficient, respectively;  $\delta$  and  $\omega$  are the rotor angle and speed, respectively;  $\rho$  is the derivative operator d/dt. The output power of the generator can be expressed in terms of the *d*-axis and *q*-axis components of the armature current, *i*, and terminal voltage, *v*, as

$$P_{\rm e} = v_d i_d + v_q i_q \tag{3}$$

The internal voltage,  $E'_{q}$ , equation is

$$\rho E'_{q} = (E_{\rm fd} - (x_d - x'_d)i_d - E'_q)/T'_{\rm do} \tag{4}$$

Here,  $E_{\rm fd}$  is the field voltage;  $T'_{\rm do}$  is the open circuit field time constant;  $x_d$  and  $x'_d$  are *d*-axis reactance and *d*-axis transient reactance of the generator, respectively.

## 2.2. Exciter and PSS

The IEEE Type-ST1 excitation system shown in Fig. 2 is considered. It can be described as

$$\rho E_{\rm fd} = (K_A (V_{\rm ref} - \nu + u_{\rm PSS}) - E_{\rm fd})/T_A \tag{5}$$

where  $K_A$  and  $T_A$  are the gain and time constant of the excitation system, respectively;  $V_{ref}$  is the reference voltage. As shown in Fig. 2, a conventional lead-lag PSS is installed in the feedback loop to generate a stabilizing signal  $u_{PSS}$ . In



Fig. 1. Single machine infinite bus system.



Fig. 2. IEEE Type-ST1 excitation system with PSS.

Eq. (5), the terminal voltage v can be expressed as

$$v = (v_d^2 + v_q^2)^{1/2} \tag{6}$$

$$v_d = x_q i_q \tag{7}$$

$$v_q = E'_q - x'_d i_d \tag{8}$$

where  $x_q$  is the q-axis reactance of the generator.

## 2.3. SVC-based stabilizer

Fig. 3 shows the block diagram of an SVC with a leadlag compensator. The susceptance of the SVC, B, can be expressed as

$$\rho B = (K_{\rm s}(B_{\rm ref} - u_{\rm SVC}) - B)/T_{\rm s} \tag{9}$$

where  $B_{ref}$  is the reference susceptance of SVC;  $K_s$  and  $T_s$  are the gain and time constant of the SVC. As shown in Fig. 3, a conventional lead-lag controller is installed in the feedback loop to generate the SVC stabilizing signal  $u_{SVC}$ .

#### 2.4. Linearized model

In the design of electromechanical mode damping controllers, the linearized incremental model around a nominal operating point is usually employed [1,2]. Linearizing the expressions of  $i_d$  and  $i_q$  and substituting into the linear form of Eqs. (1)–(9), yield the following linearized



Fig. 3. SVC with lead-lag controller.

## power system model

$$\begin{bmatrix} \rho \Delta \delta \\ \rho \Delta \omega \\ \rho \Delta E'_{q} \\ \rho \Delta E_{fd} \end{bmatrix} = \begin{bmatrix} 0 & 377 & 0 & 0 \\ -\frac{K_{1}}{M} & -\frac{D}{M} & -\frac{K_{2}}{M} & 0 \\ -\frac{K_{4}}{T'_{do}} & 0 & -\frac{K_{3}}{T'_{do}} & \frac{1}{T'_{do}} \\ -\frac{K_{A}K_{5}}{T_{A}} & 0 & -\frac{K_{A}K_{6}}{T_{A}} & -\frac{1}{T_{A}} \end{bmatrix} \\ \times \begin{bmatrix} \Delta \delta \\ \Delta \omega \\ \Delta E'_{q} \\ \Delta E_{fd} \end{bmatrix} + \begin{bmatrix} 0 & 0 \\ 0 & -\frac{K_{pB}}{M} \\ 0 & -\frac{K_{qB}}{T'_{do}} \\ \frac{K_{A}}{T_{A}} & -\frac{K_{A}K_{vB}}{T_{A}} \end{bmatrix} \begin{bmatrix} u_{PSS} \\ \Delta B \end{bmatrix}$$
(10)

