Parallel Tabu Search for Optimizing the OSPF Weight Setting Problem

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Abstract: The problem of setting the Open Shortest Path First (OSPF) weights on links such that congestion can be avoided is proved to be NP-hard. Many iterative heuristics have been applied to solve the OSPF weight setting (OSPFWS) problem. As the size of any combinatorial optimization problem increases, it becomes more difficult to find an optimum solution using sequential algorithms. Parallelization of modern iterative heuristics has been proven to produce improved solution precision and timing. In this paper, we investigate the parallelization of Tabu Search and apply two variants of a Parallel Tabu Search (PTS) heuristic on the OSPFWS problem. It is shown through experimental results that both PTS approaches produced better solutions quality compared to the sequential heuristics; specifically for larger topologies. In one approach, we propose a new design for our parallel cooperative search algorithm, which performs better than the conventional parallel heuristic. The purpose of this new design is to induce diversification into the search to explore a larger search space. We also show that the new approach performs better than the conventional parallel heuristic.

Key–Words: Open Shortest Path First (OSPF), OSPF Weight Setting Problem, NP-hard, Iterative Heuristics, Parallel Tabu Search.

1 Introduction

Open Shortest Path First (OSPF) is an intra autonomous system routing protocol which computes the shortest paths based on the weights assigned to the links. Routing on the Internet defines the traffic flows over the selected shortest paths. Traffic engineering aims at providing the required Quality of Service (QoS) to the users by efficiently utilizing the available resources and managing these traffic flows. The rapid growth in Internet traffic underlines the importance of traffic engineering.

OSPF uses the link weights as its routing metric. The major networking vendor Cisco, assigns the link weights inversely proportional to the link capacity. This is termed as inverse capacity OSPF in the literature [1, 2]. Other methods of weight assignment such as unit OSPF and random OSPF also exist. Given a set of traffic demands between each source and destination node, the OSPF weight setting problem consists of determining suitable OSPF link weights so as to optimize a certain criterion (cost function), aiming at avoiding congestion in the network. This Problem is NP-hard [1].

The application of iterative heuristics to solve the OSPFWS problem was first attempted by Fortz and Thoroup [3, 4]. They applied tabu search using their proposed cost function [1]. We call this cost function FortzCF. Sqalli et al. proposed a new cost function (NewCF) and applied Simulated Annealing [5], Simulated Evolution [6], and Tabu Search [7] using both cost functions. They proved experimentally that the new cost function minimizes the number of congested links. Ericsson et al. attempted Genetic Algorithm [2] as well as hybrid GA [8] for the same problem.

Tabu Search has also been used for many other optimization problems such as power system restoration [9] and job shop scheduling problems [10]. In addition, Balicki [11] used an evolutionary algorithm based on a tabu search procedure for multi-criteria optimization of distributed systems. Sadegheih [12] also discusses a global optimisation using evolutionary algorithms, simulated annealing, and tabu search. Adaptive Tabu Search (ATS) has been used as well in the works of Sujitjorn et al.[13] and Kluabwang et al. [14].

In this paper, we investigate parallelizing the Tabu Search iterative heuristic to solve the OSPFWS problem which, to our knowledge, has not been attempted yet. Enormous work has been done in the area of parallelization of iterative heuristics in general and Parallel Tabu Search (PTS) [15, 16, 17, 18] in particular to
solve a range of combinatorial optimization problems. Different implementation strategies are also proposed in the literature which include, using dynamic Tabu Search parameters [19] at different processors, using a cluster in some hierarchical architecture [20, 21] to enhance the search, integration of different parallelization strategies [20], etc. A detailed survey of various parallelization strategies and their application to one or more classical or specific optimization problems can also be found in the literature [22, 23, 24].

The OSPFWS problem, like any other combinatorial optimization problem, requires high computing which grows exponentially with the problem dimension [25]. Parallelism has obvious advantages due to the availability of more resources at hand. If efficiently done, it not only achieves good results in relatively lesser time compared to its sequential counterparts, but also can obtain superior solution quality due to more comprehensive and independent parallel search by multiple entities. In this paper, we present a Parallelized Tabu Search (PTS) [26] heuristic using two strategies to solve the OSPFWS problem by using the two cost functions available in the literature. The objective is to achieve better solutions quality in a given time, which could not be achieved by sequential heuristics; specifically for larger topologies and higher traffic demands.

The rest of the paper is organized as follows; The OSPFWS problem statement and the cost functions proposed in the literature are presented in Section 2. The two Parallel Tabu Search algorithms are discussed in Section 3. This is followed by the experimental results and conclusion.

