

Fig. 1 Braking resistor, reactor/capacitor location for a generator.

The swing equation for the reference (r-th) machine is

$$M_r p^2 \delta_r + D_r p \delta_r = P_{mr} - P_{er}(t) - P_{br}(t) \quad (2)$$

Dividing the right hand sides of equations (1) and (2) by the respective inertia constants and subtracting one from the other, we get

$$p^2 \delta_{ir} = \frac{1}{M_i} [P_{mi} - P_{ei}(t)] - \frac{1}{M_r} [P_{mr} - P_{er}(t)] - \frac{1}{M_i} P_{bi}(t) + \frac{1}{M_r} P_{br}(t) \quad (3)$$

Here  $\delta_{ir} = \delta_i - \delta_r$ . Damping terms are neglected. The equation is rewritten as

$$p^2 \delta_{ir} = L_{ir}(t) - L_r(t) + b_i u_i(t) + b_r u_r(t) = L_{ir}(t) + b^T u(t) \quad (4)$$

where,  $L_{ir}(t) = L_i(t) - L_r(t)$

$$b_i = -\frac{1}{M_i}, \quad b_r = \frac{1}{M_r}$$

$$P_{bi}(t) = u_i(t), \quad P_{br}(t) = u_r(t)$$

Since the power absorbed by the brakes have an upper limit (say 1 p.u.), the constraint on the control can be written as

$$0 \leq u_i(t) \leq 1 \quad i = 1, 2, \dots, n \quad (5)$$

The control problem for transient stability can be formulated as: Given the system of equation (4), find control  $u(t)$  subject to constraint (5) on all its elements, so that following a disturbance the steady state value of  $\delta_{ir}$  and its derivative  $\dot{\delta}_{ir}$  respectively are brought to

$$0 \leq \delta_{ir}(t_f) \leq \pi/2 \quad (6)$$

$$\dot{\delta}_{ir}(t_f) = 0$$

in the fastest possible time, or minimizing the cost index

$$J = \int_{t_0}^{t_f} dt \quad (7)$$

The cost index  $J$  in this problem is simply  $t_f - t_0$ . Minimization of  $J$  implies reaching the targetted stable condition in minimum time.

Extending the analysis presented in reference [8], the quasi-optimal braking control strategy can be written as

$$u_i^*(t) = \begin{cases} 1 & \text{(resistor on) if } \Sigma_b > 0 \\ 0 & \text{(reactor/capacitor on) if } \Sigma_b < 0 \end{cases} \quad (8)$$

where,

$$\Sigma_b = Y_1 U Y_2 U Y_3$$

$$Y_1: \delta_{ir} - \frac{\dot{\delta}_{ir}^2}{2[L_{ir} - \sum_{i,r} b_k \text{sgn}(\dot{\delta}_{ir})]} = 0, \quad \dot{\delta}_{ir} > 0$$

$$Y_2: 0 \leq \delta_{ir} \leq \pi/2, \quad \dot{\delta}_{ir} = 0 \quad (9)$$

$$Y_3: \delta_{ir} - \frac{\dot{\delta}_{ir}^2}{2[L_{ir} - \sum_{i,r} b_k \text{sgn}(\dot{\delta}_{ir})]} - \pi/2 = 0, \quad \dot{\delta}_{ir} < 0$$

If the reference machine is very large compared to the other machines, the part of  $L_{ir}$  due to the reference machine in equation (4) will be negligible. In the absence of a brake facility on the reference machine, algorithm (8) and (9) will give the control entirely in terms of variables local to each machine.

### The Excitation Control Strategy

The synchronous generator swing equation given in equation (1) can be rewritten as

$$M p^2 \delta = P_m - (v_d i_d + v_q i_q) \quad (10)$$

The subscript  $i$  has been dropped for simplicity. The bracketted quantity is the output power of the machine. Subscripts  $d$  and  $q$  refer to direct and quadrature axes quantities;  $i$  and  $v$  are currents and voltages respectively.

