



# Handbook of Formulae and Physical Constants

For The Use Of Students And Examination Candidates

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## Names in the Metric System

VALUE	EXPONENT	SYMBOL	PREFIX
1 000 000 000 000	$10^{12}$	T	tera
1 000 000 000	$10^9$	G	giga
1 000 000	$10^6$	M	mega
1 000	$10^3$	k	kilo
100	$10^2$	h	hecto
10	$10^1$	da	deca
0.1	$10^{-1}$	d	deci
0.01	$10^{-2}$	c	centi
0.001	$10^{-3}$	m	milli
0.000 001	$10^{-6}$	$\mu$	micro
0.000 000 001	$10^{-9}$	n	nano
0.000 000 000 001	$10^{-12}$	p	pico

## Conversion Chart for Metric Units

	To Milli-	To Centi-	To Deci-	To Metre, Gram, Litre	To Deca-	To Hecto-	To Kilo-
To Convert	Kilo-	$\times 10^6$	$\times 10^5$	$\times 10^4$	$\times 10^3$	$\times 10^2$	$\times 10^1$
	Hecto-	$\times 10^5$	$\times 10^4$	$\times 10^3$	$\times 10^2$	$\times 10^1$	$\times 10^{-1}$
	Deca-	$\times 10^4$	$\times 10^3$	$\times 10^2$	$\times 10^1$		$\times 10^{-2}$
	Metre, Gram, Litre	$\times 10^3$	$\times 10^2$	$\times 10^1$		$\times 10^{-1}$	$\times 10^{-2}$
	Deci-	$\times 10^2$	$\times 10^1$		$\times 10^{-1}$	$\times 10^{-2}$	$\times 10^{-3}$
	Centi-	$\times 10^1$		$\times 10^{-1}$	$\times 10^{-2}$	$\times 10^{-3}$	$\times 10^{-4}$
	Milli-		$\times 10^{-1}$	$\times 10^{-2}$	$\times 10^{-3}$	$\times 10^{-4}$	$\times 10^{-5}$

## BASIC UNITS

SI	IMPERIAL
<b>DISTANCE</b>	
1 metre (1 m) = 10 decimetres (10 dm) = 100 centimetres (100 cm) = 1000 millimetres (1000 mm)	12 in. = 1 ft 3 ft = 1 yd 5280 ft = 1 mile 1760 yd = 1 mile
1 decametre (1 dam) = 10 m 1 hectometre (1 hm) = 100 m 1 kilometre (1 km) = 1000 m	

### Conversions:

$$\begin{aligned}1 \text{ in.} &= 25.4 \text{ mm} \\1 \text{ ft} &= 30.48 \text{ cm} \\1 \text{ mile} &= 1.61 \text{ km} \\1 \text{ yd} &= 0.914 \text{ m} \\1 \text{ m} &= 3.28 \text{ ft}\end{aligned}$$

### Area

1 sq metre (1 m <sup>2</sup> ) = 10 000 cm <sup>2</sup> = 1 000 000 mm <sup>2</sup>	1 ft <sup>2</sup> = 144 in. <sup>2</sup> 1 yd <sup>2</sup> = 9 ft <sup>2</sup> 1 sq mile = 640 acre = 1 section
1 sq hectometre (1 hm <sup>2</sup> ) = 10 000 m <sup>2</sup> = 1 hectare (1 ha)	
1 sq km (1 km <sup>2</sup> ) = 1 000 000 m <sup>2</sup>	

### Conversions:

$$\begin{aligned}1 \text{ in.}^2 &= 6.45 \text{ cm}^2 = 645 \text{ mm}^2 \\1 \text{ m}^2 &= 10.8 \text{ ft}^2 \\1 \text{ acre} &= 0.405 \text{ ha} \\1 \text{ sq mile} &= 2.59 \text{ km}^2\end{aligned}$$

SI	IMPERIAL
<b>Volume</b>	
$1 \text{ m}^3 = 1\,000\,000 \text{ cm}^3$ $= 1 \times 10^9 \text{ mm}^3$	$1 \text{ ft}^3 = 1728 \text{ in.}^3$ $1 \text{ yd}^3 = 27 \text{ ft}^3$
$1 \text{ dm}^3 = 1 \text{ litre}$ $1 \text{ litre} = 1000 \text{ cm}^3$ $1 \text{ mL} = 1 \text{ cm}^3$ $1 \text{ m}^3 = 1000 \text{ litres}$	$1(\text{liquid}) \text{ U.S. gallon} = 231 \text{ in.}^3$ $= 4 (\text{liquid}) \text{ quarts}$ $1 \text{ U.S. barrel (bbl)} = 42 \text{ U.S. gal.}$ $1 \text{ imperial gallon} = 1.2 \text{ U.S. gal.}$

**Conversions:**

$$\begin{aligned}
 1 \text{ in.}^3 &= 16.4 \text{ cm}^3 \\
 1 \text{ m}^3 &= 35.3 \text{ ft}^3 \\
 1 \text{ litre} &= 61 \text{ in.}^3 \\
 1 \text{ U.S. gal} &= 3.78 \text{ litres} \\
 1 \text{ U.S. bbl} &= 159 \text{ litres} \\
 1 \text{ litre/s} &= 15.9 \text{ U.S. gal/min}
 \end{aligned}$$

**Mass and Weight**

$$\begin{aligned}
 1 \text{ kilogram (1 kg)} &= 1000 \text{ grams} \\
 1000 \text{ kg} &= 1 \text{ tonne}
 \end{aligned}$$

$$\begin{aligned}
 2000 \text{ lb} &= 1 \text{ ton (short)} \\
 1 \text{ long ton} &= 2240 \text{ lb}
 \end{aligned}$$

**Conversions:**

1 kg (on Earth) results in a weight of 2.2 lb

**Density**

$$\text{mass density} = \frac{\text{mass}}{\text{volume}}$$

$$\rho = \frac{m}{V} \left( \frac{\text{kg}}{\text{m}^3} \right)$$

$$\text{weight density} = \frac{\text{weight}}{\text{volume}}$$

$$\rho = \frac{w}{V} \left( \frac{\text{lb}}{\text{ft}^3} \right)$$

**Conversions:**

(on Earth) a mass density of  $1 \frac{\text{kg}}{\text{m}^3}$  results in a weight density of  $0.0623 \frac{\text{lb}}{\text{ft}^3}$

**SI****Imperial****RELATIVE DENSITY**

In SI R.D. is a comparison of mass density to a standard. For solids and liquids the standard is fresh water.

