

# Digital Systems

COE 202

Digital Logic Design

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# Welcome to COE 202

## ❖ Course Webpage:

<http://faculty.kfupm.edu.sa/coe/mudawar/coe202/>

## ❖ Lecture Slides:

<http://faculty.kfupm.edu.sa/coe/mudawar/coe202/lectures/>

## ❖ Assignments:

<http://faculty.kfupm.edu.sa/coe/mudawar/coe202/assignments.htm>

## ❖ Blackboard:

<https://blackboard.kfupm.edu.sa/>

# Which Book will be Used?

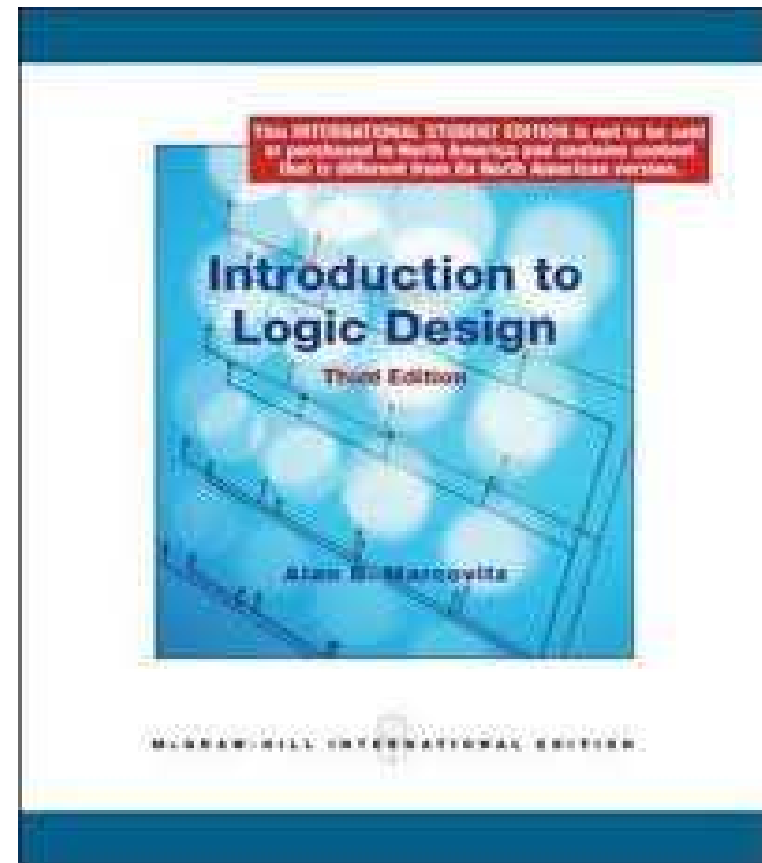
## ❖ Introduction to Logic Design

### ❖ Alan B. Marcovitz

❖ Third Edition

❖ McGraw Hill

❖ 2010



# What you will I Learn in this Course?

- ❖ Towards the end of this course, you should be able to:
  - ✧ Carry out arithmetic computation in various number systems
  - ✧ Apply rules of Boolean algebra to simplify Boolean expressions
  - ✧ Translate truth tables into equivalent Boolean expressions and logic gate implementations and vice versa
  - ✧ Design efficient combinational and sequential logic circuit implementations from functional description of digital systems
  - ✧ Use software tools to simulate and verify the operation of logic circuits

# Is it Worth the Effort?

- ❖ Absolutely!
- ❖ Digital circuits are employed in the design of:
  - ✧ Digital computers
  - ✧ Data communication
  - ✧ Digital phones
  - ✧ Digital cameras
  - ✧ Digital TVs, etc.
- ❖ This course provides the fundamental concepts and the basic tools for the design of digital circuits and systems

# Grading Policy

❖ Assignments & Quizzes	20%
❖ Midterm Exam I	20%
❖ Midterm Exam II	25%
❖ Final Exam	35%

❖ **NO makeup exam** will be given whatsoever

# Presentation Outline

- ❖ Analog versus Digital Systems
- ❖ Digitization of Analog Signals
- ❖ Binary Numbers and Number Systems
- ❖ Number System Conversions
- ❖ Representing Fractions
- ❖ Binary Codes

# Analog versus Digital

- ❖ **Analog** means **continuous**
- ❖ Analog parameters have **continuous range of values**
  - ✧ Example: temperature is an analog parameter
  - ✧ Temperature increases/decreases continuously
  - ✧ Like a continuous mathematical function, No discontinuity points
  - ✧ Other examples?
- ❖ **Digital** means using numerical **digits**
- ❖ Digital parameters have **fixed set of discrete values**
  - ✧ Example: month number  $\in \{1, 2, 3, \dots, 12\}$
  - ✧ Thus, the month number is a digital parameter (cannot be 1.5!)
  - ✧ Other examples?



# Analog versus Digital System

- ❖ Are computers analog or digital systems?