Differentiate both sides of equation (10) with respect to time to get

$$M p^3 \delta = -v_d p i_d - v_q p i_q - i_d p v_d - i_q p v_q \quad (11)$$

Here,  $\dot{P}_m = 0$  since no governor action is considered. From basic machine equations we have [15]

$$v_d = x_q' i_q + e_d' \quad (12)$$

$$v_q = -x_d' i_d + e_q' \quad (13)$$

$$p e_q' = (E_{fd} - e_q') / T_{do}' \quad (14)$$

$$p e_d' = -e_d' / T_{qo}' \quad (15)$$

In the above, ' represents the transient quantities,  $T_{do}'$  and  $T_{qo}'$  are the open circuit field time constants. Using the fact that

$$p e_q' = x_d' p i_d \quad (16)$$

$$p e_d' = x_q' p i_q \quad (17)$$

and substituting (12) - (17) in (11) and after some algebraic manipulations we can write

$$p^3 \delta = L_e(t) + b_e(t) u(t) \quad (18)$$

where

$$L_e(t) = \frac{v_d' e_q'}{M x_d' T_{do}'} + \frac{v_q' e_d'}{M x_q' T_{qo}'} + \frac{2 i_d' e_d'}{M T_{qo}'}$$

$$b_e(t) = -v_d' / M x_d' T_{do}'$$

$$u(t) = E_{fd}$$

The control  $u(t)$  is limited by the excitation ceilings given as  $|u(t)| \leq k$  (19)

Introducing the subscripts  $i$  and  $r$  for the  $i$ -th and  $r$ -th (reference) machines and writing equations similar to (17) for each, we can get

$$p^3 \delta_{ir} = L_{ir}(t) + b(t) u(t) \quad (20)$$

where  $L_{ir} = L_{ei}(t) - L_{er}(t)$

$$b(t) = [b_{ei}(t) \quad b_{er}(t)]^T$$

$$u(t) = [u_i(t) \quad u_r(t)]^T$$

The time optimal control for system (20) subject to constraint (19) on each control can be expressed as follows [15]:

$$\begin{aligned} u_i^*(t) &= -k & \text{if } \Sigma_1 > 0 \\ u_i^*(t) &= k & \text{if } \Sigma_2 < 0 \\ u_i^*(t) &= k \operatorname{sgn} \Sigma_e, & \text{otherwise} \end{aligned} \quad (21)$$

where,

$$\begin{aligned} \Sigma_1 &= \delta_{ir} - \delta_{ir} \cdot \dot{\delta}_{ir} + \frac{1}{2} (\dot{\delta}_{ir})^2 - \pi/2 \\ \Sigma_2 &= \Sigma_1 + \pi/2 \\ \alpha &= \begin{cases} u_i \max & \text{if } \dot{\delta}_{ir} > 0 \\ u_i \min & \text{if } \dot{\delta}_{ir} < 0 \end{cases} \end{aligned} \quad (22)$$

$$\Sigma_e = \delta_{ir} - \frac{(\dot{\delta}_{ir})^2}{2 [L_{ir} - \sum_{i,r} b_{i,r} \operatorname{sgn} \{ \dot{\delta}_{ir} \} ]}$$

$b_{ei}$  and  $b_{er}$  are considered to be negative in strategies (21) and (22).

Finally, the additional stabilizing signal  $u_s(t)$  in the voltage regulator-exciter loop is expressed as

$$u_s(t) = k_e \Upsilon \quad (23)$$

where  $\Upsilon$  is  $\Sigma_1$ ,  $\Sigma_2$  or  $\Sigma_e$  as the case may be.  $k_e$  is selected by trial and error so that the exciter is driven to the ceilings in a bang bang manner when the disturbance is large.