In Imperial the corresponding quantity is **specific gravity**; for solids and liquids a comparison of weight density to that of water.

**Conversions:**

In both systems the same numbers hold for R.D. as for S.G. since these are equivalent ratios.

**RELATIVE DENSITY (SPECIFIC GRAVITY) OF VARIOUS SUBSTANCES**

Water (fresh).....	1.00	Mica.....	2.9
Water (sea average) ....	1.03	Nickel .....	8.6
Aluminum.....	2.56	Oil (linseed) .....	0.94
Antimony.....	6.70	Oil (olive) .....	0.92
Bismuth.....	9.80	Oil (petroleum) .....	0.76-0.86
Brass .....	8.40	Oil (turpentine) .....	0.87
Brick .....	2.1	Paraffin .....	0.86
Calcium.....	1.58	Platinum.....	21.5
Carbon (diamond).....	3.4	Sand (dry) .....	1.42
Carbon (graphite).....	2.3	Silicon.....	2.6
Carbon (charcoal) .....	1.8	Silver.....	10.57
Chromium.....	6.5	Slate .....	2.1-2.8
Clay.....	1.9	Sodium.....	0.97
Coal.....	1.36-1.4	Steel (mild) .....	7.87
Cobalt .....	8.6	Sulphur .....	2.07
Copper .....	8.77	Tin.....	7.3
Cork .....	0.24	Tungsten .....	19.1
Glass (crown).....	2.5	Wood (ash) .....	0.75
Glass (flint).....	3.5	Wood (beech) .....	0.7-0.8
Gold .....	19.3	Wood (ebony).....	1.1-1.2
Iron (cast).....	7.21	Wood (elm).....	0.66
Iron (wrought) .....	7.78	Wood (lignum-vitae) ..	1.3
Lead .....	11.4	Wood (oak).....	0.7-1.0
Magnesium .....	1.74	Wood (pine).....	0.56
Manganese.....	8.0	Wood (teak) .....	0.8
Mercury .....	13.6	Zinc.....	7.0

## Greek Alphabet

Alpha	$\alpha$	Iota	$\iota$	Rho	$\rho$
Beta	$\beta$	Kappa	$\kappa$	Sigma	$\Sigma, \sigma$
Gamma	$\gamma$	Lambda	$\lambda$	Tau	$\tau$
Delta	$\Delta$	Mu	$\mu$	Upsilon	$\upsilon$
Epsilon	$\varepsilon$	Nu	$\nu$	Phi	$\Phi, \phi$
Zeta	$\zeta$	Xi	$\xi$	Kai	$\chi$
Eta	$\eta$	Omicron	$O$	Psi	$\Psi$
Theta	$\theta$	Pi	$\pi$	Omega	$\Omega, \omega$

## MATHEMATICAL FORMULAE

### Algebra

#### 1. Expansion Formulae

$$(x + y)^2 = x^2 + 2xy + y^2$$

$$(x - y)^2 = x^2 - 2xy + y^2$$

$$x^2 - y^2 = (x - y)(x + y)$$

$$(x + y)^3 = x^3 + 3x^2y + 3xy^2 + y^3$$

$$x^3 + y^3 = (x + y)(x^2 - xy + y^2)$$

$$(x - y)^3 = x^3 - 3x^2y + 3xy^2 - y^3$$

$$x^3 - y^3 = (x - y)(x^2 + xy + y^2)$$

#### 2. Quadratic Equation

$$\text{If } ax^2 + bx + c = 0,$$

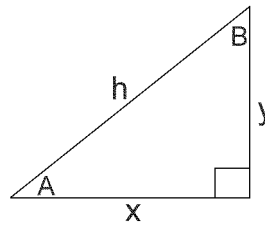
$$\text{Then } x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$



## Trigonometry

### 1. Basic Ratios

$$\sin A = \frac{y}{h}, \quad \cos A = \frac{x}{h}, \quad \tan A = \frac{y}{x}$$



### 2. Pythagoras' Law

$$x^2 + y^2 = h^2$$

### 3. Trigonometric Function Values

Sin is positive from  $0^\circ$  to  $90^\circ$  and positive from  $90^\circ$  to  $180^\circ$

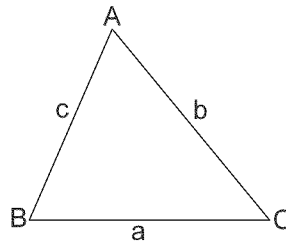
Cos is positive from  $0^\circ$  to  $90^\circ$  and negative from  $90^\circ$  to  $180^\circ$

Tan is positive from  $0^\circ$  to  $90^\circ$  and negative from  $90^\circ$  to  $180^\circ$

### 4. Solution of Triangles

#### a. Sine Law

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$



#### b. Cosine Law

$$c^2 = a^2 + b^2 - 2 ab \cos C$$

$$a^2 = b^2 + c^2 - 2 bc \cos A$$

$$b^2 = a^2 + c^2 - 2 ac \cos B$$

## Geometry

### 1. Areas of Triangles

#### a. All Triangles

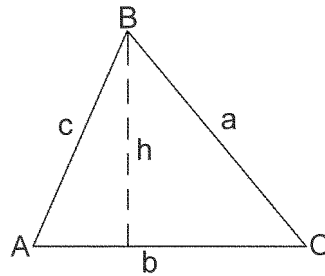
$$\text{Area} = \frac{\text{base} \times \text{perpendicular height}}{2}$$

$$\text{Area} = \frac{bc \sin A}{2} = \frac{ab \sin C}{2} = \frac{ac \sin B}{2}$$

and,

$$\text{Area} = \sqrt{s(s-a)(s-b)(s-c)}$$

where,  $s$  is half the sum of the sides, or  $s = \frac{a+b+c}{2}$



#### b. Equilateral Triangles

$$\text{Area} = 0.433 \times \text{side}^2$$

### 2. Circumference of a Circle

$$C = \pi d$$

### 3. Area of a Circle

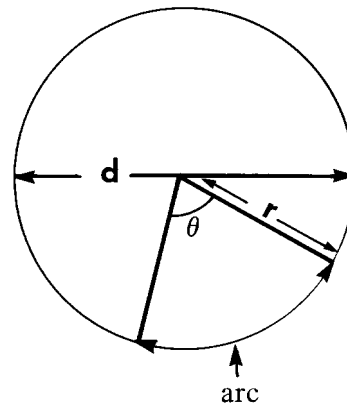
$$A = \pi r^2 = \frac{\text{circumference} \times r}{2} = \frac{\pi}{4} d^2 = 0.7854 d^2$$