Computer are digital systems

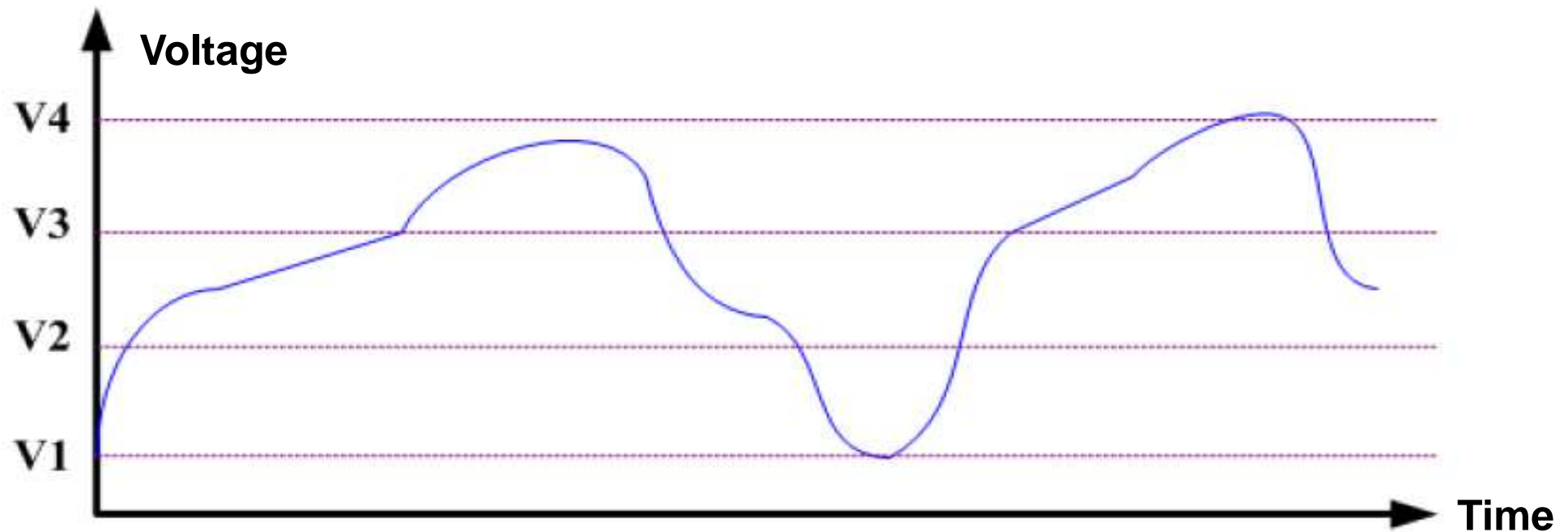
- ❖ Which is easier to design an analog or a digital system?

Digital systems are easier to design, because they deal with a limited set of values rather than an infinitely large range of continuous values

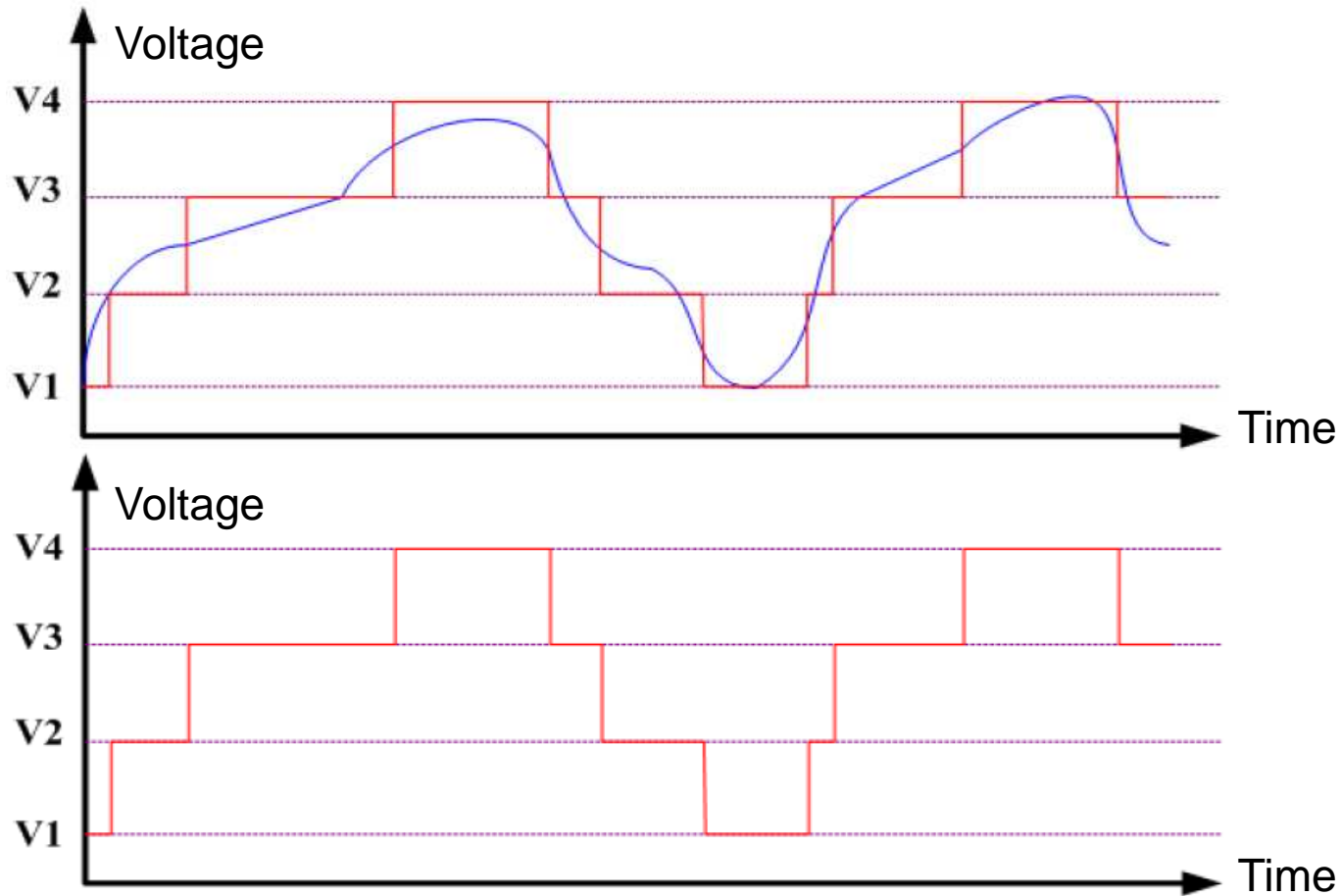
- ❖ The world around us is analog
- ❖ It is common to convert analog parameters into digital form
- ❖ This process is called **digitization**