If each machine in the system is assumed to be controlled ( $0 \leq \delta(t_p) \leq \pi/2$ ) it is possible to simplify the entire control strategy and the stabilizing control in such a case can be expressed simply as

$$u_s(t) = k_e \Sigma_e \quad (24)$$

where  $\Sigma_e$  is given in equation (22). Again, if the reference machine is large and there is no excitation controller on it, equation (24) gives a strategy which depends on local variables only.

### SIMULATION STUDIES

The proposed control strategies were tested on a 4 machine power system shown in Figure 2. System data are given in reference [7].

Symmetrical 3- $\phi$  faults were simulated on buses 2, 3 and 4. Generator #1 was considered to be the reference machine. Results of fault studies on bus #3 are presented in the following. Machine #3 is the most severely disturbed generator and the responses of this machine with various control strategies are given.

Each machine in the system is simulated through a fourth order model -- the electromechanical equation and

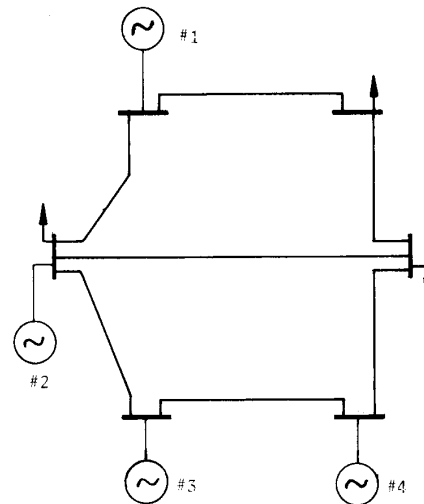


Fig. 2 Power system configuration

the d-q axes flux decay equations. The excitation system of each generator is represented by a fourth order model. The dynamic equations are converted to algebraic ones and solved through an iterative trapezoidal integration technique. Intermediate load flow calculations are done through a fast decoupled technique.

Three dynamic braking configurations with and without excitation controls are studied. These are

- o Only resistor brake
- o Resistor and reactor
- o Resistor and capacitor

In the first strategy, the resistor should be switched in when  $\Sigma_b > 0$ . There is no control action when  $\Sigma_b < 0$ . In the second and third, reactor and capacitor will be switched in respectively when  $\Sigma_b < 0$ . No two controls will be switched in simultaneously. The brake will be discontinued when the switching function  $\Sigma_b$  is within a deadband. This deadband also applies in respect of switching of resistor, reactor or capacitor. A value of 0.008 for the deadband has been arrived at by trial and error such that a stable response is obtained without much of unnecessary switchings. The value of conductance and susceptances of the brake elements were assumed to be 1 and 10 p.u. respectively as in reference [7].

Generator #1 in Fig. 2 is extremely large. This study considers that it is not equipped with any brakes. This makes the braking strategy given by equations (8) and (9) a function of only quantities local to individual generators. It is also assumed that generator #1 has no additional excitation controller. Since the application of resistor and reactor/capacitor brake will control the initial larger swings, the restriction on rotor angle swings in excitation strategy is not required. The excitation control then can be obtained from equation (24) which is a simpler version of the one given in (21).

### Resistor Brake and Excitation Control

The rotor angle variations of machine #3 is given in Fig. 3 following a fault at the terminal of the machine. Curve a is with no control. The uncontrolled system is unstable. Curves b and c are with only braking resistor, and braking resistor plus excitation control respectively. Only braking resistor (no reactor, capacitor) captures the first swing instability, but the system falls into sustained oscillatory mode. The excitation control provides a smooth transition to normal operating condition as shown by curve c.

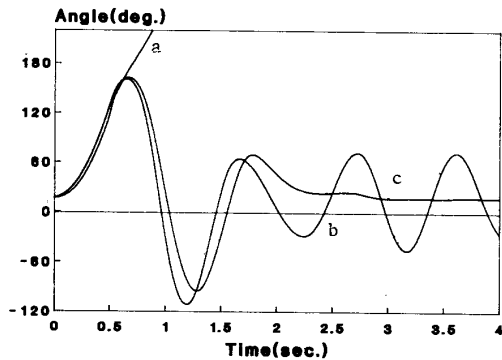


Fig. 3 Angle-time characteristics of machine #3 following a 3- $\phi$  fault on bus # 3 cleared after 0.52 sec., with (a) no control (b) with resistor brake only, and (c) with resistor brake and excitation control.