In short;

$$\rho X = AX + HU \tag{11}$$

Here, the state vector X is  $[\Delta \delta, \Delta \omega, \Delta E'_q, \Delta E_{\rm fd}]^{\rm T}$  and the control vector U is  $[u_{\rm PSS}, \Delta B]^{\rm T}$ . The block diagram of the linearized power system model is depicted as shown in Fig. 4, where  $K_1 - K_6$ ,  $K_p$ ,  $K_q$ , and  $K_v$  are linearization constants defined as

$$K_{1} = \frac{\partial P_{e}}{\partial \delta}, \qquad K_{2} = \frac{\partial P_{e}}{\partial E'_{q}}, \qquad K_{pB} = \frac{\partial P_{e}}{\partial B},$$

$$K_{4} = \frac{\partial E_{q}}{\partial \delta}, \qquad K_{3} = \frac{\partial E_{q}}{\partial E'_{q}}, \qquad K_{qB} = \frac{\partial E_{q}}{\partial B}, \qquad (12)$$

$$K_{qB} = \frac{\partial V}{\partial B}, \qquad K_{qB} = \frac{\partial V_{pB}}{\partial B},$$

$$K_5 = \frac{\partial V}{\partial \delta}, \qquad K_6 = \frac{\partial V}{\partial E'_q}, \qquad K_{\nu B} = \frac{\partial V}{\partial B}$$

## 3. The proposed approach

## 3.1. Electromechanical mode identification

The state equations of the linearized model can be used to determine the eigenvalues of the system matrix A. Out of these eigenvalues, there is a mode of oscillations related to machine inertia. For the stabilizers to be effective, it is extremely important to identify the eigenvalue associated with the electromechanical mode. In this study, the participation factors method [17] is used.

## 3.2. Controllability measure

To measure the controllability of the electromechanical mode by a given input, the SVD is employed in this study.



Fig. 4. Block diagram of the linearized model.

Mathematically, if *G* is an  $m \times n$  complex matrix, then there exist unitary matrices *W* and *V* with dimensions of  $m \times m$  and  $n \times n$ , respectively, such that *G* can be written as

$$G = W \Sigma V^H \tag{13}$$

where

$$\Sigma = \begin{bmatrix} \Sigma_1 & 0\\ 0 & 0 \end{bmatrix},\tag{14}$$

 $\Sigma_1 = \operatorname{diag}(\sigma_1, ..., \sigma_r)$  with  $\sigma_1 \ge \cdots \ge \sigma_r \ge 0$ 

where  $r = \min\{m, n\}$  and  $\sigma_1, ..., \sigma_r$  are the singular values of *G*.

The minimum singular value  $\sigma_r$  represents the distance of the matrix *G* from all the matrices with a rank of r - 1. This property can be utilized to quantify modal controllability [18]. In this study, the matrix *H* in Eq. (11) can be written as  $H = [h_1, h_2]$ , where  $h_i$  is the column of matrix *H* corresponding to the *i*th input. The minimum singular value,  $\sigma_{\min}$ , of the matrix  $[\lambda I - Ah_i]$  indicates the capability of the *i*th input to control the mode associated with the eigenvalue  $\lambda$ . As a matter of fact, higher the  $\sigma_{\min}$ , the higher the controllability of this mode by the input considered. Having been identified, the controllability of the electromechanical mode can be examined with both inputs in order to identify the most effective one to control that mode.

## 3.3. Stabilizer design

A widely used conventional lead-lag structure for both excitation and SVC-based stabilizers, shown in Figs. 2 and 3, is considered. In this structure, the washout time constant  $T_{\rm w}$  and the time constants  $T_2$  and  $T_4$  are usually prespecified. The controller gain *K* and time constants  $T_1$  and  $T_3$  are to be determined.