# Digitization of Analog Signals

- ❖ **Digitization** is converting an analog signal into digital form
- ❖ Example: consider digitizing an analog voltage signal
- ❖ Digitized output is limited to four values =  $\{V1, V2, V3, V4\}$



# Digitization of Analog Signals - cont'd



- ❖ Some loss of accuracy, why?
- ❖ How to improve accuracy?

**Add more voltage values**

# ADC and DAC Converters

## ❖ Analog-to-Digital Converter (ADC)

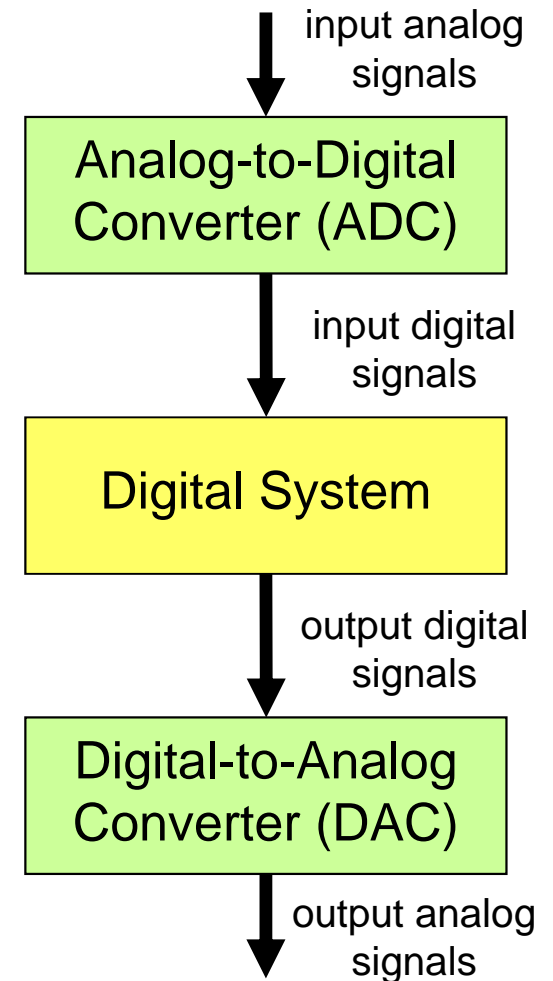
- ❖ Produces digitized version of analog signals
- ❖ Analog input => Digital output

## ❖ Digital-to-Analog Converter (DAC)

- ❖ Regenerate analog signal from digital form
- ❖ Digital input => Analog output

## ❖ Our focus is on digital systems only

- ❖ Both input and output to a digital system are digital signals

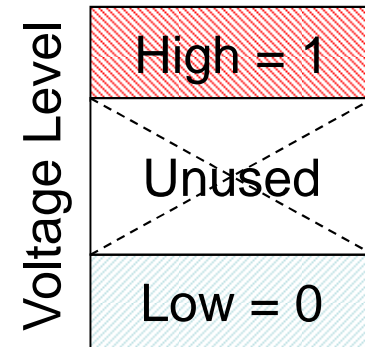


# Next . . .

- ❖ Analog versus Digital Systems
- ❖ Digitization of Analog Signals
- ❖ Binary Numbers and Number Systems
- ❖ Number System Conversions
- ❖ Representing Fractions
- ❖ Binary Codes