With the selected deadband of 0.008 on the switching function  $\Sigma_b$ , the optimal switching strategy given by equations (8) and (9) switches the resistor twice into the system. Out of these two switchings, the first one is for a relatively longer duration (about 1/2 sec). Figure 4 shows the angle variation of machine #3 if the brake is switched in only the first time. The system is first swing stable but extremely oscillatory (curve b). The excitation control though does not seem to be very effective in the first cycle of the transient, provides sufficient damping to eliminate all the oscillations in about 3.5 secs. This demonstrates that some of the switchings can be eliminated with a properly coordinated excitation strategy. Note that one switching of resistor can be simulated approximately by relaxing the deadband on  $\Sigma_b$ .

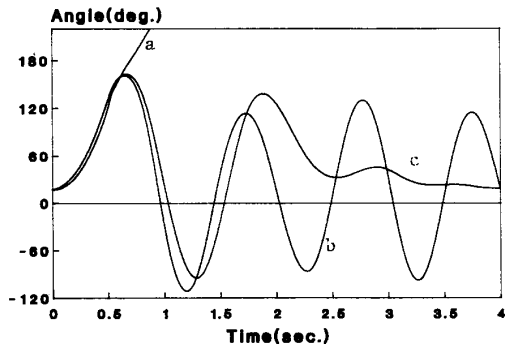


Fig. 4 Angle variations of machine #3 for the fault condition of Fig. 3, with (a) no control (b) braking resistor switched only once, and (c) braking resistor switched once plus excitation control.

#### Resistor-reactor Brake and Excitation Control

When the generator ceases to accelerate, the braking resistor is switched off. The machine is in deceleration mode when  $\Sigma_b < 0$ . Switching in the reactor reduces the terminal voltage of the machine, reducing the output power and thus reducing the deceleration of the machine.

Figure 5 shows the rotor angle variation for the faulted conditions studied when the optimal resistor-reactor switching strategy is used. Curve a is with no control, b with resistor-reactor control, and c with resistor-reactor plus excitation control.

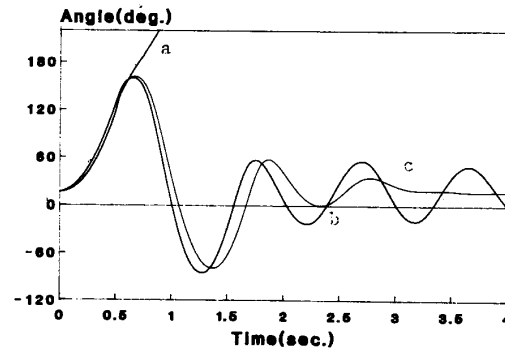


Fig. 5 Angle time characteristics of machine #3 following the fault, with (a) no control, (b) optimum resistor-reactor control, and (c) resistor-reactor and excitation control.

Comparison of curves b in Figures 3 and 5 clearly shows that the resistor-reactor control reduces the electromechanical transients significantly. The excitation control gives a very good transient elimination as depicted in Fig. 5c. Figure 6 shows the variation of frequency of generator #3 corresponding to the case of Fig. 5.

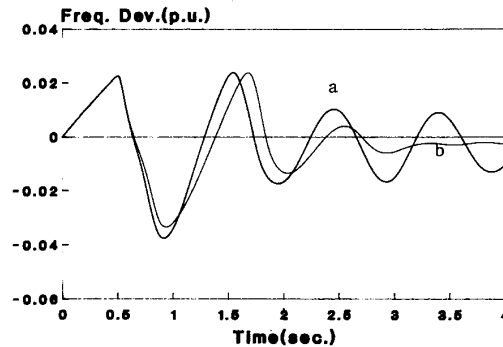


Fig. 6 Frequency variation characteristics corresponding to Fig. 5 with (a) resistor-reactor control, and (b) resistor-reactor and excitation control.