In this study, several loading conditions representing nominal, light, high, and leading power factor without and with system parameter uncertainties are considered to ensure the robustness of the proposed stabilizers. In the stabilizer design process, it is aimed to maximize the damping ratio,  $\zeta$ , of the poorly damped electromechanical mode eigenvalues at the entire range of the specified loading conditions. Therefore, the following eigenvalue-based objective function J is used.

## $J = \min{\{\zeta_i : \zeta_i \text{ is the electromechanical mode}\}}$

## damping ratio of the *i*th loading condition $\{15\}$

In the optimization process, it is aimed to maximize J while satisfying the problem constraints that are the optimized parameter bounds. Therefore, the design problem can be formulated as the following optimization problem.

subject to

$$K^{\min} \le K \le K^{\max} \tag{17}$$

$$T_1^{\min} \le T_1 \le T_1^{\max} \tag{18}$$

$$T_3^{\min} \le T_3 \le T_3^{\max} \tag{19}$$

The proposed approach employs RCGA to solve this optimization problem and search for optimal or near optimal set of the optimized parameters. To investigate the capability of PSS and SVC controller when applied individually and also through coordinated application, both are designed independently first and then in a coordinated manner.

## 3.4. Damping torque coefficient calculation

To assess the effectiveness of the designed stabilizers, the damping torque coefficient is evaluated and analyzed. The torque can be decomposed into synchronizing and damping components as follows

$$\Delta T_{\rm e}(t) = K_{\rm syn} \Delta \delta(t) + K_{\rm d} \Delta \omega(t) \tag{20}$$

where  $K_{\text{syn}}$  and  $K_{\text{d}}$  are the synchronizing and damping torque coefficients, respectively. It is worth mentioning that  $K_{\text{d}}$  is a damping measure to the electromechanical mode of oscillations [19].

In order to calculate  $K_{syn}$  and  $K_d$ , the error between the actual torque deviation and that obtained by summing both components can be defined as

$$E(t) = \Delta T_{\rm e}(t) - (K_{\rm syn}\Delta\delta(t) + K_{\rm d}\Delta\omega(t))$$
(21)

Then  $K_{syn}$  and  $K_d$  are computed to minimize the sum of the squared errors over the simulation period  $t_{sim}$  as

$$\sum_{n=1}^{N} [E]^2 = \sum_{n=1}^{N} [\Delta T_{\rm e} - (K_{\rm syn}\Delta\delta + K_{\rm d}\Delta\omega)]^2$$
(22)

where  $t_{sim} = NT_{samp}$ ,  $T_{samp}$  is the sampling period. Thus, these coefficients should satisfy

$$\frac{\partial}{\partial K_{\text{syn}}} \sum_{k=1}^{N} [E]^2 = 0$$
 and  $\frac{\partial}{\partial K_d} \sum_{k=1}^{N} [E]^2 = 0$  (23)

That yields

$$\sum_{n=1}^{N} \Delta T_{\rm e} \Delta \delta = K_{\rm syn} \sum_{n=1}^{N} \left[ \Delta \delta \right]^2 + K_{\rm d} \sum_{n=1}^{N} \left[ \Delta \omega \Delta \delta \right] \tag{24}$$

$$\sum_{n=1}^{N} \Delta T_{e} \Delta \omega = K_{d} \sum_{n=1}^{N} [\Delta \omega]^{2} + K_{syn} \sum_{n=1}^{N} [\Delta \omega \Delta \delta]$$
(25)

Solving Eqs. (24) and (25),  $K_{syn}$  and  $K_d$  can be calculated.

## 4. Implementation

#### 4.1. Real-coded genetic algorithm

Genetic algorithms (GA) are search algorithms based on the mechanics of natural selection and survival-of-thefittest. One of the most important features of the GA as a method of control system design is the fact that minimal knowledge of the plant under investigation is required. Since the GA optimize, a performance index based on input/output relationships only, far less information than other design techniques is needed. Further, as the GA search is directed towards increasing a specified performance, the net result is a controller, which ultimately meets the performance criteria. In addition, because the GA do not need an explicit mathematical relationship between the performance of the system and the search update, the GA offer a more general optimization methodology than conventional analytical techniques.