### 4. Area of a Sector of a Circle

$$A = \frac{\text{arc} \times r}{2}$$

$$A = \frac{\theta^\circ}{360} \times \pi r^2 \quad (\theta = \text{angle in degrees})$$

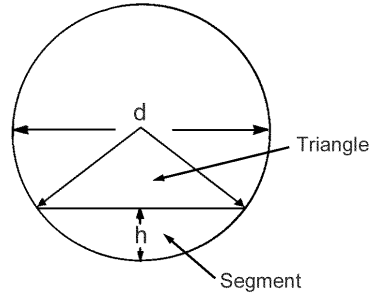
$$A = \frac{\theta^{\text{radians}}}{2} r^2 \quad (\theta = \text{angle in radians})$$



**5. Area of a Segment of a Circle**

$A = \text{area of sector} - \text{area of triangle}$

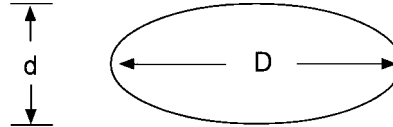
Also approximate area  $= \frac{4}{3} h^2 \sqrt{\frac{d}{h} - 0.608}$



**6. Ellipse**

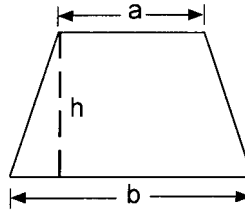
$A = \frac{\pi}{4} Dd$

Approx. circumference  $= \pi \frac{(D+d)}{2}$



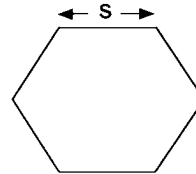
**7. Area of Trapezoid**

$A = \left( \frac{a+b}{2} \right) h$



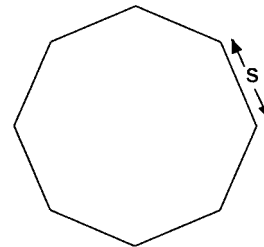
**8. Area of Hexagon**

$A = 2.6s^2$  where  $s$  is the length of one side



**9. Area of Octagon**

$A = 4.83s^2$  where  $s$  is the length of one side



**10. Sphere**

Total surface area  $A = 4\pi r^2$

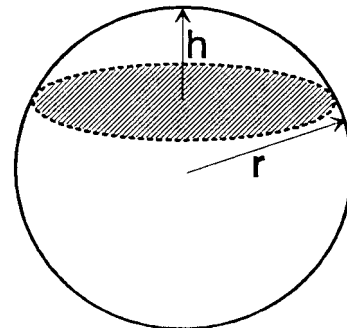
Surface area of segment  $A_s = \pi dh$

Volume  $V = \frac{4}{3} \pi r^3$

Volume of segment

$V_s = \frac{\pi h^2}{3} (3r - h)$

$V_s = \frac{\pi h}{6} (h^2 + 3a^2)$  where  $a = \text{radius of segment base}$



### 11. Volume of a Cylinder

$$V = \frac{\pi}{4} d^2 L \quad \text{where } L \text{ is cylinder length}$$

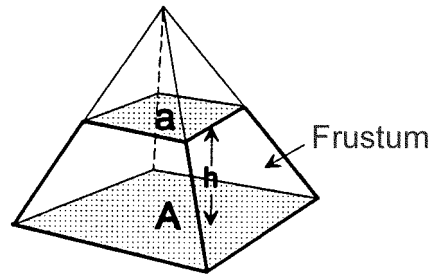
### 12. Pyramid

Volume

$$V = \frac{1}{3} \text{ base area} \times \text{perpendicular height}$$

Volume of frustum

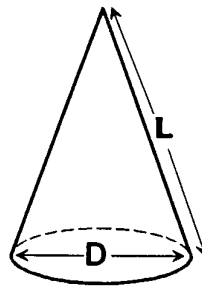
$$V_F = \frac{h}{3} (A + a + \sqrt{Aa}) \quad \text{where } h \text{ is the perpendicular height, } A \text{ and } a \text{ are areas as shown}$$



### 13. Cone

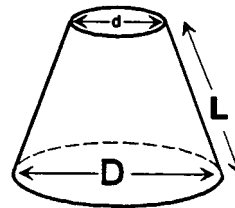
Area of curved surface of cone:

$$A = \frac{\pi DL}{2}$$



Area of curved surface of frustum

$$A_F = \frac{\pi (D + d)L}{2}$$



Volume of cone:

$$V = \frac{\text{base area} \times \text{perpendicular height}}{3}$$

Volume of frustum:

$$V_F = \frac{\text{perpendicular height} \times \pi (R^2 + r^2 + Rr)}{3}$$

## APPLIED MECHANICS

**Scalar** - a property described by a magnitude only

**Vector** - a property described by a magnitude and a direction

**Velocity** - vector property equal to  $\frac{\text{displacement}}{\text{time}}$

The magnitude of velocity may be referred to as **speed**

In SI the basic unit is  $\frac{\text{m}}{\text{s}}$ , in Imperial  $\frac{\text{ft}}{\text{s}}$

Other common units are  $\frac{\text{km}}{\text{h}}$ ,  $\frac{\text{mi}}{\text{h}}$

$$\text{Conversions: } 1 \frac{\text{m}}{\text{s}} = 3.28 \frac{\text{ft}}{\text{s}}$$

$$1 \frac{\text{km}}{\text{h}} = 0.621 \frac{\text{mi}}{\text{h}}$$

Speed of sound in dry air is  $331 \frac{\text{m}}{\text{s}}$  at  $0^\circ\text{C}$  and increases by about  $0.61 \frac{\text{m}}{\text{s}}$  for each  $^\circ\text{C}$  rise

Speed of light in vacuum equals  $3 \times 10^8 \frac{\text{m}}{\text{s}}$

**Acceleration** - vector property equal to  $\frac{\text{change in velocity}}{\text{time}}$

In SI the basic unit is  $\frac{\text{m}}{\text{s}^2}$ , in Imperial  $\frac{\text{ft}}{\text{s}^2}$

$$\text{Conversion: } 1 \frac{\text{m}}{\text{s}^2} = 3.28 \frac{\text{ft}}{\text{s}^2}$$

Acceleration due to gravity, symbol "g", is  $9.81 \frac{\text{m}}{\text{s}^2}$  or  $32.2 \frac{\text{ft}}{\text{s}^2}$

## LINEAR VELOCITY AND ACCELERATION

u initial velocity  
 v final velocity  
 t elapsed time  
 s displacement  
 a acceleration