#### Resistor-capacitor Brake and Excitation Control

A very good transient response is obtained when the reactor is replaced by a capacitor in the dynamic braking strategy. Figure 7 gives the responses with resistor-capacitor (curve b) and resistor-capacitor plus excitation control strategies (curve c). Comparison of Fig. 5 (curve b) and Fig. 7 (curve b) shows that the resistor-capacitor strategy controls the transients much better than the resistor-reactor scheme. The first swing deceleration is completely stopped by the resistor-capacitor strategy and subsequent swings are also reduced. The additional excitation control gives a very smooth transition to normal operating condition (curve c). It can be seen that the oscillations are completely eliminated in about 2.5 sec.

Figures 8 and 9 show the terminal voltage and field voltage variations with resistor-capacitor (curve a) and resistor-capacitor plus excitation control (curve b) respectively. The excitation control reduces the sharp variations in terminal voltage of the machine by slowing down the transients. The terminal voltage recovery is achieved by a wider variation of field voltage (Fig. 9b) compared to that without excitation control.

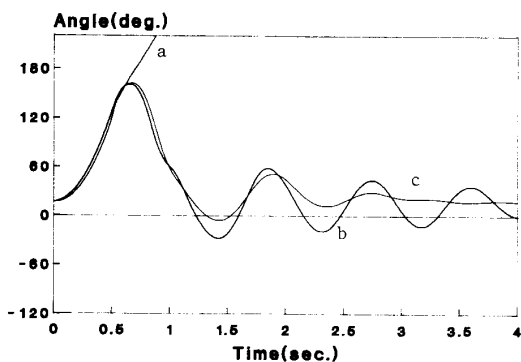


Fig. 7 Angle-time characteristics of machine #3 following a 3- $\phi$  fault, with (a) no control, (b) resistor-capacitor brake, and (c) resistor-capacitor plus excitation control.

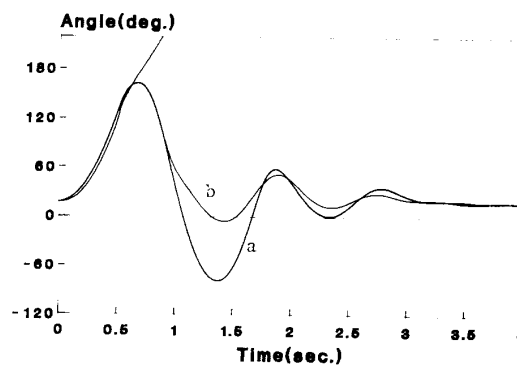


Fig. 10 Angle-time characteristics of machine #3 following a 3- $\phi$  fault on bus #3 cleared after 0.52 sec., with (a) resistor-reactor plus excitation control, (b) resistor-capacitor plus excitation control.

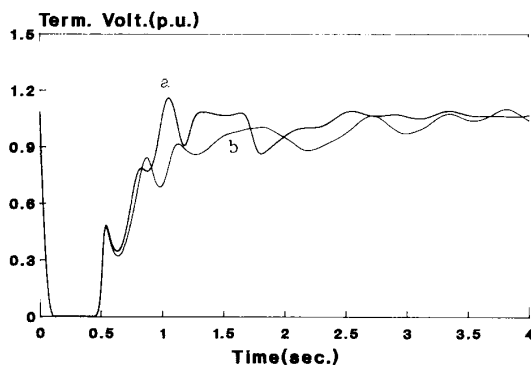


Fig. 8 Terminal voltage of machine #3 corresponding to Fig. 7, with (a) resistor-capacitor brake, (b) excitation control in addition to (a).