Due to difficulties of binary representation when dealing with continuous search space with large dimension, the proposed approach has been implemented using RCGA [20]. A decision variable  $x_i$  is represented by a real number within its lower limit  $a_i$  and upper limit  $b_i$ , i.e.  $x_i \in [a_i, b_i]$ . The RCGA crossover and mutation operators are described as follows:

*Crossover*. A blend crossover operator (BLX- $\alpha$ ) has been employed in this study. This operator starts by choosing randomly a number from the interval  $[x_i - \alpha(y_i - x_i), y_i + \alpha(y_i - x_i)]$ , where  $x_i$  and  $y_i$  are the *i*th parameter values of the parent solutions and  $x_i < y_i$ . To ensure the balance between exploitation and exploration of the search space,  $\alpha = 0.5$  is selected. This operator is depicted in Fig. 5.

*Mutation*. The non-uniform mutation operator has been employed in this study. In this operator, the new value  $x'_i$  of the parameter  $x_i$  after mutation at generation t is given as

$$x'_{i} = \begin{cases} x_{i} + \Delta(t, b_{i} - x_{i}), & \text{if } \tau = 0, \\ x_{i} - \Delta(t, x_{i} - a_{i}), & \text{if } \tau = 1, \end{cases}$$
(26)

$$\Delta(t, y) = y(1 - r^{(1 - (t/g_{\max}))^{\beta}})$$
(27)

where  $\tau$  is a binary random number, r is a random number  $r \in [0, 1]$ ,  $g_{\text{max}}$  is the maximum number of generations, and  $\beta$  is a positive constant chosen arbitrarily. In this study,  $\beta = 5$  was selected. This operator gives a value  $x_i^t \in [a_i, b_i]$  such that the probability of returning a value close to  $x_i$  increases as the algorithm advances. This makes uniform search in the initial stages, where t is small and very locally at the later stages.

#### 4.2. RCGA application

Linearizing the system model at each loading condition of the specified range, the electromechanical mode is identified and its damping ratio is calculated. Then, the objective function is evaluated and RCGA is applied to



Fig. 5. Blend crossover operator (BLX-α).



Fig. 6. Flow chart of the proposed design approach.

search for optimal settings of the optimized parameters of the proposed control schemes. In our implementation, the crossover and mutation probabilities of 0.9 and 0.01, respectively, are found to be quite satisfactory. The number of individuals in each generation is selected to be 100. In addition, the search will terminate if the best solution does not change for more than 50 generations or the number of generations reaches 500. The computational flow chart of the proposed design approach is shown in Fig. 6.

## 5. Results and discussions

## 5.1. Loading conditions and proposed stabilizers

In this study, the PSS and SVC-based controller parameters are optimized over a wide range of operating conditions and system parameter uncertainties. Four loading conditions representing nominal, light, heavy, and leading power factor are considered. Each loading condition is considered without and with parameter uncertainties as given in Table 1. Hence, the total number of points considered for the design process is 16.

| Table 1            |     |           |               |
|--------------------|-----|-----------|---------------|
| Loading conditions | and | parameter | uncertainties |

| Loading condition $(P, Q)$ (pu)                | Parameter uncertainties  |  |
|--|--|--|
| Nominal (1.0, 0.015)                           | No parameter uncertainty   |  |
| Light (0.3, 0.100)                             | 30% increase of line reactance X   |  |
| Heavy (1.1, 0.100)<br>Leading pf (0.7, -0.300) | 30% decrease of field time constant $T'_{do}$ 25% decrease of machine inertia <i>M</i> |  |



The proposed approach has been implemented on a weakly connected power system. The detailed data of the power system used in this study is given in Ref. [1]. The convergence rate of the objective function J when PSS and SVC controller designed individually and through coordinated design is shown in Fig. 7. It can be seen that the damping characteristics of the coordinated design approach are much better than those of the individual design one. The final settings of the optimized parameters for the proposed stabilizers are given in Table 2.