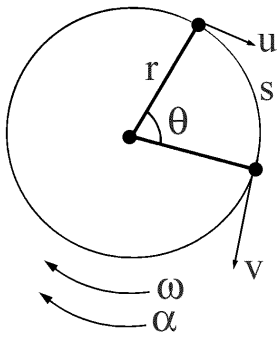
$$v = u + at$$

$$s = \left(\frac{v + u}{2}\right)t$$

$$s = ut + \frac{1}{2}at^2$$

$$v^2 = u^2 + 2as$$

### Angular Velocity and Acceleration



$\theta$  angular displacement (radians)  
 $\omega$  angular velocity (radians/s);  $\omega_1 =$  initial,  $\omega_2 =$  final  
 $\alpha$  angular acceleration (radians/s<sup>2</sup>)

$$\omega_2 = \omega_1 + \alpha t$$

$$\theta = \frac{\omega_1 + \omega_2}{2} \times t$$

$$\theta = \omega_1 t + \frac{1}{2} \alpha t^2$$

$$\omega_2^2 = \omega_1^2 + 2 \alpha \theta$$

linear displacement,  $s = r \theta$

linear velocity,  $v = r \omega$

linear, or tangential acceleration,  $a_T = r \alpha$

## Tangential, Centripetal and Total Acceleration

Tangential acceleration  $a_T$  is due to angular acceleration  $\alpha$

$$a_T = r\alpha$$

Centripetal (Centrifugal) acceleration  $a_c$  is due to change in direction only

$$a_c = v^2/r = r\omega^2$$

Total acceleration,  $a$ , of a rotating point experiencing angular acceleration is the vector sum of  $a_T$  and  $a_c$

$$a = a_T + a_c$$

## FORCE

Vector quantity, a push or pull which changes the shape and/or motion of an object

In SI the unit of force is the newton, N, defined as a  $\frac{\text{kg m}}{\text{s}^2}$

In Imperial the unit of force is the pound lb

$$\text{Conversion: } 9.81 \text{ N} = 2.2 \text{ lb}$$

## Weight

The gravitational force of attraction between a mass,  $m$ , and the mass of the Earth

In SI weight can be calculated from

$$\text{Weight} = F = mg, \quad \text{where } g = 9.81 \text{ m/s}^2$$

In Imperial, the mass of an object (rarely used), in slugs, can be calculated from the known weight in pounds

$$m = \frac{\text{Weight}}{g} \quad g = 32.2 \frac{\text{ft}}{\text{s}^2}$$

## Newton's Second Law of Motion

An unbalanced force  $F$  will cause an object of mass  $m$  to accelerate  $a$ , according to:

$$F = ma \quad (\text{Imperial } F = \frac{W}{g} a, \text{ where } w \text{ is weight})$$

## Torque Equation

$$T = I \alpha \quad \text{where } T \text{ is the acceleration torque in Nm, } I \text{ is the moment of inertia in } \text{kg m}^2 \text{ and } \alpha \text{ is the angular acceleration in radians/s}^2$$

## Momentum

Vector quantity, symbol  $p$ ,

$$p = mv \quad (\text{Imperial } p = \frac{W}{g} v, \text{ where } w \text{ is weight})$$

in SI unit is  $\frac{\text{kg m}}{\text{s}}$

## Work

Scalar quantity, equal to the (vector) product of a force and the displacement of an object. In simple systems, where  $W$  is work,  $F$  force and  $s$  distance

$$W = F s$$

In SI the unit of work is the joule, J, or kilojoule, kJ

$$1 \text{ J} = 1 \text{ Nm}$$

In Imperial the unit of work is the ft-lb

## Energy

Energy is the ability to do work, the units are the same as for work; J, kJ, and ft-lb



## **Kinetic Energy**

Energy due to motion

$$E_k = \frac{1}{2}mv^2$$

In Imperial this is usually expressed as  $E_k = \frac{W}{2g}v^2$  where  $w$  is weight

## **Kinetic Energy of Rotation**

$$E_R = \frac{1}{2}mk^2\omega^2 \quad \text{where } k \text{ is radius of gyration, } \omega \text{ is angular velocity in rad/s}$$

or

$$E_R = \frac{1}{2}I\omega^2 \quad \text{where } I = mk^2 \text{ is the moment of inertia}$$

## **CENTRIPETAL (CENTRIFUGAL) FORCE**

$$F_C = \frac{mv^2}{r} \quad \text{where } r \text{ is the radius}$$

or

$$F_C = m\omega^2 r \quad \text{where } \omega \text{ is angular velocity in rad/s}$$

## **Potential Energy**

Energy due to position in a force field, such as gravity

$$E_p = m g h$$

In Imperial this is usually expressed  $E_p = w h$  where  $w$  is weight, and  $h$  is height above some specified datum

## Thermal Energy

In SI the common units of thermal energy are J, and kJ, (and kJ/kg for specific quantities)

In Imperial, the units of thermal energy are British Thermal Units (Btu)

**Conversions:**     1 Btu = 1055 J  
                      1 Btu = 778 ft-lb

## Electrical Energy

In SI the units of electrical energy are J, kJ and kilowatt hours kWh. In Imperial, the unit of electrical energy is the kWh

**Conversions:**     1 kWh = 3600 kJ  
                      1 kWh = 3412 Btu =  $2.66 \times 10^6$  ft-lb

## Power

A scalar quantity, equal to the rate of doing work

In SI the unit is the Watt W (or kW)

$$1 \text{ W} = 1 \frac{\text{J}}{\text{s}}$$

In Imperial, the units are:

Mechanical Power -  $\frac{\text{ft-lb}}{\text{s}}$ , horsepower h.p.

Thermal Power -  $\frac{\text{Btu}}{\text{s}}$

Electrical Power - W, kW, or h.p.