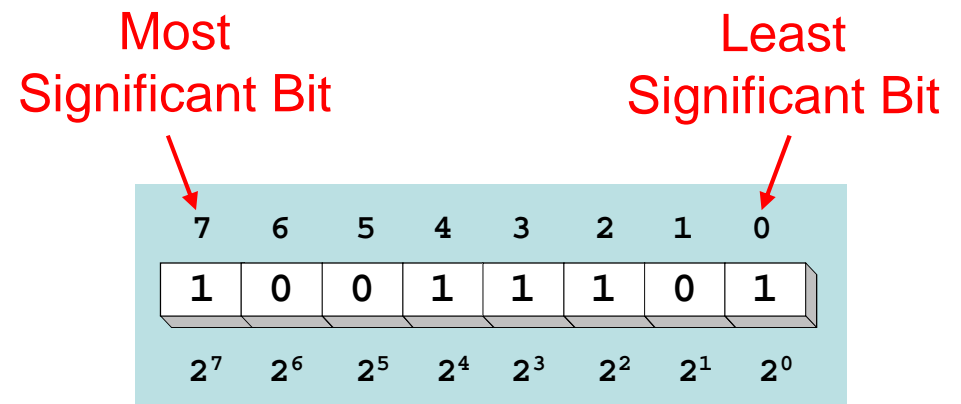
# How do Computers Represent Digits?

- ❖ Binary digits (0 and 1) are the simplest to represent
- ❖ Using electric voltage
  - ✧ Used in processors and digital circuits
  - ✧ High voltage = 1, Low voltage = 0
- ❖ Using electric charge
  - ✧ Used in memory cells
  - ✧ Charged memory cell = 1, discharged memory cell = 0
- ❖ Using magnetic field
  - ✧ Used in magnetic disks, magnetic polarity indicates 1 or 0
- ❖ Using light
  - ✧ Used in optical disks, optical lens can sense the light or not



# Binary Numbers

- ❖ Each binary digit (called a bit) is either 1 or 0
- ❖ Bits have no inherent meaning, they can represent ...
  - ✧ Unsigned and signed integers
  - ✧ Fractions
  - ✧ Characters
  - ✧ Images, sound, etc.



## ❖ Bit Numbering

- ✧ Least significant bit (LSB) is rightmost (bit 0)
- ✧ Most significant bit (MSB) is leftmost (bit 7 in an 8-bit number)

# Decimal Value of Binary Numbers

- ❖ Each bit represents a power of 2
- ❖ Every binary number is a sum of powers of 2
- ❖ Decimal Value =  $(d_{n-1} \times 2^{n-1}) + \dots + (d_1 \times 2^1) + (d_0 \times 2^0)$
- ❖ Binary  $(10011101)_2 = 2^7 + 2^4 + 2^3 + 2^2 + 1 = 157$

7	6	5	4	3	2	1	0
1	0	0	1	1	1	0	1
$2^7$	$2^6$	$2^5$	$2^4$	$2^3$	$2^2$	$2^1$	$2^0$

Some common  
powers of 2



$2^n$	Decimal Value	$2^n$	Decimal Value
$2^0$	1	$2^8$	256
$2^1$	2	$2^9$	512
$2^2$	4	$2^{10}$	1024
$2^3$	8	$2^{11}$	2048
$2^4$	16	$2^{12}$	4096
$2^5$	32	$2^{13}$	8192
$2^6$	64	$2^{14}$	16384
$2^7$	128	$2^{15}$	32768



# Positional Number Systems

## Different Representations of Natural Numbers

XXVII Roman numerals (not positional)

27 Radix-10 or **decimal** number (positional)

$11011_2$  Radix-2 or **binary** number (also positional)

## Fixed-radix positional representation with $n$ digits

Number  $N$  in radix  $r = (d_{n-1}d_{n-2} \dots d_1d_0)_r$

$N_r$  Value =  $d_{n-1} \times r^{n-1} + d_{n-2} \times r^{n-2} + \dots + d_1 \times r + d_0$

Examples:  $(11011)_2 = 1 \times 2^4 + 1 \times 2^3 + 0 \times 2^2 + 1 \times 2 + 1 = 27$

$(2107)_8 = 2 \times 8^3 + 1 \times 8^2 + 0 \times 8 + 7 = 1095$

# Convert Decimal to Binary

- ❖ Repeatedly divide the decimal integer by 2
- ❖ Each remainder is a binary digit in the translated value
- ❖ Example: Convert  $37_{10}$  to Binary

Division	Quotient	Remainder
$37 / 2$	18	1
$18 / 2$	9	0
$9 / 2$	4	1
$4 / 2$	2	0
$2 / 2$	1	0
$1 / 2$	0	1

