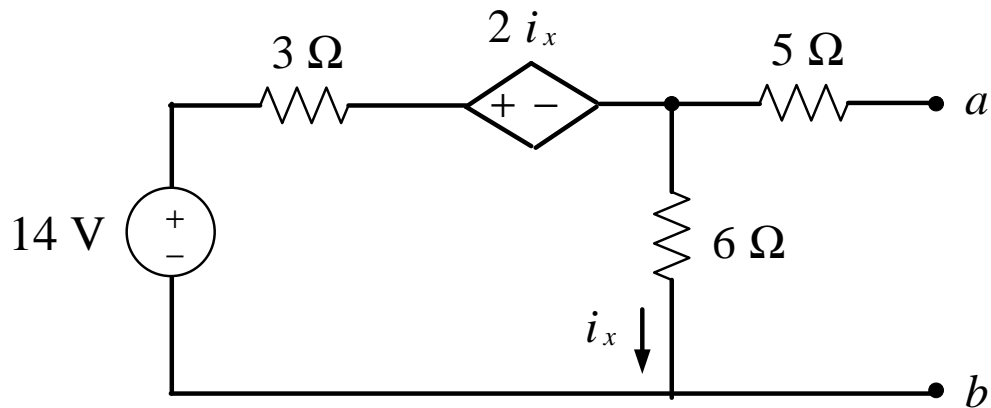


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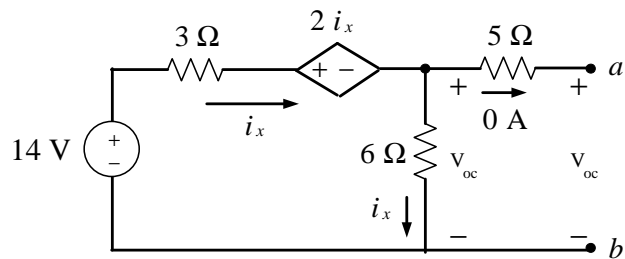
For the circuit shown above find

- (a) The **open circuit voltage** V_{oc} between **a** and **b** directly
(Do not find short circuit current)
- (b) The R_{th} using a test voltage method ?

(a) KVL : $-14 + 3i_x + 2i_x + 6i_x = 0$

$$\Rightarrow i_x = \frac{14}{11} \text{ A}$$

$$\Rightarrow V_{oc} = 6i_x = \frac{84}{11} = 7.6363 \text{ V}$$



(b) KCL $\Rightarrow i = I_T - i_x$

KVL on the inner loop1:

$$-V_T + 5I_T + 6i_x = 0$$

$$\Rightarrow V_T = 5I_T + 6i_x \quad (1)$$

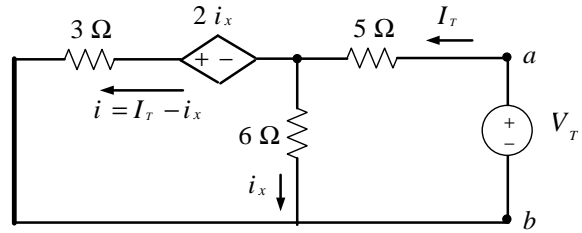
KVL on the inner loop2:

$$-2i_x + 3(I_T - i_x) - 6i_x = 0$$

$$\Rightarrow i_x = \frac{3I_T}{11} \quad (2)$$

$$\Rightarrow \text{From (1) and (2)} \Rightarrow V_T = 5I_T + 6\left(\frac{3I_T}{11}\right)$$

$$\Rightarrow R_{Th} = \frac{V_T}{I_T} = \frac{73}{11} \Omega$$



Extra : Finding Isc (Not included in the grading)