**Conversions:**     746 W = 1 h.p.

$$1 \text{ h.p.} = 550 \frac{\text{ft-lb}}{\text{s}}$$

$$1 \text{ kW} = 0.948 \frac{\text{Btu}}{\text{s}}$$

## Pressure

A vector quantity, force per unit area

In SI the basic units of pressure are pascals Pa and kPa

$$1 \text{ Pa} = 1 \frac{\text{N}}{\text{m}^2}$$

In Imperial, the basic unit is the pound per square inch, psi

## Atmospheric Pressure

At sea level atmospheric pressure equals 101.3 kPa or 14.7 psi

## Pressure Conversions

$$1 \text{ psi} = 6.895 \text{ kPa}$$

Pressure may be expressed in standard units, or in units of static fluid head, in both SI and Imperial systems

Common equivalencies are:

$$1 \text{ kPa} = 0.294 \text{ in. mercury} = 7.5 \text{ mm mercury}$$

$$1 \text{ kPa} = 4.02 \text{ in. water} = 102 \text{ mm water}$$

$$1 \text{ psi} = 2.03 \text{ in. mercury} = 51.7 \text{ mm mercury}$$

$$1 \text{ psi} = 27.7 \text{ in. water} = 703 \text{ mm water}$$

$$1 \text{ m H}_2\text{O} = 9.81 \text{ kPa}$$

Other pressure unit conversions:

$$1 \text{ bar} = 14.5 \text{ psi} = 100 \text{ kPa}$$

$$1 \text{ kg/cm}^2 = 98.1 \text{ kPa} = 14.2 \text{ psi} = 0.981 \text{ bar}$$

$$1 \text{ atmosphere (atm)} = 101.3 \text{ kPa} = 14.7 \text{ psi}$$

## Simple Harmonic Motion

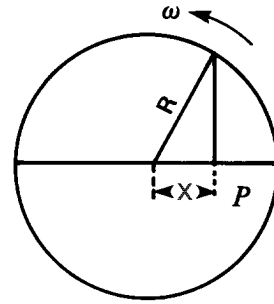
$$\text{Velocity of P} = \omega \sqrt{R^2 - x^2} \frac{\text{m}}{\text{s}}$$

$$\text{Acceleration of P} = \omega^2 x \text{ m/s}^2$$

$$\text{The period or time of a complete oscillation} = \frac{2\pi}{\omega} \text{ seconds}$$

General formula for the period of S.H.M.

$$T = 2\pi \sqrt{\frac{\text{displacement}}{\text{acceleration}}}$$



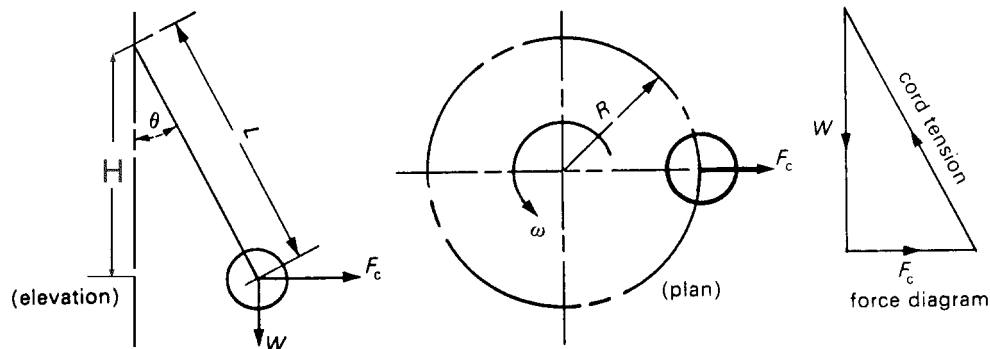
## Simple Pendulum

$$T = 2\pi \sqrt{\frac{L}{g}}$$

T = period or time in seconds for a double swing

L = length in metres

## The Conical Pendulum



$$R/H = \tan \theta = F_c/W = \omega^2 R/g$$

## Lifting Machines

$W$  = load lifted,       $F$  = force applied

$$\text{M.A.} = \frac{\text{load}}{\text{effort}} = \frac{W}{F}$$

$$\text{V.R. (velocity ratio)} = \frac{\text{effort distance}}{\text{load distance}}$$

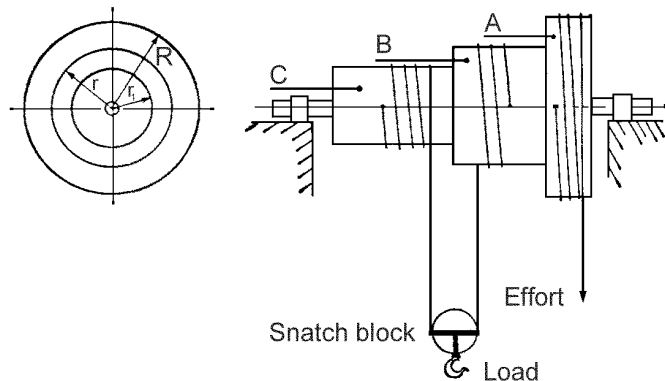
$$\eta = \text{efficiency} = \frac{\text{M.A.}}{\text{V.R.}}$$

### 1. Lifting Blocks

V.R. = number of rope strands supporting the load block

### 2. Wheel & Differential Axle

$$\begin{aligned} \text{Velocity ratio} &= \frac{2\pi R}{\frac{2\pi(r - r_1)}{2}} \\ &= \frac{2R}{r - r_1} \cdot 2 \end{aligned}$$



Or, using diameters instead of radii,

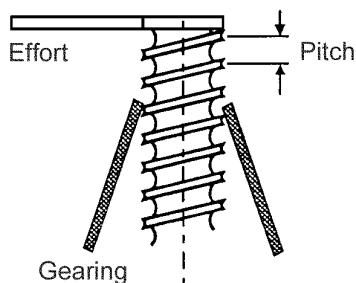
$$\text{Velocity ratio} = \frac{2D}{(d - d_1)}$$

### 3. Inclined Plane

$$\text{V.R.} = \frac{\text{length}}{\text{height}}$$

### 4. Screw Jack

$$\text{V.R.} = \frac{\text{circumference of leverage}}{\text{pitch of thread}}$$



## Indicated Power

I.P. =  $P_m A L N$  where I.P. is power in W,  $P_m$  is mean or "average" effective pressure in Pa,  $A$  is piston area in  $m^2$ ,  $L$  is length of stroke in m and  $N$  is number of power strokes per second

## Brake Power

B.P. =  $T\omega$  where B.P. is brake power in W,  $T$  is torque in Nm and  $\omega$  is angular velocity in radian/second

## STRESS, STRAIN and MODULUS OF ELASTICITY

$$\text{Direct stress} = \frac{\text{load}}{\text{area}} = \frac{P}{A}$$

$$\text{Direct strain} = \frac{\text{extension}}{\text{original length}} = \frac{\Delta \ell}{L}$$

