

**KING FAHD UNIVERSITY OF PETROLEUM & MINERALS**

**ELECTRICAL ENGINEERING DEPARTMENT**

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**EE 360**

**MAJOR EXAM # 1**

**October 20, 2005**

**1:30 – 2:30 pm**

**Key Solution**

**Section:**

**Student Name:**

**Student I.D.#**

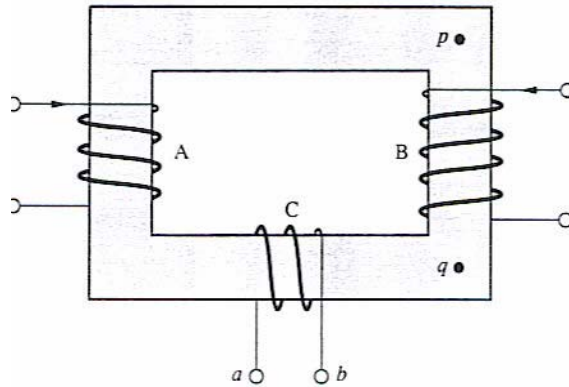
**Serial #**

<b>Question # 1</b>	
<b>Question # 2</b>	
<b>Total</b>	

**Q. 1)** The magnetic circuit shown below has a uniform cross-sectional area of  $5 \times 10^{-4} \text{ m}^2$  and a mean length of 0.4 m. Three coils (A, B, C) are wound on the cast steel core. Coil A has 200 turns and carries a current of 0.5 A. Coil B has 400 turns and carries a current of 0.75 A. Coil C has 100 turns. The relative permeability of the ferromagnetic material is 950.

**a)** Determine the **magnitude** and **direction** of the current flowing in coil C in order to produce a magnetic flux of  $0.45 \times 10^{-3}$  webers in a **counterclockwise** direction.

**b)** What should be the **magnitude** and **direction** of the current flowing in coil C in order to reverse the direction of the magnetic flux produced in part (a).



(50 Marks)

**Solution:**

**a)** From Amper's Law

$$200 * (0.5) + 400 * (0.75) + 100 * I_c = - \frac{0.4}{950 * 4 * \pi * 10^{-7} * 5 * 10^{-4}} * 0.45 * 10^{-3}$$

$$I_c = - 7 \text{ A (i.e., Coil C should carry a current of 7 A entering terminal "a")}$$

**b)**  $I_c = - 1 \text{ A (i.e., Coil C should carry a current of 1 A entering terminal "a")}$

**Q. 2)** A 15-kVA, 2400/240 V, transformer has a series equivalent impedance of  $Z_{e1} = 6 + j 8.5$  Ohm referred to the high voltage side. The shunt magnetizing branches are  $R_{c1} = 50$  kOhm, and  $X_{m1} = 15$  kOhm referred to the high voltage side.

**a)** If the transformer delivers rated current to a load at 240 V and 0.8 lagging power factor, calculate the primary voltage of the transformer referred to the high voltage side.

**b)** If the transformer delivers rated current to a load at 240 V and 0.8 lagging power factor for 12 hours, and delivers 75% of the rated current to the same load for the remaining 12 hours. Calculate the daily kilowatt-hour energy consumption by the load.

(50 Marks)

**Solution:**

$$\text{a) } V_2 = 240 \angle 0^\circ \text{ V ( or } V_2' = 2400 \angle 0^\circ \text{ V )}$$

$$I_2 = \frac{15000}{240} \angle -\cos^{-1} 0.8 = 62.5 \angle -36.9^\circ \text{ A (or } I_2' = 6.25 \angle -36.9^\circ \text{ A )}$$

**Considering the excitation branch between the secondary voltage and  $Z_{eq}$**

$$I_1 = 6.25 \angle -36.9^\circ + (2400 \angle 0^\circ) * \left( \frac{1}{50000} + j \frac{1}{15000} \right) = 5.046 - j 3.913 = 6.385 \angle -37.8^\circ \text{ A}$$

$$V_1 = 2400 \angle 0^\circ + (6.385 \angle -37.8^\circ) * (6 + j 8.5) = 2463.6 \angle 0.45^\circ \text{ V}$$

**OR considering the excitation branch between the primary voltage and  $Z_{eq}$**

$$V_1 = 2400 \angle 0^\circ + (6.25 \angle -36.9^\circ) * (6 + j 8.5) = 2462 \angle 0.47^\circ \text{ V}$$

$$\text{b) Load Energy} = (12) * (240) * (62.5) * (0.8) + (12) * (240) * (0.75 * 62.5) * (0.8)$$

$$= 144 + 108 = 252 \text{ kWh}$$