← least significant bit

$$37 = (100101)_2$$

← most significant bit

← stop when quotient is zero

# Decimal to Binary Conversion

- ❖  $N = (d_{n-1} \times 2^{n-1}) + \dots + (d_1 \times 2^1) + (d_0 \times 2^0)$
- ❖ Dividing  $N$  by 2 we first obtain
  - ✧  $\text{Quotient}_1 = (d_{n-1} \times 2^{n-2}) + \dots + (d_2 \times 2) + d_1$
  - ✧  $\text{Remainder}_1 = d_0$
  - ✧ Therefore, first remainder is least significant bit of binary number
- ❖ Dividing first quotient by 2 we first obtain
  - ✧  $\text{Quotient}_2 = (d_{n-1} \times 2^{n-3}) + \dots + (d_3 \times 2) + d_2$
  - ✧  $\text{Remainder}_2 = d_1$
- ❖ Repeat dividing quotient by 2
  - ✧ Stop when new quotient is equal to zero
  - ✧ Remainders are the bits from least to most significant bit

# Popular Number Systems

- ❖ Binary Number System: Radix = 2
  - ✧ Only two digit values: 0 and 1
  - ✧ Numbers are represented as 0s and 1s
- ❖ Octal Number System: Radix = 8
  - ✧ Eight digit values: 0, 1, 2, ..., 7
- ❖ Decimal Number System: Radix = 10
  - ✧ Ten digit values: 0, 1, 2, ..., 9
- ❖ Hexadecimal Number Systems: Radix = 16
  - ✧ Sixteen digit values: 0, 1, 2, ..., 9, A, B, ..., F
  - ✧ A = 10, B = 11, ..., F = 15
- ❖ Octal and Hexadecimal numbers can be converted easily to Binary and vice versa

# Octal and Hexadecimal Numbers

- ❖ Octal = Radix 8
- ❖ Only eight digits: 0 to 7
- ❖ Digits 8 and 9 not used
- ❖ Hexadecimal = Radix 16
- ❖ 16 digits: 0 to 9, A to F
- ❖ A=10, B=11, ..., F=15
- ❖ First 16 decimal values (0 to 15) and their values in binary, octal and hex.

**Memorize table**

Decimal Radix 10	Binary Radix 2	Octal Radix 8	Hex Radix 16
0	0000	0	0
1	0001	1	1
2	0010	2	2
3	0011	3	3
4	0100	4	4
5	0101	5	5
6	0110	6	6
7	0111	7	7
8	1000	10	8
9	1001	11	9
10	1010	12	A
11	1011	13	B
12	1100	14	C
13	1101	15	D
14	1110	16	E
15	1111	17	F

# Binary, Octal, and Hexadecimal

- ❖ Binary, Octal, and Hexadecimal are related:  
Radix 16 =  $2^4$  and Radix 8 =  $2^3$
- ❖ Hexadecimal digit = 4 bits and Octal digit = 3 bits
- ❖ Starting from least-significant bit, group each 4 bits into a hex digit or each 3 bits into an octal digit
- ❖ Example: Convert 32-bit number into octal and hex

3	5	3	0	5	5	2	3	6	2	4	Octal																					
1	1	1	0	1	0	1	1	0	0	0	1	0	1	1	0	1	0	1	0	0	1	1	1	1	0	0	1	0	1	0	0	32-bit binary
E	B	1	6	A	7	9	4	Hexadecimal																								

# Converting Octal & Hex to Decimal

❖ Octal to Decimal:  $N_8 = (d_{n-1} \times 8^{n-1}) + \dots + (d_1 \times 8) + d_0$

❖ Hex to Decimal:  $N_{16} = (d_{n-1} \times 16^{n-1}) + \dots + (d_1 \times 16) + d_0$

❖ Examples:

$$(7204)_8 = (7 \times 8^3) + (2 \times 8^2) + (0 \times 8) + 4 = 3716$$

$$(3BA4)_{16} = (3 \times 16^3) + (11 \times 16^2) + (10 \times 16) + 4 = 15268$$

# Converting Decimal to Hexadecimal

- ❖ Repeatedly divide the decimal integer by 16
- ❖ Each remainder is a hex digit in the translated value
- ❖ Example: convert 422 to hexadecimal

Division	Quotient	Remainder
422 / 16	26	6
26 / 16	1	A
1 / 16	0	1

← least significant digit

← most significant digit

$$422 = (1A6)_{16}$$

← stop when  
quotient is zero

- ❖ To convert decimal to octal divide by 8 instead of 16



# Important Properties

- ❖ How many possible digits can we have in Radix  $r$ ?

$r$  digits: 0 to  $r - 1$

- ❖ What is the result of adding 1 to the largest digit in Radix  $r$ ?

Since digit  $r$  is not represented, result is  $(10)_r$  in Radix  $r$

Examples:  $1_2 + 1 = (10)_2$        $7_8 + 1 = (10)_8$

$9_{10} + 1 = (10)_{10}$        $F_{16} + 1 = (10)_{16}$

- ❖ What is the largest value using 3 digits in Radix  $r$ ?

In binary:  $(111)_2 = 2^3 - 1$

In octal:  $(777)_8 = 8^3 - 1$

In decimal:  $(999)_{10} = 10^3 - 1$

In Radix  $r$ :

largest value =  $r^3 - 1$

# Important Properties - cont'd

❖ How many possible values can be represented ...