Modulus of elasticity

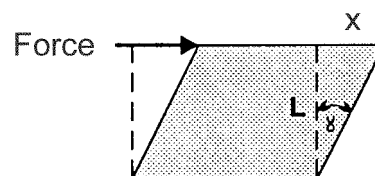
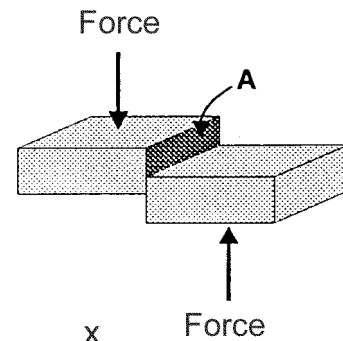
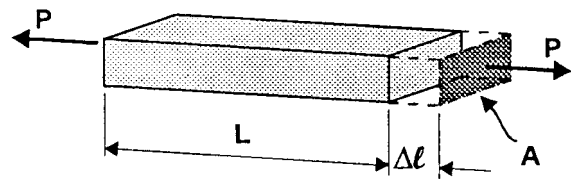
$$E = \frac{\text{direct stress}}{\text{direct strain}} = \frac{P/A}{\Delta \ell / L} = \frac{PL}{A\Delta \ell}$$

$$\text{Shear stress } \tau = \frac{\text{force}}{\text{area under shear}}$$

$$\text{Shear strain} = \frac{x}{L}$$

Modulus of rigidity

$$G = \frac{\text{shear stress}}{\text{shear strain}}$$



## General Torsion Equation (Shafts of circular cross-section)

$$\frac{T}{J} = \frac{\tau}{r} = \frac{G \theta}{L}$$

### 1. For Solid Shaft

$$J = \frac{\pi}{2} r^4 = \frac{\pi d^4}{32}$$

### 2. For Hollow Shaft

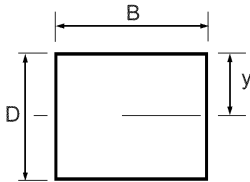
$$J = \frac{\pi}{2} (r_1^4 - r_2^4)$$
$$= \frac{\pi}{32} (d_1^4 - d_2^4)$$

- T = torque or twisting moment in newton metres  
J = polar second moment of area of cross-section about shaft axis.  
 $\tau$  = shear stress at outer fibres in pascals  
r = radius of shaft in metres  
G = modulus of rigidity in pascals  
 $\theta$  = angle of twist in radians  
L = length of shaft in metres  
d = diameter of shaft in metres

## Relationship Between Bending Stress and External Bending Moment

$$\frac{M}{I} = \frac{\sigma}{y} = \frac{E}{R}$$

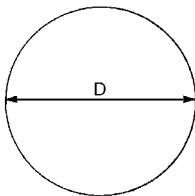
### 1. For Rectangle



$$I = \frac{BD^3}{12}$$

- M = external bending moment in newton metres  
I = second moment of area in m<sup>4</sup>  
 $\sigma$  = bending stress at outer fibres in pascals  
y = distance from centroid to outer fibres in metres  
E = modulus of elasticity in pascals  
R = radius of curvature in metres

### 2. For Solid Shaft



$$I = \frac{\pi D^4}{64}$$

## **THERMODYNAMICS**

### **Temperature Scales**

$$^{\circ}\text{C} = \frac{5}{9} (^{\circ}\text{F} - 32) \qquad ^{\circ}\text{F} = \frac{9}{5} ^{\circ}\text{C} + 32$$

$$^{\circ}\text{R} = ^{\circ}\text{F} + 460 \text{ (R Rankine)} \quad \text{K} = ^{\circ}\text{C} + 273 \text{ (K Kelvin)}$$

### **Sensible Heat Equation**

$$Q = mc\Delta T$$

m is mass

c is specific heat

$\Delta T$  is temperature change

### **Latent Heat**

$$\begin{aligned} \text{Latent heat of fusion of ice} &= 335 \text{ kJ/kg} \\ \text{Latent heat of steam from and at } 100^{\circ}\text{C} &= 2257 \text{ kJ/kg} \\ \text{1 tonne of refrigeration} &= 335\,000 \text{ kJ/day} \\ &= 233 \text{ kJ/min} \end{aligned}$$

### **Gas Laws**

#### **1. Boyle's Law**

When gas temperature is constant

$$PV = \text{constant or}$$

$$P_1V_1 = P_2V_2$$

where P is absolute pressure and V is volume

#### **2. Charles' Law**

When gas pressure is constant,  $\frac{V}{T} = \text{constant}$

$$\text{or } \frac{V_1}{T_1} = \frac{V_2}{T_2}, \text{ where V is volume and T is absolute temperature}$$



### 3. Gay-Lussac's Law

When gas volume is constant,  $\frac{P}{T} = \text{constant}$

Or  $\frac{P_1}{T_1} = \frac{P_2}{T_2}$ , where P is absolute pressure and T is absolute temperature

### 4. General Gas Law

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2} = \text{constant}$$

$P V = m R T$  where P = absolute pressure (kPa)  
 V = volume (m<sup>3</sup>)  
 T = absolute temp (K)  
 m = mass (kg)  
 R = characteristic constant (kJ/kgK)

Also

$PV = nR_0T$  where P = absolute pressure (kPa)  
 V = volume (m<sup>3</sup>)  
 T = absolute temperature K  
 N = the number of kmoles of gas  
 R<sub>0</sub> = the universal gas constant 8.314 kJ/kmol/K

### SPECIFIC HEATS OF GASES

GAS	Specific Heat at Constant Pressure kJ/kgK or kJ/kg °C	Specific Heat at Constant Volume kJ/kgK or kJ/kg °C	Ratio of Specific Heats $\gamma = c_p / c_v$
Air	1.005	0.718	1.40
Ammonia	2.060	1.561	1.32
Carbon Dioxide	0.825	0.630	1.31
Carbon Monoxide	1.051	0.751	1.40
Helium	5.234	3.153	1.66
Hydrogen	14.235	10.096	1.41
Hydrogen Sulphide	1.105	0.85	1.30
Methane	2.177	1.675	1.30
Nitrogen	1.043	0.745	1.40
Oxygen	0.913	0.652	1.40
Sulphur Dioxide	0.632	0.451	1.40

## Efficiency of Heat Engines

Carnot Cycle  $\eta = \frac{T_1 - T_2}{T_1}$  where  $T_1$  and  $T_2$  are absolute temperatures of heat source and sink

## Air Standard Efficiencies

### 1. Spark Ignition Gas and Oil Engines (Constant Volume Cycle or Otto Cycle)

$$\eta = 1 - \frac{1}{r_v^{(\gamma-1)}} \quad \text{where } r_v = \text{compression ratio} = \frac{\text{cylinder volume}}{\text{clearance volume}}$$

$$\gamma = \frac{\text{specific heat (constant pressure)}}{\text{specific heat (constant volume)}}$$