2 Problem Statement

The OSPF weight setting problem can be stated as follows: Given a directed network of nodes and arcs $G = (N, A)$, a demand matrix $D$, and capacity $C_a$ for each arc $a \in A$, determine a positive integer weight $w_a \in [1, w_{max}]$ for each arc $a \in A$ such that the objective function or cost function $\Phi$ is minimized. When routing is performed using OSPF, the assigned link weights completely determine the shortest paths, and hence the traffic flows. Based on these traffic flows, the partial loads on each arc for a given destination are computed. This is done for all destination nodes. The aggregated partial loads for all destinations on a particular arc give the total load $l_a$ on that arc. The cost of sending traffic through this arc is given by $\Phi_a(l_a)$. The cost value depends on the utilization of the arc and is given by the linear function proposed by Fortz and Thorup [1].

$$\Phi_a(l) = \begin{cases} 
1 & \text{for } 0 \leq l/c_a < 1/3, \\
3 & \text{for } 1/3 \leq l/c_a < 2/3, \\
10 & \text{for } 2/3 \leq l/c_a < 9/10, \\
70 & \text{for } 9/10 \leq l/c_a < 1, \\
500 & \text{for } 1 \leq l/c_a < 11/10, \\
5000 & \text{for } 11/10 \leq l/c_a < \infty
\end{cases}$$

(1)

The Fortz cost function is given in equation 2.

$$\Phi = \sum_{a \in A} \Phi_a(l_a)$$

(2)

The objective is to minimize $\Phi$, subject to these constraints:

$$l_a = \sum_{(s,t) \in N \times N} f_a^{(s,t)} a \in A, \quad (3)$$

$$f_a^{(s,t)} \geq 0 \quad (4)$$

In constraint 3, for traffic between a source and a destination pair $(s,t)$, $f_a^{(s,t)}$ indicates the amount of traffic flow that goes over arc $a$. The detailed steps showing the formulation of this cost function can be found in the literature [1, 5].

The New cost function [5] is shown in equation 5,

$$\Phi = MU + \frac{\sum_{a \in \text{SetCA}} (l_a - c_a)}{E}$$

(5)

This function contains two terms. The first term is the maximum utilization (MU) in the network. The second term represents the extra load on the network divided by the number of edges present in the network to normalize the entire cost function.

We have applied our proposed parallel heuristics on both cost functions presented in this section.

3 Parallel Tabu Search (PTS)

In conventional parallel implementations of tabu search, all the processors including the master independently generate an initial solution and compute its cost. After searching its part of the current neighborhood, repeatedly for a certain number of iterations, each slave process reports its best move back to the
master. The master process selects the best among the received best moves (subject to tabu conditions). If the stopping criteria are met then the search stops; otherwise the master broadcasts the selected move back to the slaves. The selection criterion for the best move and also the slaves to which this best move is broadcasted, depend on the implementation strategy. The search continues, where each processor sets the received solution from the master as its current solution and explores the neighborhood. The master also broadcasts the tabu list pertaining to the selected solution and all slaves update their individual tabu lists.

Two strategies, namely, PTS-Star and PTS-Ring were implemented to parallelize Tabu Search. The implementation aspects of the two strategies mainly differ in the way the processors coordinate during the periodic solution exchanges. From the functional aspect, they differ in the search space each processor works on after each solution exchange. In this section, we discuss the two strategies in detail.

3.1 PTS-Star

In the PTS-Star strategy, the parallel cluster consists of \( n + 1 \) processors with 1 master and \( n \) slave processors/nodes. Each processor starts by generating a random initial solution. Due to the independent random number generation by each entity the initial solution generated by a processor is different from the other. Each slave processor starts Tabu Search and continues for \( K \) iterations. After each move the current and best cost are computed. At the end of the \( K^{th} \) iteration, the best cost and solution are sent to the master. The master waits to receive the cost and solution from all slaves, after which it compares the received costs and picks the best cost among the \( n \) slaves. Once the comparison is done and the best cost is selected, the master broadcasts the corresponding best solution to all slaves. Each slave processor receives the new best solution from the master and sets this received solution as the current solution. With this current solution, Tabu Search is started for another \( K \) iterations.

This process of parallel Tabu Searches with processor coordination by periodic solution exchange continues until the termination criterion is met. The master is the central point of coordination between all slaves, which means that all communications go through the master and each processor is directly connected only to the master. The processor arrangement resembles a star topology and hence the name PTS-Star. The structure of the PTS-Star algorithm is shown in Figure 1.

With multiple processors working on the solution and exploring the search space, the convergence is expected to be faster and the final solution quality is also expected to be better by visiting more points (solutions) in the search space.

This technique however has the limitation that, after every periodic solution exchange, all processors start Tabu Search with the same current solution, and hence searching in similar regions of the search space. To prevent this redundant search, some technique is required where different processors can coordinate to explore a larger search space. The next strategy PTS-Ring addresses this issue.

