

EE 200- Digital Logic Circuit Design

2.7 Logic Operations

2.8 Logic Gates

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Entry Questions

- What are the logic functions we learned so far?
- Can you name other logic functions?



Objectives

- 1 Other Logic Operation
 - Boolean Expressions
 - Digital Logic Gates



Boolean Expressions

Table 2.8
Boolean Expressions for the 16 Functions of Two Variables

Boolean Functions	Operator Symbol	Name	Comments
$F_0 = 0$		Null	Binary constant 0
$F_1 = xy$	$x \cdot y$	AND	x and y
$F_2 = xy'$	x/y	Inhibition	x , but not y
$F_3 = x$		Transfer	x
$F_4 = x'y$	y/x	Inhibition	y , but not x
$F_5 = y$		Transfer	y
$F_6 = xy' + x'y$	$x \oplus y$	Exclusive-OR	x or y , but not both
$F_7 = x + y$	$x + y$	OR	x or y
$F_8 = (x + y)'$	$x \downarrow y$	NOR	Not-OR
$F_9 = xy + x'y'$	$(x \oplus y)'$	Equivalence	x equals y
$F_{10} = y'$	y'	Complement	Not y
$F_{11} = x + y'$	$x \subset y$	Implication	If y , then x
$F_{12} = x'$	x'	Complement	Not x
$F_{13} = x' + y$	$x \supset y$	Implication	If x , then y
$F_{14} = (xy)'$	$x \uparrow y$	NAND	Not-AND
$F_{15} = 1$		Identity	Binary constant 1

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AND, OR, Not (review)

- AND: Output c is TRUE if inputs a AND b are TRUE, else it is FALSE.



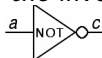
$$(a \cdot b \text{ or } ab)$$

- OR: Output c is TRUE if input a OR b is TRUE, else it is FALSE.



$$(a + b)$$

- NOT: Output c is TRUE if input a is FALSE, else it is FALSE.
 c is the inverse of a .



$$(\bar{a} \text{ or } a')$$



NAND & NOR

- NAND: Output c is FALSE if inputs a AND b are TRUE, else it is TRUE.



$$(ab)'$$

- NOR: Output c is FALSE if input a OR b is TRUE, else it is TRUE.



$$(a + b)'$$



XOR & XNOR

- XOR: Output c is TRUE if input a OR b is TRUE, else it is FALSE.



$$(a \oplus b = a'b + ab')$$

- XNOR: Output c is TRUE if both input a AND b are TRUE or FALSE, else it is FALSE.



$$(a \oplus b)' = ab + a'b'$$



Logic Gates

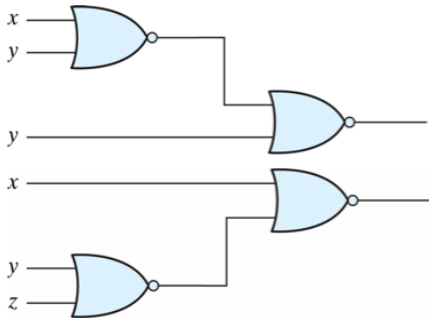
Name	Graphic symbol	Algebraic function	Truth table															
AND		$F = x \cdot y$	<table border="1"> <thead> <tr> <th>x</th> <th>y</th> <th>F</th> </tr> </thead> <tbody> <tr><td>0</td><td>0</td><td>0</td></tr> <tr><td>0</td><td>1</td><td>0</td></tr> <tr><td>1</td><td>0</td><td>0</td></tr> <tr><td>1</td><td>1</td><td>1</td></tr> </tbody> </table>	x	y	F	0	0	0	0	1	0	1	0	0	1	1	1
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Inverter		$F = x'$	<table border="1"> <thead> <tr> <th>x</th> <th>F</th> </tr> </thead> <tbody> <tr><td>0</td><td>1</td></tr> <tr><td>1</td><td>0</td></tr> </tbody> </table>	x	F	0	1	1	0									
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NAND		$F = (xy)'$	<table border="1"> <thead> <tr> <th>x</th> <th>y</th> <th>F</th> </tr> </thead> <tbody> <tr><td>0</td><td>0</td><td>1</td></tr> <tr><td>0</td><td>1</td><td>1</td></tr> <tr><td>1</td><td>0</td><td>1</td></tr> <tr><td>1</td><td>1</td><td>0</td></tr> </tbody> </table>	x	y	F	0	0	1	0	1	1	1	0	1	1	1	0
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NOR		$F = (x + y)'$	<table border="1"> <thead> <tr> <th>x</th> <th>y</th> <th>F</th> </tr> </thead> <tbody> <tr><td>0</td><td>0</td><td>1</td></tr> <tr><td>0</td><td>1</td><td>0</td></tr> <tr><td>1</td><td>0</td><td>0</td></tr> <tr><td>1</td><td>1</td><td>0</td></tr> </tbody> </table>	x	y	F	0	0	1	0	1	0	1	0	0	1	1	0
x	y	F																
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Exclusive-OR (XOR)		$F = xy' + x'y$ $= x \oplus y$	<table border="1"> <thead> <tr> <th>x</th> <th>y</th> <th>F</th> </tr> </thead> <tbody> <tr><td>0</td><td>0</td><td>0</td></tr> <tr><td>0</td><td>1</td><td>1</td></tr> <tr><td>1</td><td>0</td><td>1</td></tr> <tr><td>1</td><td>1</td><td>0</td></tr> </tbody> </table>	x	y	F	0	0	0	0	1	1	1	0	1	1	1	0
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Exclusive-NOR or equivalence		$F = xy + x'y'$ $= (x \oplus y)'$	<table border="1"> <thead> <tr> <th>x</th> <th>y</th> <th>F</th> </tr> </thead> <tbody> <tr><td>0</td><td>0</td><td>1</td></tr> <tr><td>0</td><td>1</td><td>0</td></tr> <tr><td>1</td><td>0</td><td>0</td></tr> <tr><td>1</td><td>1</td><td>1</td></tr> </tbody> </table>	x	y	F	0	0	1	0	1	0	1	0	0	1	1	1
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Extending Logic Properties

- NAND and NOR are not associative.





Summary

- 1 Other Logic Operation
 - Boolean Expressions
 - Digital Logic Gates



Next Lecture

- Boolean Functions.
- Canonical and Standard Forms.