### 2. Diesel Cycle

$$\eta = 1 - \frac{(R^\gamma - 1)}{r_v^{\gamma-1} \gamma (R - 1)} \quad \text{where } r = \text{ratio of compression}$$

$R = \text{ratio of cut-off volume to clearance volume}$

### 3. High Speed Diesel (Dual-Combustion) Cycle

$$\eta = 1 - \frac{k\beta^\gamma - 1}{r_v^{\gamma-1} [(k-1) + \gamma k(\beta-1)]}$$

$$\text{where } r_v = \frac{\text{cylinder volume}}{\text{clearance volume}}$$

$$k = \frac{\text{absolute pressure at end of constant V heating (combustion)}}{\text{absolute pressure at beginning of constant V combustion}}$$

$$\beta = \frac{\text{volume at end of constant P heating (combustion)}}{\text{clearance volume}}$$

### 4. Gas Turbines (Constant Pressure or Brayton Cycle)

$$\eta = 1 - \frac{1}{r_p^{\left(\frac{\gamma-1}{\gamma}\right)}}$$

**THERMODYNAMIC EQUATIONS FOR PERFECT GASES (Non-Flow Processes)**

where  $r_p = \text{pressure ratio} = \frac{\text{compressor discharge pressure}}{\text{compressor intake pressure}}$

Name of Process	Value of $n$	$P - V - T$ Relationships			Heat Added ${}_1Q_2$ kJ	Work Done ${}_1W_2$ kJ	Change In Internal Energy $U_2 - U_1$ kJ	Change In Enthalpy $H_2 - H_1$ kJ	Change In Entropy $S_2 - S_1$ kJ/K
		$P - V$	$T - P$	$T - V$					
Constant Volume $V = \text{Const.}$	$\infty$	—	$\frac{T_1}{T_2} = \frac{P_1}{P_2}$	—	0	$m c_v (T_2 - T_1)$	$m c_p (T_2 - T_1)$	$m c_v \log_e \frac{T_2}{T_1}$	
Constant Pressure $P = \text{Const.}$	0	—	—	$\frac{T_1}{T_2} = \frac{V_1}{V_2}$	$m c_p (T_2 - T_1)$	$m c_v (T_2 - T_1)$	$m c_p (T_2 - T_1)$	$m c_p \log_e \frac{T_2}{T_1}$	
Isothermal $T = \text{Const.}$	1	$\frac{P_1}{P_2} = \frac{V_2}{V_1}$	—	—	$m R T \log_e \frac{P_1}{P_2}$	0	0	$m R \log_e \frac{P_1}{P_2}$	
Isentropic* $S = \text{Const.}$	$\gamma$	$\frac{P_1}{P_2} = \left(\frac{V_2}{V_1}\right)^\gamma$	$\frac{T_1}{T_2} = \left(\frac{P_1}{P_2}\right)^{\frac{\gamma-1}{\gamma}}$	$\frac{T_1}{T_2} = \left(\frac{V_2}{V_1}\right)^{\gamma-1}$	0	$m c_v (T_2 - T_1)$	$m c_p (T_2 - T_1)$	0	
Polytropic $PV^n = \text{Const.}$	$n$	$\frac{P_1}{P_2} = \left(\frac{V_2}{V_1}\right)^n$	$\frac{T_1}{T_2} = \left(\frac{P_1}{P_2}\right)^{\frac{n-1}{n}}$	$\frac{T_1}{T_2} = \left(\frac{V_2}{V_1}\right)^{n-1}$	$\frac{mR}{n-1} (T_1 - T_2)$	$m c_v (T_2 - T_1)$	$m c_p (T_2 - T_1)$	$m c_n \log_e \frac{T_2}{T_1}$	

\*Can be used for reversible adiabatic processes

$c_v$  = Specific heat at constant volume, kJ/kgK

$c_p$  = Specific heat at constant pressure, kJ/kgK

$c_n$  = Specific heat for a polytropic process =  $c_v \left(\frac{\gamma - n}{1 - n}\right)$  kJ/kgK

H = Enthalpy, kJ

$\gamma$  = Isentropic exponent,  $c_p/c_v$

$n$  = Polytropic exponent

P = Pressure, kPa

R = Gas content, kJ/kgK

S = Entropy, kJ/K

T = Absolute temperature, K = 273 + °C

U = Internal energy, kJ

V = Volume, m<sup>3</sup>

m = Mass of gas, kg

## Heat Transfer by Conduction

$$Q = \frac{\lambda A t \Delta T}{d}$$

where Q = heat transferred in joules

$\lambda$  = thermal conductivity or coefficient of heat

transfer in  $\frac{\text{J} \times \text{m}}{\text{m}^2 \times \text{s} \times ^\circ\text{C}}$  or  $\frac{\text{W}}{\text{m} \times ^\circ\text{C}}$

A = area in  $\text{m}^2$

t = time in seconds

$\Delta T$  = temperature difference between surfaces in  $^\circ\text{C}$

d = thickness of layer in m

## COEFFICIENTS OF THERMAL CONDUCTIVITY

Material	Coefficient of Thermal Conductivity W/m $^\circ\text{C}$
Air	0.025
Aluminum	206
Brass	104
Brick	0.6
Concrete	0.85
Copper	380
Cork	0.043
Felt	0.038
Glass	1.0
Glass, fibre	0.04
Iron, cast	70
Plastic, cellular	0.04
Steel	60
Wood	0.15
Wallboard, paper	0.076

## Thermal Expansion of Solids

$$\text{Increase in length} = L \alpha (T_2 - T_1)$$

where  $L$  = original length

$\alpha$  = coefficient of linear expansion

$(T_2 - T_1)$  = rise in temperature

$$\text{Increase in volume} = V \beta (T_2 - T_1)$$

Where  $V$  = original volume

$\beta$  = coefficient of volumetric expansion

$(T_2 - T_1)$  = rise in temperature

coefficient of volumetric expansion = coefficient of linear expansion x 3

$$\beta = 3\alpha$$

### SPECIFIC HEAT and LINEAR EXPANSION OF SOLIDS

Solid	Mean Specific Heat between 0°C and 100°C kJ/kgK or kJ/kg °C	Coefficient of Linear Expansion between 0°C and 100°C (Multiply by 10 <sup>-6</sup> )	Solid	Mean Specific Heat between 0°C and 100°C kJ/kgK or kJ/kg °C	Coefficient of Linear Expansion between 0°C and 100°C (Multiply by 10 <sup>-6</sup> )
Aluminum	0.909	23.8	Iron (cast)	0.544	10.4
Antimony	0.209	17.5	Iron (wrought)	0.465	12.0
Bismuth	0.125	12.4	Lead	0.131	29.0
Brass	0.383	18.4	Nickel	0.452	13.0
Carbon	0.795	7.9	Platinum	0.134	8.6
Cobalt	0.402	12.3	Silicon	0.741	7.8
Copper	0.388	16.5	Silver	0.235	19.5
Glass	0.896	9.0	Steel (mild)	0.494	12.0
Gold	0.130	14.2	Tin	0.230	26.7
Ice (between -20°C and 0°C)	2.135	50.4	Zinc	0.389	16.5