KCL $\Rightarrow i = i_x + I_{sc}$

KVL : KVL on the inner loop

$$-14 + 3(i_x + I_{sc}) + 2i_x + 5I_{sc} = 0$$

$$\Rightarrow 5i_x + 8I_{sc} = 14 \quad (1)$$

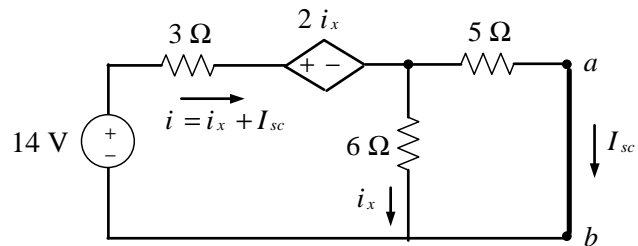
KVL on the inner loop

$$-14 + 3(i_x + I_{sc}) + 2i_x + 6i_x = 0$$

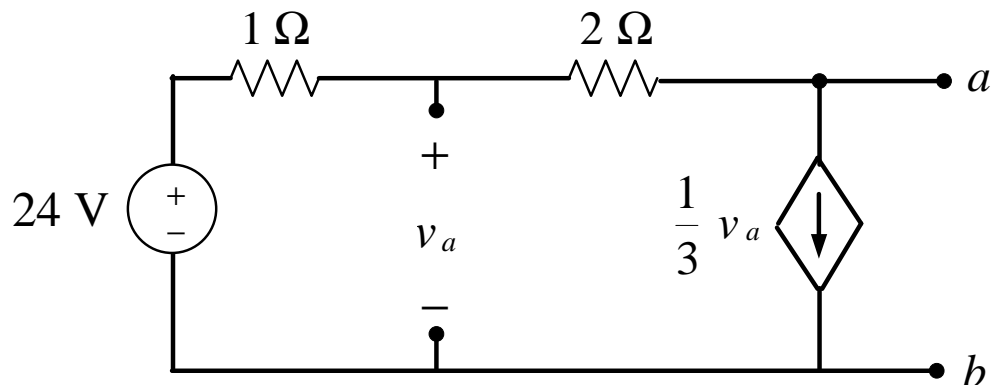
$$\Rightarrow 11i_x + 3I_{sc} = 14 \quad (2)$$

\Rightarrow From (1) and (2)

$$\Rightarrow I_{sc} = \frac{84}{73} = 1.1507 \text{ A}$$



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For the circuit shown above find

(a) The **short circuit current** I_{SC} between a and b directly
(**Do not find open circuit voltage**)

(b) The R_{th} using a test voltage method ?

(a) KCL $\Rightarrow i = \frac{1}{3} v_a + I_{sc}$

KVL on the outer loop:

$$-24 + (1+2) \left(\frac{1}{3} v_a + I_{sc} \right) = 0$$

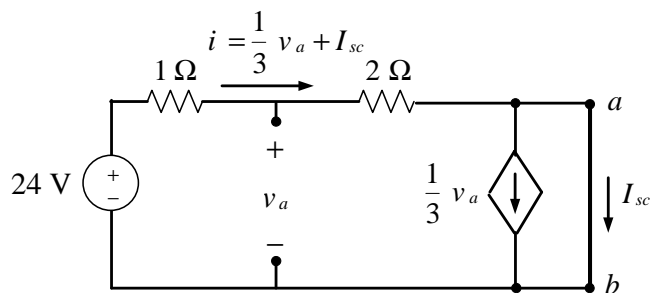
$$\Rightarrow I_{sc} + \frac{1}{3} v_a = 8 \quad (1)$$

KVL on the inner loop:

$$-24 + (1) \left(\frac{1}{3} v_a + I_{sc} \right) + v_a = 0$$

$$\Rightarrow \frac{3}{4} I_{sc} + v_a = 18 \quad (2)$$

solving (1) and (2) $\Rightarrow I_{sc} = \frac{8}{3} = 2.6667 \text{ A}$



$$(b) \text{ KCL} \Rightarrow I_r = \frac{1}{3} v_a + i \quad \mathbf{(1)}$$

KVL on the outer loop:

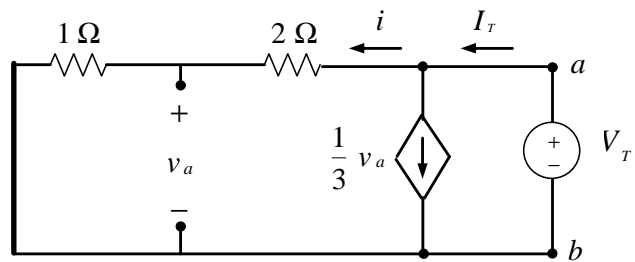
$$-V_r + (2+1)i = 0 \Rightarrow i = \frac{V_r}{3}$$

KVL on the inner loop:

$$-v_a + (1)i = 0 \Rightarrow v_a = i = \frac{V_r}{3}$$

$$\text{From (1)} \Rightarrow I_r = \frac{V_r/3}{3} + \frac{V_r}{3}$$

$$\Rightarrow R_{th} = \frac{V_r}{I_r} = \frac{9}{4} \Omega$$



Extra : Finding Voc (Not included in the grading)

$$\text{KCL} \Rightarrow i = \frac{1}{3} v_a$$

KVL on the outer loop:

$$-24 + (1+2)\left(\frac{1}{3} v_a\right) + V_{oc} = 0$$

$$\Rightarrow v_a + V_{oc} = 24 \quad \mathbf{(1)}$$

KVL on the inner loop:

$$-24 + (1)\left(\frac{1}{3} v_a\right) + v_a = 0 \Rightarrow v_a = 18 \text{ V}$$

$$\text{From (1)} \Rightarrow V_{oc} = 24 - v_a = 24 - 18 = 6 \text{ V}$$