Using  $n$  binary digits?

$2^n$  values: 0 to  $2^n - 1$

Using  $n$  octal digits

$8^n$  values: 0 to  $8^n - 1$

Using  $n$  decimal digits?

$10^n$  values: 0 to  $10^n - 1$

Using  $n$  hexadecimal digits

$16^n$  values: 0 to  $16^n - 1$

Using  $n$  digits in Radix  $r$ ?

$r^n$  values: 0 to  $r^n - 1$

# Next . . .

- ❖ Analog versus Digital Systems
- ❖ Digitization of Analog Signals
- ❖ Binary Numbers and Number Systems
- ❖ Number System Conversions
- ❖ **Representing Fractions**
- ❖ Binary Codes

# Representing Fractions

- ❖ A number  $N_r$  in *radix*  $r$  can also have a fraction part:

$$N_r = \underbrace{d_{n-1}d_{n-2} \dots d_1d_0}_{\text{Integer Part}} \cdot \underbrace{d_{-1}d_{-2} \dots d_{-m+1}d_{-m}}_{\text{Fraction Part}} \quad 0 \leq d_i < r$$

Radix Point

- ❖ The number  $N_r$  represents the value:

$$N_r = d_{n-1} \times r^{n-1} + \dots + d_1 \times r + d_0 + \quad (\text{Integer Part})$$

$$d_{-1} \times r^{-1} + d_{-2} \times r^{-2} \dots + d_{-m} \times r^{-m} \quad (\text{Fraction Part})$$

$$N_r = \sum_{i=0}^{i=n-1} d_i \times r^i + \sum_{j=-m}^{j=-1} d_j \times r^j$$

# Examples of Numbers with Fractions

$$\diamond (2409.87)_{10} = 2 \times 10^3 + 4 \times 10^2 + 9 + 8 \times 10^{-1} + 7 \times 10^{-2}$$

$$\diamond (1101.1001)_2 = 2^3 + 2^2 + 2^0 + 2^{-1} + 2^{-4} = 13.5625$$

$$\diamond (703.64)_8 = 7 \times 8^2 + 3 + 6 \times 8^{-1} + 4 \times 8^{-2} = 451.8125$$

$$\diamond (A1F.8)_{16} = 10 \times 16^2 + 16 + 15 + 8 \times 16^{-1} = 2591.5$$

$$\diamond (423.1)_5 = 4 \times 5^2 + 2 \times 5 + 3 + 5^{-1} = 113.2$$

$$\diamond (263.5)_6$$

Digit 6 is NOT allowed in radix 6

# Converting Decimal Fraction to Binary

- ❖ Convert  $N = 0.6875$  to Radix 2
- ❖ Solution: **Multiply**  $N$  by 2 repeatedly & collect integer bits

Multiplication	New Fraction	Bit	
$0.6875 \times 2 = 1.375$	0.375	1	→ First fraction bit
$0.375 \times 2 = 0.75$	0.75	0	
$0.75 \times 2 = 1.5$	0.5	1	
$0.5 \times 2 = 1.0$	0.0	1	→ Last fraction bit

- ❖ Stop when new fraction = 0.0, or when enough fraction bits are obtained
- ❖ Therefore,  $N = 0.6875 = (0.1011)_2$
- ❖ Check  $(0.1011)_2 = 2^{-1} + 2^{-3} + 2^{-4} = 0.6875$

# Converting Fraction to any Radix $r$

- ❖ To convert fraction  $N$  to any radix  $r$

$$N_r = (0.d_{-1} d_{-2} \dots d_{-m})_r = d_{-1} \times r^{-1} + d_{-2} \times r^{-2} \dots + d_{-m} \times r^{-m}$$

- ❖ Multiply  $N$  by  $r$  to obtain  $d_{-1}$

$$N_r \times r = d_{-1} + d_{-2} \times r^{-1} \dots + d_{-m} \times r^{-m+1}$$

- ❖ The integer part is the digit  $d_{-1}$  in radix  $r$

- ❖ The new fraction is  $d_{-2} \times r^{-1} \dots + d_{-m} \times r^{-m+1}$

- ❖ Repeat multiplying the new fractions by  $r$  to obtain  $d_{-2} d_{-3} \dots$

- ❖ Stop when new fraction becomes 0.0 or enough fraction digits are obtained

# More Conversion Examples

- ❖ Convert  $N = 139.6875$  to Octal (Radix 8)
- ❖ Solution:  $N = 139 + 0.6875$  (split integer from fraction)
- ❖ The integer and fraction parts are converted separately

Division	Quotient	Remainder
$139 / 8$	17	3
$17 / 8$	2	1
$2 / 8$	0	2

Multiplication	New Fraction	Digit
$0.6875 \times 8 = 5.5$	0.5	5
$0.5 \times 8 = 4.0$	0.0	4