## 5.2. Mode controllability measure

With each input signal, the minimum singular value  $\sigma_{\min}$ has been estimated to measure the controllability of the electromechanical mode from that input. Fig. 8 shows  $\sigma_{\min}$ with loading conditions over the range of  $P_e = [0.05 - 1.4]$ pu and  $Q \in \{-0.4, 0.0, 0.4\}$  pu. At each loading condition in the specified range, the system model is linearized, the electromechanical mode is identified, and the SVD-based controllability measure is implemented. It can be seen that the electromechanical mode controllability is almost the same with both PSS and SVC. This controllability increases with the loading.

## 5.3. Damping torque coefficient

In order to evaluate the effectiveness of the proposed stabilizers, the damping torque coefficient has been

Table 2 Optimal parameter settings of the proposed stabilizers

|       | Individual design |        | Coordinated design |        |
|-------|-------------------|--------|--------------------|--------|
|       | PSS               | SVC    | PSS                | SVC    |
| K     | 17.849            | 300.00 | 43.457             | 99.737 |
| $T_1$ | 0.4334            | 0.2143 | 0.1647             | 0.7650 |
| $T_2$ | 0.1000            | 0.3000 | 0.1000             | 0.3000 |
| $T_3$ | _                 | 0.0100 | _                  | 0.3789 |
| $T_4$ | _                 | 0.3000 | _                  | 0.3000 |



Fig. 8. Minimum singular value with loading variations. (a) Q = -0.4 pu, (b) Q = 0.0 pu, (c) Q = 0.4 pu.

estimated with PSS and SVC-based stabilizer when designed individually and in coordinated manner. Fig. 9 shows K<sub>d</sub> versus the loading variations with PSS only, SVCbased stabilizer only, and coordinated PSS and SVC-based

(b) Q = 0.0 pu, (c) Q = 0.4 pu.

stabilizer. Consistent with the findings of Refs. [15,16], the SVC provides negative damping at low loading conditions in particular with positive Q. This problem is alleviated with the coordinated design approach. It can be also seen that PSS outperforms SVC and does not suffer from such a problem. It is also evident that the coordinated design of

1.40

1.40

1.40

Table 3 System eigenvalues with the proposed stabilizers at nominal loading

| No control            | PSS<br>only                 | SVC<br>only              | Coordinated<br>design            |
|-----------------------|-----------------------------|--------------------------|----------------------------------|
| +0.30<br>± j4.96;     | $-1.80 \pm j3.52;$<br>0.466 | $-0.57 \pm j5.98; 0.095$ | $-2.21 \pm j3.05;$<br>0.587      |
| -10.39<br>$\pm i3.29$ | $-3.24 \pm$ j9.00           | $-2.98 \pm j1.06$        | $-7.01 \pm j12.20$               |
| -                     | - 20.12;<br>- 0.204         | -20.24; -12.57           | $-2.85 \pm j0.34$                |
| -                     | _                           | - 6.96; - 0.204<br>-     | -17.93; -14.77<br>-0.210; -0.200 |

Table 4 System eigenvalues with the proposed stabilizers at light loading

| No control                  | PSS<br>only                 | SVC<br>only                 | Coordinated design          |
|-----------------------------|-----------------------------|-----------------------------|-----------------------------|
| $-0.01 \pm j4.85;$<br>0.002 | $-1.16 \pm j4.67;$<br>0.241 | $-0.21 \pm j4.85;$<br>0.043 | $-1.31 \pm j5.03;$<br>0.252 |
| $-10.09 \pm$                | $-5.47 \pm j6.26$           | $-9.84 \pm j3.03$           | $-6.94 \pm j5.92$           |
| _                           | -16.93;<br>-0.202           | $-3.40\pm j0.82$            | $-3.03 \pm j0.40$           |
| -                           | _                           | -19.96; -0.200              | -20.50; -13.80              |
| -                           | -                           | —                           | -0.204, -0.200              |

PSS and SVC-based stabilizer provides great damping characteristics and enhance significantly the system stability compared to individual design of these stabilizers.