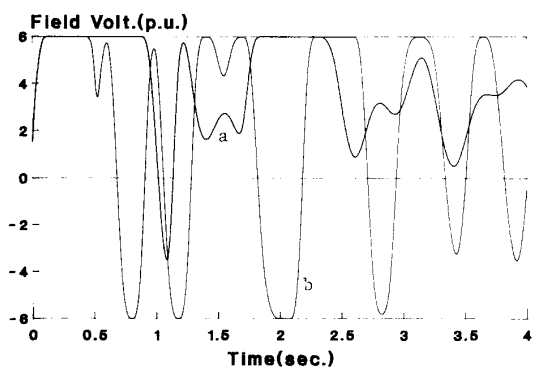


Fig. 9 Field voltage variation of machine #3 corresponding to Fig. 7, with (a) resistor-capacitor control, and (b) resistor-capacitor plus excitation control.

Figure 10 gives a comparison of angle variations with resistor-reactor and resistor-capacitor strategies in the presence of excitation control on both. The co-ordinated resistor-capacitor and excitation control provides a very good transient control as shown by curve b.

Note that all the three generators (#2, #3 and #4) other than reference are assumed to be equipped with excitation controllers. The exciter of generator #3 contributes the most

to the damping of transients for the particular fault, while contributions from those of #2 and #4 are marginal. The combined effect of exciters on #2, #3 and #4 is slightly better than that of #3 alone. This has been observed for almost all the cases studied.

#### CONCLUSIONS

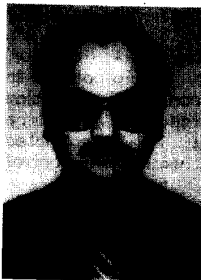
Optimal strategies for controlling first swing instability as well as subsequent oscillations in the system are presented. Three braking strategies - resistor, resistor-reactor and resistor-capacitor, are proposed to enhance transient stability while a nonlinear excitation control removes the oscillations following a large disturbance. It was observed that a co-ordinated resistor-capacitor strategy with the excitation control provides the best response.

All the proposed control strategies are expressed as functions of system states and other measurable quantities. Under certain conditions, the controls can be expressed in terms of variables local to each machine in the system. This makes online implementation of the control strategies easy.

#### REFERENCES

1. W.H. Croft and R.H. Hartley, "Improving Transient Stability by Use of Dynamic Braking", IEEE Trans. on Power App. & Systems, Vol. PAS-59, pp. 17-26, 1962.
2. R.H. Park, "The Design and Use of Braking Resistors", IEEE Proc. Roundup, C12 Reg. 6, pp. 52-61, 1969.
3. M.L. Shelton and P.F. Winkelman, "Bonneville Power Administration 1400-MW Braking Resistors", IEEE Trans. on Power App. and Systems, Vol. PAS 94, pp. 602-611, 1975.
4. H.M. Ellis et al, "Dynamic Stability of Peace River Transmission System", IEEE Trans. on Power App. and Systems, Vol. PAS-85, pp. 586-600, 1966.
5. R.G. Farmer, et al, "Four Corner Project Stability Studies", IEEE Paper 68-CP 708 PWR, 1968.
6. S.S. Joshi and D.G. Tamasker, "Augmentation of Transient Stability Limit of a Power System by Automatic Multiple Application of Dynamic Braking", IEEE Trans. on Power App. and Systems, Vol. PAS-104, No. 11, Nov. 1985.
7. U.O. Aliyu and A.H. El-Abiad, "A Local Control Strategy for Power Systems in Transient Emergency State, Part I: Functional Design", IEEE Trans. on Power App. and Systems, Vol. PAS-101, pp. 4245-4253, 1982.
8. A.H.M.A. Rahim, and D.A.H. Alamgir, "A Closed-loop Quasi-optimal Dynamic Braking Resistor and Shunt