- ❖ Therefore,  $139 = (213)_8$  and  $0.6875 = (0.54)_8$
- ❖ Now, join the integer and fraction parts with radix point  
 $N = 139.6875 = (213.54)_8$



# Conversion Procedure to Radix $r$

- ❖ To convert decimal number  $N$  (with fraction) to radix  $r$
- ❖ Convert the Integer Part
  - ✧ Repeatedly divide the integer part of number  $N$  by the radix  $r$  and **save the remainders**. The integer digits in radix  $r$  are the remainders in **reverse order** of their computation. If radix  $r > 10$ , then convert all remainders  $> 10$  to digits A, B, ... etc.
- ❖ Convert the Fractional Part
  - ✧ Repeatedly multiply the fraction of  $N$  by the radix  $r$  and **save the integer digits** that result. The fraction digits in radix  $r$  are the integer digits in **order of their computation**. If the radix  $r > 10$ , then convert all digits  $> 10$  to A, B, ... etc.
- ❖ Join the result together with the radix point



# Important Properties of Fractions

- ❖ How many fractional values exist with  $m$  fraction bits?

$2^m$  fractions, because each fraction bit can be 0 or 1

- ❖ What is the largest fraction value if  $m$  bits are used?

Largest fraction value =  $2^{-1} + 2^{-2} + \dots + 2^{-m} = 1 - 2^{-m}$

Because if you add  $2^{-m}$  to largest fraction you obtain 1

- ❖ In general, what is the largest fraction value if  $m$  fraction digits are used in radix  $r$ ?

Largest fraction value =  $r^{-1} + r^{-2} + \dots + r^{-m} = 1 - r^{-m}$

For decimal, largest fraction value =  $1 - 10^{-m}$

For hexadecimal, largest fraction value =  $1 - 16^{-m}$

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# Binary Codes

- ❖ How to represent characters, colors, etc?
- ❖ Define the set of all **represented elements**
- ❖ Assign a unique binary code to each element of the set
- ❖ Given  $n$  bits, a **binary code** is a mapping from the set of elements to a subset of the  $2^n$  binary numbers
- ❖ Coding Numeric Data (example: coding decimal digits)
  - ✧ Coding must simplify common arithmetic operations
  - ✧ Tight relation to binary numbers
- ❖ Coding Non-Numeric Data (example: coding colors)
  - ✧ More flexible codes since arithmetic operations are not applied

# Example of Coding Non-Numeric Data

- ❖ Suppose we want to code 7 colors of the rainbow
- ❖ As a minimum, we need 3 bits to define 7 unique values
- ❖ 3 bits define 8 possible combinations
- ❖ Only 7 combinations are needed
- ❖ Code 111 is not used
- ❖ Other assignments are also possible

Color	3-bit code
Red	000
Orange	001
Yellow	010
Green	011
Blue	100
Indigo	101
Violet	110

# Minimum Number of Bits Required

- ❖ Given a set of  $M$  elements to be represented by a binary code, the **minimum number of bits**,  $n$ , should satisfy:

$$2^{(n-1)} < M \leq 2^n$$

$n = \lceil \log_2 M \rceil$  where  $\lceil x \rceil$ , called the **ceiling function**, is the integer greater than or equal to  $x$

- ❖ How many bits are required to represent 10 decimal digits with a binary code?
- ❖ **Answer:**  $\lceil \log_2 10 \rceil = 4$  bits can represent 10 decimal digits

# Decimal Codes

- ❖ Binary number system is most natural for computers
- ❖ But people are used to the decimal number system
- ❖ Must convert decimal numbers to binary, do arithmetic on binary numbers, then convert back to decimal
- ❖ To simplify conversions, decimal codes can be used
- ❖ Define a binary code for each decimal digit
- ❖ Since 10 decimal digits exist, a 4-bit code is used
- ❖ But a 4-bit code gives 16 unique combinations
- ❖ 10 combinations are used and 6 will be unused



# Binary Coded Decimal (BCD)

- ❖ Simplest binary code for decimal digits
- ❖ Only encodes ten digits from 0 to 9
- ❖ BCD is a **weighted code**
- ❖ The weights are 8,4,2,1
- ❖ Same weights as a binary number
- ❖ There are **six invalid code words**  
1010, 1011, 1100, 1101, 1110, 1111
- ❖ Example on BCD coding:  
 $13 \Leftrightarrow (0001\ 0011)_{\text{BCD}}$

Decimal	BCD
0	0000
1	0001
2	0010
3	0011
4	0100
5	0101
6	0110
7	0111
8	1000
9	1001
Unused	1010
	...
	1111

# Warning: Conversion or Coding?

- ❖ Do **NOT** mix up **conversion** of a decimal number to a binary number with **coding** a decimal number with a binary code
- ❖  $13_{10} = (1101)_2$  This is **conversion**
- ❖  $13 \Leftrightarrow (0001\ 0011)_{\text{BCD}}$  This is **coding**
- ❖ In general, coding requires more bits than conversion
- ❖ A number with  $n$  decimal digits is coded with  $4n$  bits in BCD