#### 5.4. Eigenvalue analysis and non-linear simulation

For completeness and verification, all the proposed stabilizers were tested at the following disturbances and loading conditions.

- (a) Nominal loading (P, Q) = (1.0, 0.015) pu with 6-cycle three-phase fault.
- (b) Light loading (P,Q) = (0.3, 0.015) pu with 6-cycle three-phase fault.
- (c) Heavy loading (P,Q) = (1.1, 0.4) pu with 3-cycle three-phase fault.

 Table 5

 System eigenvalues with the proposed stabilizers at heavy loading

| No control  | PSS<br>only                                      | SVC<br>only                                   | Coordinated design                                   |
|---|--|---|--|
| $+0.49 \pm j3.69;$<br>-0.131<br>-10.58 $\pm$<br>j3.69 | $-1.02 \pm j2.84;$<br>0.338<br>$-4.05 \pm j8.68$ | $-0.49 \pm j5.23;$<br>0.093<br>-20.52; -10.87 | $-1.73 \pm j1.67;$<br>0.719<br>$-7.67 \pm j12.65$    |
| -   | - 20.05; - 0.207<br>-<br>-                       | -9.02; -3.71<br>-1.74; -0.217<br>-            | $-15.69 \pm j2.74$<br>-3.90; -2.74<br>-0.226; -0.200 |



Fig. 10. System response for 6-cycle fault disturbance with nominal loading. (a) Rotor angle response; (b) PSS stabilizing signal; (c)  $B_{SVC}$  variation.

The system eigenvalues without and with the proposed stabilizers at these loading conditions are given in Tables 3-5, respectively, where the first row represents the electromechanical mode eigenvalues and their damping ratios. It is clear that the system stability is greatly enhanced with the proposed stabilizers. It can also be seen that the coordinated design outperforms the individual



Fig. 11. System response for 3-cycle fault disturbance with heavy loading. (a) Rotor angle response; (b) PSS stabilizing signal; (c)  $B_{SVC}$  variation.

design at all points considered in the sense that the damping ratios of the electromechanical modes at all points are greatly improved.

The non-linear time domain simulations have been carried out at the disturbances and the loading conditions specified above. Fig. 10 shows the system response with 6-cycle fault disturbance at the nominal loading condition. It can be seen that the coordinated design

approach provides the best damping characteristics and enhance greatly the first swing stability. The response of the proposed schemes is compared to that of CPSS given in Ref. [1]. It is clear that the system response with the proposed PSS is better than that with the CPSS in the sense of the settling time is reduced. The stabilizing signal of PSS,  $U_{PSS}$ , and the susceptance of the SVC,  $B_{SVC}$ , when designed individually and in coordinated manner are compared and shown in Fig. 10(b) and (c), respectively. It is clear that the control effort is greatly reduced with the coordinated design approach.

Fig. 11 shows the results with a 3-cycle fault disturbance at a heavy loading condition. It is clear that the first swing stability is greatly improved with the coordinated design approach. This confirms the findings of Fig. 9. The proposed schemes outperform the CPSS and the control efforts are significantly reduced. This confirms the potential of the proposed approach for ultimate utilization of the control schemes to enhance the system dynamic stability.

## 6. Conclusion

In this study, the power system stability enhancement via PSS and SVC-based stabilizer when applied independently and also through coordinated application was discussed and investigated. For the proposed stabilizer design problem, an eigenvalue-based objective function to increase the system damping was developed. Then, the RCGA was implemented to search for the optimal stabilizer parameters. In addition, a controllability measure for the poorly damped electromechanical modes using a SVD approach was used to assess the effectiveness of the proposed stabilizers. The damping characteristics of the proposed schemes were also evaluated in terms of the damping torque coefficient. The proposed stabilizers have been tested on a weakly connected power system with different loading conditions. The eigenvalue analysis and non-linear simulation results show the effectiveness and robustness of the proposed stabilizers to enhance the system stability.