- Reactor Control Strategy for Transient Stability", IEEE Trans. on Power Systems, Vol. 3, pp. 879-886, 1988.
9. A.H.M.A. Rahim and A.I.J. Al-Sammak, "Optimal Switchings of Dynamic Braking Resistor, Reactor or Capacitor for Transient Stability of Power Systems", Accepted for publication in the Proc. IEE, Part C.
  10. F.P. DeMello and C. Concordia, "Concepts of Synchronous Machine Stability as Affected by Excitation Control", IEEE Trans. Power App. and Systems, Vol. PAS-88, pp. 316-329, 1969.
  11. W.A. Mittelstadt, "Four Methods of Power System Damping", IEEE Trans. on Power App. and Systems, Vol. PAS-87, pp. 1323-1329, 1968.
  12. E.V. Lassen and D.A. Swann, "Applying Power System Stabilizers Part I, II and III" IEEE Trans. Power App. and Systems, Vol. PAS-100, pp. 3017-3046, 1981.
  13. R.J. Fleming et al, "Selection of Parameters of Stabilizers in Multimachine Power Systems", IEEE Trans. on Power App. and Systems, Vol. PAS-100, pp. 2329-2333, 1981.
  14. A.H.M.A. Rahim, A.M. Al-Shehri, and D.A.H. Almgir, "Strategies for Controlling Transient as well as Dynamic Instability Problems for Power Systems", Proceedings of the Power System Conference MEPCON 89, Cairo, pp. 286-290, January 1989.
  15. A.H.M.A. Rahim, et al, "A Simple Quasi-optimal Control of Excitation for Stabilization of Multimachine Power System", Electrical Power and Energy Systems, Vol. 3, pp. 208-214, 1981.

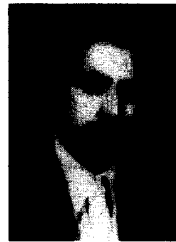


**Abu Hamed M.A. Rahim** (S'69, M'72, SM'83) was born in Comilla, Bangladesh in 1945. He did his B.Sc. in Electrical Engineering from the Bangladesh University of Engineering and Technology (BUET), Dhaka in 1966 and Ph.D. from the University of Alberta, Canada in 1972.

After a brief post doctoral work at the University of Alberta, he rejoined the Faculty in BUET, Dhaka. Dr. Rahim was a Visiting Fellow at the University of Strathclyde, Glasgow (U.K.) in 1978.

He was with the King Fahd University of Petroleum and Minerals, Dhahran, Saudi Arabia during the period 1978-1988. Presently he is working as an Associate Professor in the University of Bahrain. Dr. Rahim's main field of interest are Power System Stability, Control and Optimization.

Dr. Rahim is a Fellow of the Institute of Engineers, Bangladesh and a member of the CIGRE.



**Abdallah Al-Shehri** (S'80 - M'85) was born in Saudi Arabia on June 15, 1953. He received the B.Sc. and M. Sc. in Electrical Engineering from King Fahd University of Petroleum and Minerals, Saudi Arabia and the Ph. D degree in Electrical Engineering from Oregon State University, Corvallis, OR in 1978, 1980 and 1985, respectively.

In 1985 he joined the faculty of King Fahd University of Petroleum

and Minerals and is now an Assistant Professor of Electrical Engineering. His main fields of interest are energy resources, power system planning and control. Dr. Al-Shehri is a member of the IEEE Power Engineering Society and a member of CIGRE.



**A-Imam Al-Sammak** was born in 1956 in Bahrain. He obtained his B.S in Electrical Engineering since 1977 from University of Riyadh, Saudi Arabia. He received his M.S in Electronics from University of Kent, U.K. and his Ph.D. in Electrical Engineering from University of Manchester, U.K. in 1980 and 1986 respectively. He joined University of Bahrain as a lecturer in 1977 where he is now an Assistant Professor in the Department of Electrical Engineering and Computer Science. His research interests include

computer simulations, communications and control.

Dr. Al-Sammak is a member of ACM, IEE and Bahrain Society of Engineers.