

KING FAHD UNIVERSITY OF PETROLEUM & MINERALS  
ELECTRICAL ENGINEERING DEPARTMENT

EE380 [081]	SEC# _____	Quiz # 7
Name: <u>Key</u>	ID: _____	Grade: _____

1) A system has the characteristic equation

$$q(s) = s^3 + 4Ks^2 + (5 + K)s + 10 = 0.$$

The range of  $K$  for a stable system is:

- $K > 0.46$
- $K < 0.46$
- $0 < K < 0.46$
- Unstable for all  $K$

Routh Table:

$s^3$	1	$K+5$
$s^2$	$4K$	10
$s^1$	$a$	0
$s^0$	10	0

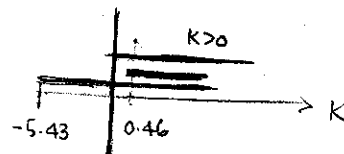
$$a = \frac{4K(K+5) - 10}{4K} > 0$$

$$\therefore 4K^2 + 20K - 10 > 0$$

$$K^2 + 5K - 2.5 > 0$$

$$(K - 0.46)(K + 5.435) > 0$$

$$\therefore \boxed{K > 0.46}$$



- 2) Utilizing the Routh-Hurwitz criterion, determine whether the following polynomials are stable or unstable:

$$p_1(s) = s^2 + 10s + 5 = 0$$

$$p_2(s) = s^4 + s^3 + 5s^2 + 20s + 10 = 0.$$

- $p_1(s)$  is stable,  $p_2(s)$  is stable  
  $p_1(s)$  is unstable,  $p_2(s)$  is unstable  
  $p_1(s)$  is unstable,  $p_2(s)$  is stable  
  $p_1(s)$  is stable,  $p_2(s)$  is unstable

$$P_1(s) = s^2 + 10s + 5$$

$s^2$	1	5	
$s^1$	10	0	$\Rightarrow P_1(s)$ is <u>stable</u>
$s^0$	5		

$$P_2(s) = s^4 + s^3 + 5s^2 + 20s + 10$$

$s^4$	1	5	10	
$s^3$	1	20	0	$\Rightarrow P_2(s)$ is <u>unstable</u>
$s^2$	-15	10		
$s^1$	$+\frac{310}{15}$	0		
$s^0$	10			

2 sign change

3) **A marginally stable system has poles on the  $j\omega$ -axis.**

- True
- False

4) **A system is stable if all poles lie in the right half-plane.**

- True
- False

5) **The Routh-Hurwitz criterion is a necessary and sufficient criterion for determining the stability of linear systems.**

- True
- False