3.2 PTS-Ring

The primary objective of devising this new strategy is to improve the solution quality by making the processors work in different regions of the search space. This is done by making different set of processors start the search from different starting points (solutions) after each solution exchange, thereby diversifying the search considerably. It is practically important to search a new region when the neighborhood search fails to improve the best solution for a while; and diversification techniques can help achieve this goal. In the PTS-Ring strategy, the parallel cluster consists of \( n+1 \) processors with 1 master and \( n \) slaves. Each slave node \( S_i \) has a rank \( i \) associated with it. A node exchanges its solution only with its neighbors. Neighborhood is defined as a set of three nodes with ranks \( i - 1, i, i + 1 \); hence the neighbors of node \( S_i \) are \((S_{i-1}, S_{i+1})\). Further, the neighbors of the last node \( S_n \) are \((S_{n-1}, S_1)\) while the neighbors of the first node

Algorithm: PTS-Star

Begin:

Slave:
1: Generate Initial Solution.
2: Continue TS for \( K \) Iterations.
3: Send the bestsol and bestcost to master.
Master:
4: Receive individual bestcost from each slave.
5: Compare the received costs.
6: Select the bestsol among all slaves.
7: if termination criteria is met: then
   Save the results.
   Stop.
8: else:
   Broadcast bestsol to all slaves.
9: GoTo: 4
Slave:
10: Receive the solution from master.
11: Update current solution based on the received solution.
12: if termination criteria is met: Stop.
13: else: GoTo: 2
End:
The utilization of the link is the ratio of load on the link to its capacity. If the utilization of the link is more than one, the link is congested. The Maximum Utilization is the utilization of the maximum utilized link in the network. In other words, it is the utilization of the link having the highest degree of congestion. The extra load on a particular link is the load present in excess to its capacity. If the load on the link is less than its capacity \((\text{utilization} < 1)\), then the extra load on that link is zero. The percentage of extra load is the sum of the extra load present in the network divided by the sum of capacities of congested links. As explained earlier, congested links are the links which have a utilization greater than 1 (i.e., load on the link exceeds its capacity). The statistics for these performance metrics are plotted with respect to both parallel strategies PTS-Star and PTS-Ring, using the two cost functions: FortzCF and NewCF.

4 Results

In this section, we present the experimental results for the two Parallel Tabu Search algorithms. The test cases and demand matrices are the same as used in the literature [1, 4]. The generation of these test cases is done using GT-ITM generator [27], based on a model of Calvert [28] and Zegura [29].

Experimental results have been recorded for the following four performance metrics:

1. Cost
2. Maximum Utilization (MU)
3. Percentage of Extra Load (PXLoad)
4. Number of Congested Links (NOCL)

4.1 PTS-Star

In this section, we first present the results of the PTS-Star strategy in which we show the Cost comparison versus the number of processors for four test cases. In Figure 3, the results for the maximum demand are shown. It can be seen here that the cost improves with the number of processors for all cases but this improvement for the cases h100N360a and w100N476a is very minimal. The total demand and also the aver-
average load per arc (Total Demand/Number of Links) on these topologies is less when compared to the random graphs (r100N403a, r100N503a). The cost of a solution is dependent on the utilization of the links, and lower input demands lead to lesser utilization. Hence, when the input demands are low, a large set of solutions (weight combinations) will result in links with low utilization and hence, a lower cost. These solution sets representing a good solution, form a slightly bigger fraction of the search space and can also be explored by sequential heuristics. Hence, for topologies with lower input demands, the improvement due to parallelization is not significant when compared to sequential heuristics.

The other two cost curves for r100N403a and r100N503a graphs show a significant improvement in cost with the increase in the number of processors. The same trend is also observed for Demand-11, as can be seen in Figure 4. The random graphs used in this work are the graphs with large sizes and higher demands when compared to any other topology. None of the sequential heuristics mentioned in this paper have achieved results close to PTS for these topologies. The final costs achieved using PTS are even up to one third of the best achieved using the sequential Tabu Search heuristic (TS). TS has also the best results among all sequential heuristics [7].

![Figure 3: Cost vs. # of Processors Using PTS-Star for D12.](image)

![Figure 4: Cost vs. # of Processors Using PTS-Star for D11.](image)

![Figure 5: Time vs. # of Processors Using PTS-Star for D12.](image)

4.2 PTS-Ring

Cost comparison for the above mentioned four topologies is shown here for the PTS-Ring strategy. The results for Demand-12 and Demand-11 are shown in Figure 7 and Figure 8 respectively. It can be seen that, with the increase in the number of processors, the cost improves considerably for the two test cases r100N403a, r100N503a. The PTS-Ring strategy also
could not achieve a linear speedup with the increase in the number of processors, but was again able to achieve costs which are about three times better than the sequential heuristics.