## Acknowledgements

The authors acknowledge the support of King Fahd University of Petroleum & Minerals via funded Project #FT/2000-25.

## References

- Yu YN. Electric power system dynamics. New York: Academic Press; 1983.
- [2] Sauer PW, Pai MA. Power system dynamics and stability. Englewood Cliffs, NJ, USA: Prentice-Hall; 1998.

- [3] Yang TC. Applying  $H_{\infty}$  optimisation method to power system stabilizer design. Parts 1 and 2. Int J Electr Power Energy Syst 1997; 19(1):29–43.
- [4] Asgharian R. A robust  $H_{\infty}$  power system stabilizer with no adverse effect on shaft torsional modes. IEEE Trans Energy Conv 1994;9(3): 475–81.
- [5] Vidyasagar M, Kimura H. Robust controllers for uncertain linear multivariable systems. Automatica 1986;22(1):85–94.
- [6] Kwakernaak H. Robust control and  $H_{\infty}$  optimization—tutorial. Automatica 1993;29(2):255–73.
- [7] Kundur P, Klein M, Rogers GJ, Zywno MS. Application of power system stabilizers for enhancement of overall system stability. IEEE Trans PWRS 1989;4(2):614–26.
- [8] Gibbard MJ. Robust design of fixed-parameter power system stabilizers over a wide range of operating conditions. IEEE Trans PWRS 1991;6(2):794-800.
- [9] Abdel-Magid YL, Abido MA, Al-Baiyat S, Mantawy AH. Simultaneous stabilization of multimachine power systems via genetic algorithms. IEEE PES, Paper #98 SM 322.
- [10] Hammad AE. Analysis of power system stability enhancement by static VAR compensators. IEEE Trans PWRS 1986;1(4):222-7.
- [11] Padiyar KR, Varma RK. Damping torque analysis of static VAR system oscillations. IEEE Trans PWRS 1991;6(2):458–65.
- [12] Mahran AR, Hogg BW, El-Sayed ML. Coordinated control of synchronous generator excitation and static VAR compensator. IEEE Trans Energy Conv 1992;7:615–22.

- [13] Rahim A, Nassimi S. Synchronous generator damping enhancement through coordinated control of exciter and SVC. IEE Proc Gener Transm Distrib 1996;143(2):211–8.
- [14] Noroozian M, Anderson G. Damping of power system oscillations by use of controllable components. IEEE Trans PWRD 1994;9(4): 2046-54.
- [15] Wang HF, Swift FJ. A unified model for the analysis of FACTS devices in damping power system oscillations. Part I. Single-machine infinite-bus power systems. IEEE Trans PWRD 1997;12(2):941–6.
- [16] Abido MA, Abdel-Magid YL. Analysis and design of power system stabilizers and FACTS based stabilizers using genetic algorithms. 14th Power Systems Computation Conference PSCC-2002, Session 14, Paper 4, Seville, Spain, June 24–28, 2002, CD-ROM.
- [17] Hsu YY, Chen CL. Identification of optimum location for stabilizer applications using participation factors. IEE Proc, Part C 1987;134(3): 238–44.
- [18] Hamdan AMA. An investigation of the significance of singular value decomposition in power system dynamics. Int J Electr Power Energy Syst 1999;21:417–24.
- [19] Failat EA, Bettayyeb M, Al-Duwaish H, Abido MA, Mantawy A. A neural network based approach for on-line dynamic stability assessment using synchronizing and damping torque coefficients. Electr Power Syst Res 1996;39(2):103–10.
- [20] Herrera F, Lozano M, Verdegay JL. Tackling real-coded genetic algorithms: operators and tools for behavioral analysis. Artif Intell Rev 1998;12(4):265–319.