# Other Decimal Codes

- ❖ BCD, 5421, 2421, and 8 4 -2 -1 are **weighted codes**
- ❖ Excess-3 is not a weighted code
- ❖ 2421, 8 4 -2 -1, and Excess-3 are **self complementary codes**

Decimal	BCD 8421	5421 code	2421 code	8 4 -2 -1 code	Excess-3 code
0	0000	0000	0000	0000	0011
1	0001	0001	0001	0111	0100
2	0010	0010	0010	0110	0101
3	0011	0011	0011	0101	0110
4	0100	0100	0100	0100	0111
5	0101	1000	1011	1011	1000
6	0110	1001	1100	1010	1001
7	0111	1010	1101	1001	1010
8	1000	1011	1110	1000	1011
9	1001	1100	1111	1111	1100
Unused	...	...	...	...	...

# Character Codes

## ❖ Character sets

- ❖ Standard ASCII: 7-bit character codes (0 – 127)
- ❖ Extended ASCII: 8-bit character codes (0 – 255)
- ❖ Unicode: 16-bit character codes (0 – 65,535)
- ❖ Unicode standard represents a universal character set
  - Defines codes for characters used in all major languages
  - Each character is encoded as 16 bits
- ❖ UTF-8: variable-length encoding used in HTML
  - Encodes all Unicode characters
  - Uses 1 byte for ASCII, but multiple bytes for other characters

## ❖ Null-terminated String

- ❖ Array of characters followed by a NULL character

# Printable ASCII Codes

	0	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F
2	space	!	"	#	\$	%	&	'	(	)	*	+	,	-	.	/
3	0	1	2	3	4	5	6	7	8	9	:	;	<	=	>	?
4	@	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
5	P	Q	R	S	T	U	V	W	X	Y	Z	[	\	]	^	_
6	`	a	b	c	d	e	f	g	h	i	j	k	l	m	n	o
7	p	q	r	s	t	u	v	w	x	y	z	{		}	~	DEL

## ❖ Examples:

- ❖ ASCII code for space character = 20 (hex) = 32 (decimal)
- ❖ ASCII code for 'L' = 4C (hex) = 76 (decimal)
- ❖ ASCII code for 'a' = 61 (hex) = 97 (decimal)

# Control Characters

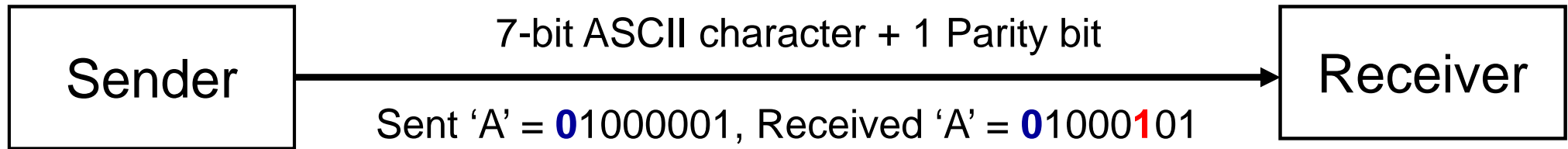
- ❖ The first 32 characters of ASCII table are used for control
- ❖ Control character codes = 00 to 1F (hexadecimal)
  - ✧ Not shown in previous slide
- ❖ Examples of Control Characters
  - ✧ Character 0 is the **NULL** character  $\Rightarrow$  used to terminate a string
  - ✧ Character 9 is the **Horizontal Tab (HT)** character
  - ✧ Character 0A (hex) = 10 (decimal) is the **Line Feed (LF)**
  - ✧ Character 0D (hex) = 13 (decimal) is the **Carriage Return (CR)**
  - ✧ The LF and CR characters are used together
    - They advance the cursor to the beginning of next line
- ❖ One control character appears at end of ASCII table
  - ✧ Character 7F (hex) is the **Delete (DEL)** character

# Parity Bit & Error Detection Codes

- ❖ Binary data are typically transmitted between computers
- ❖ Because of noise, a corrupted bit will change value
- ❖ To detect errors, **extra bits** are added to each data value
- ❖ **Parity bit**: is used to make the number of 1's odd or even
- ❖ **Even parity**: number of 1's in the transmitted data is even
- ❖ **Odd parity**: number of 1's in the transmitted data is odd

7-bit ASCII Character	With Even Parity	With Odd Parity
'A' = 1000001	<b>0</b> 1000001	<b>1</b> 1000001
'T' = 1010100	<b>1</b> 1010100	<b>0</b> 1010100

# Detecting Errors



- ❖ Suppose we are transmitting 7-bit ASCII characters
- ❖ A parity bit is added to each character to make it 8 bits
- ❖ Parity can detect all single-bit errors
  - ✧ If even parity is used and a single bit changes, it will change the parity to odd, which will be detected at the receiver end
  - ✧ The receiver end can detect the error, but cannot correct it because it does not know which bit is erroneous
- ❖ Can also detect some multiple-bit errors
  - ✧ Error in an **odd number** of bits