### 4.3 PTS-Star Versus PTS-Ring

Results for the Fortz cost function show that the costs achieved by PTS-Ring are slightly better than PTS-Star for all the test cases and demands. This improvement is expected and can be attributed to the diversification feature of the Ring approach. The slave processors, in PTS-Ring, start from slightly different solutions after every solution exchange; thereby covering a wider search space and achieving better solutions when compared to the ring approach. The cost curves for the FortzCF are shown in Figure 9 and 10 for Demand-12 and Demand-11 respectively.

Figure 11 and 12 shows the cost curves for Demand-12 and Demand-11 respectively using the new cost function (NewCF). The PTS-Ring Strategy, with a better diversification mechanism, again pro-
duced better results than the PTS-Star Strategy for the NewCF which can be seen from these results.

![Cost Comparison - Star vs Ring](image1)

Figure 11: Cost Results of PTS For NewCF for D12.

The comparisons of other performance metrics for both cost functions are shown in the following subsections.

### 4.4 Number of Congested Links

The comparison of the Number of Congested Links (NOCL) for both cost functions for the topology r100N403a is shown in Figure 13. It can be observed that for FortzCF, there is no improvement of the NOCL with the increase in the number of processors. We have seen in previous results that there is a significant improvement in cost with the number of processors. Hence, we can conclude that the improvement in cost is due to reducing the extra load on the network at the expense of the number of congested links. FortzCF attempts to load balance the congestion on the network among all links by reducing the load from the more congested links and placing it on the lesser congested links. However, for the NewCF, there is a minimization in the NOCL. Similar results are displayed in Figure 14 for Demand-11. Among the two strategies, the PTS-Ring minimizes the NOCL better than the PTS-Star for the same cost function, as it also minimizes the overall cost better for both cost functions. The best results for the NOCL were obtained when optimizing weights using the NewCF and the Ring Topology.

![Number of Congested Links](image2)

Figure 13: NOCL Results of PTS Using Both CFs for D12.

![Number of Congested Links](image3)

Figure 14: NOCL Results of PTS Using Both CFs for D11.

### 4.5 Percentage of Extra Load

We now discuss the results for the Percentage of extra load (PXLoad). In the case of Demand-12 as shown in Figure 15, and Demand-11 as shown in Figure 16 the values of PXLoad are better for FortzCF when optimized using the PTS-Ring strategy compared to the NewCF; and PTS-Ring performs better than PTS-Star. Hence, it can be said that when weights are optimized using the FortzCF, the links which are over-utilized are not highly congested; while with the NewCF, a lesser number of links are congested but each individual congested link has a higher load. However, from the results of NOCL and PXLoad, it is important here to note that when weights are optimized using the NewCF and the Ring topology, it is found to produce comparable values of PXLoad and at the same time give better results for the Number of congested links.
Links. Similar results for NOCL and PXLoad were also achieved for the r100N503a topology.

Figure 15: PXLoad Results of PTS Using Both CFs for D12.

Figure 16: PXLoad Results of PTS Using Both CFs for D11.

4.6 Maximum Utilization

The results for the Maximum Utilization (MU) are shown in Figure 17 and Figure 18. From this figure, it can be seen that the Maximum Utilization in the case of FortzCF is better than that of the NewCF.

From the above results it was observed that the PTS-Ring strategy produced better results for both cost functions and the NewCF produced very good results for minimizing the Number of congested links. The percentage of extra load was found to be best (Minimum) using the FortzCF and the Ring topology. However, in many cases, the NewCF also produced values close to the FortzCF. For both topologies, a significant improvement in the performance metrics was observed using parallelization.

As the size of any combinatorial optimization problem increases, not only its search space increases exponentially but also it becomes more complex as the fraction of solutions that are close to the optimal one becomes smaller. Sequential heuristics often fail to explore this small fraction from the huge search space. Having seen the results of sequential heuristics, PTS-Star, and PTS-Ring in terms of speedup and final cost, it is evident that, as the size and routing complexity of the network increases, there is a significant improvement in the solution quality with parallelized heuristics.

5 Conclusion

Two different Parallel Tabu Search iterative heuristics were implemented on several networks using two cost functions. Results for four performance metrics are reported for FortzCF and NewCF. Both PTS heuristics produced the desired results in the case of large topologies in terms of cost. The PTS-Ring strategy which was designed to induce diversification into the search was found to achieve better cost than any other approach including the PTS-Star for the same run time. However, linear speedup could not be achieved in any strategy. Both the strategies produced better results for smaller topologies also, but did not provide a significant improvement in cost as achieved for the larger topologies. Hence, it can be concluded that if
the problem size is large, parallel Tabu Search or any other parallel algorithm can be efficiently applied to the OSPFWS problem to achieve a solution quality which can not be achieved by using sequential algorithms within the same or comparable time frame.

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