

King Fahd University of Petroleum and Minerals
Department of Electrical Engineering

EE570 Stochastic Processes

Major Examination #1

Time allowed: 75 minutes

Date: November 12, 2007

Student Name:

Student Number:

Part I - Short Questions (18 Marks)

Question 1

List at least three properties of a distribution function.

- 1.
- 2.
- 3.
- 4.
- 5.

Question 2

A_1, A_2, \dots, A_n is an infinite sequence of sets in F . What conditions should be attached to it so that it is declared a Borel set?

Question 3

Given that an arbitrary random variable, x has a continuous distribution, what is the probability of an event $x = b$?

Question 4

The probability of a bit error in a communications line is 10^{-4} . Find the probability that a block of 10000 bits has a maximum of three errors.

Question 5

Moment generating function can be found for

1. Continuous random variable ranging from $-\infty$ to ∞ .
2. Continuous random variable ranging from 0 to ∞
3. Discrete random variable with possible values ranging from $-\infty$ to ∞
4. Discrete random variable with possible values ranging from 0 to ∞

Question 6

Given that $F_{xy}(x,y)$ is a continuous function whose joint *pdf* is defined as

$$f_{xy}(x, y) = \frac{\partial^2}{\partial x \partial y} F_{xy}(x, y)$$

What inference would you draw about the nature of $f_{xy}(x,y)$ if interchanging the order of differentiation does not result in identical answers?

Part II Long Questions (32 Marks)

Question 1

Probabilities to the regions of a triangle as follows:

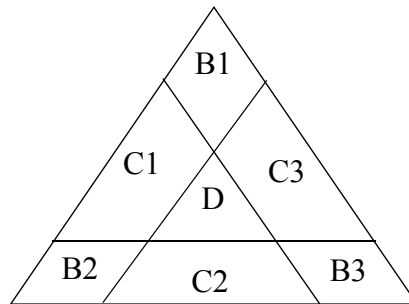


Figure 1 Assignment of probabilities

$$\begin{aligned} Pr[B1] &= Pr[B2] = Pr[B3] = 0.09 \\ Pr[C1] &= Pr[C2] = Pr[C3] = 0.12 \\ Pr[D] &= 0.37 \end{aligned} \tag{1}$$

These probabilities sum to unity. Now define events $F=B1+C1+B2$, $G=B2+C2+B3$, and $H=B3+C3+B1$.

(a) Find probabilities $Pr[F]$, $Pr[G]$, and $Pr[H]$.

- (b) Are events F , G , and H pairwise independent?
- (c) What is the probability of $F \cap G \cap H$?
- (d) Are events F , G , and H independent?

Question 2

Only 1% of all produced components of a certain kind fulfill the exacting requirements for a high precision component. How many components must be ordered to obtain at least one component of the required quality with a probability of at least 95%?

Question 3

Find the distribution function and its complement of the random variable x if the distribution of the latter is (a) normal, (b) uniform. (c) Rayleigh

$$\underbrace{\frac{1}{2\pi\sigma^2} \exp\left(-\frac{(x-a)^2}{2\sigma^2}\right)}_{\text{Normal}}$$

$$\underbrace{\begin{cases} \frac{1}{b-a} & a \leq x \leq b \\ 0 & \text{otherwise} \end{cases}}_{\text{Uniform}}$$

$$\underbrace{\frac{2x}{\alpha} \exp\left(-\frac{x^2}{2\sigma^2}\right)}_{\text{Rayleigh}}$$

Question 4

A normally distributed noise voltage V is applied to the terminals of a resistor R . Find the distribution of the noise power.