### SPECIFIC HEAT and VOLUME EXPANSION FOR LIQUIDS

Liquid	Specific Heat (at 20° C) kJ/kgK or kJ/kg° C	Coefficient of Volume Expansion (Multiply by 10 <sup>-4</sup> )	Liquid	Specific Heat (at 20°) kJ/kgK or kJ/kg° C	Coefficient of Volume Expansion (Multiply by 10 <sup>-4</sup> )
Alcohol (ethyl)	2.470	11.0	Olive Oil	1.633	
Ammonia	0.473		Petroleum	2.135	
Benzine	1.738	12.4	Gasoline	2.093	12.0
Carbon Dioxide	3.643	1.82	Turpentine	1.800	9.4
Mercury	0.139	1.80	Water	4.183	3.7

### Chemical Heating Value of a Fuel

$$\text{Chemical Heating Value MJ per kg of fuel} = 33.7 C + 144 \left( H_2 - \frac{O_2}{8} \right) + 9.3 S$$

C is the mass of carbon per kg of fuel

H<sub>2</sub> is the mass of hydrogen per kg of fuel

O<sub>2</sub> is the mass of oxygen per kg of fuel

S is the mass of sulphur per kg of fuel

### Theoretical Air Required to Burn Fuel

$$\text{Air (kg per kg of fuel)} = \left[ \frac{8}{3} C + 8 \left( H_2 - \frac{O_2}{8} \right) + S \right] \frac{100}{23}$$

### Air Supplied from Analysis of Flue Gases

$$\text{Air in kg per kg of fuel} = \frac{N_2}{33 (CO_2 + CO)} \times C$$

C is the percentage of carbon in fuel by mass

N<sub>2</sub> is the percentage of nitrogen in flue gas by volume

CO<sub>2</sub> is the percentage of carbon dioxide in flue gas by volume

CO is the percentage of carbon monoxide in flue gas by volume

### Boiler Formulae

$$\text{Equivalent evaporation} = \frac{\dot{m}_s (h_1 - h_2)}{2257 \text{ kJ/kg}}$$

$$\text{Factor of evaporation} = \frac{(h_1 - h_2)}{2257 \text{ kJ/kg}}$$

$$\text{Boiler efficiency} = \frac{\dot{m}_s (h_1 - h_2)}{\dot{m}_f \times \text{calorific value of fuel}}$$

where  $\dot{m}_s$  = mass flow rate of steam

$h_1$  = enthalpy of steam produced in boiler

$h_2$  = enthalpy of feedwater to boiler

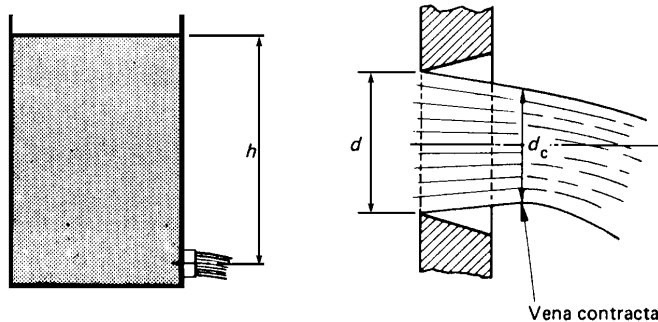
$\dot{m}_f$  = mass flow rate of fuel

## FLUID MECHANICS

### Discharge from an Orifice

$$\begin{aligned}\text{Let } A &= \text{cross-sectional area of the orifice} = (\pi/4)d^2 \\ \text{and } A_c &= \text{cross-sectional area of the jet at the vena contracta} = ((\pi/4) d_c^2) \\ \text{then } A_c &= C_c A \\ \text{or } C_c &= \frac{A_c}{A} = \left(\frac{d_c}{d}\right)^2\end{aligned}$$

where  $C_c$  is the coefficient of contraction



At the vena contracta, the volumetric flow rate  $Q$  of the fluid is given by

$$\begin{aligned}Q &= \text{area of the jet at the vena contracta} \times \text{actual velocity} \\ &= A_c v \\ \text{or } Q &= C_c A C_v \sqrt{2gh}\end{aligned}$$

The coefficients of contraction and velocity are combined to give the coefficient of discharge,  $C_d$

$$\begin{aligned}\text{i.e. } C_d &= C_c C_v \\ \text{and } Q &= C_d A \sqrt{2gh}\end{aligned}$$

Typically, values for  $C_d$  vary between 0.6 and 0.65

$$\text{Circular orifice: } Q = 0.62 A \sqrt{2gh}$$

Where  $Q$  = flow ( $\text{m}^3/\text{s}$ )     $A$  = area ( $\text{m}^2$ )     $h$  = head (m)

$$\text{Rectangular notch: } Q = 0.62 (B \times H) \frac{2}{3} \sqrt{2gh}$$

Where  $B$  = breadth (m)     $H$  = head (m above sill)

$$\text{Triangular Right Angled Notch: } Q = 2.635 H^{5/2}$$

Where  $H$  = head (m above sill)

## Bernoulli's Theory

$$H = h + \frac{P}{w} + \frac{v^2}{2g}$$

H = total head (metres)

w = force of gravity on 1 m<sup>3</sup> of fluid (N)

h = height above datum level (metres)

v = velocity of water (metres per second)

P = pressure (N/m<sup>2</sup> or Pa)

## Loss of Head in Pipes Due to Friction

$$\text{Loss of head in metres} = f \frac{L}{d} \frac{v^2}{2g}$$

L = length in metres

v = velocity of flow in metres per second

d = diameter in metres

f = constant value of 0.01 in large pipes to 0.02 in small pipes

**Note:** This equation is expressed in some textbooks as

Loss =  $4f \frac{L}{d} \frac{v^2}{2g}$  where the f values range from 0.0025 to 0.005

## Actual Pipe Dimensions

Schedule 40 (SI Units)

Nominal Pipe Size (in)	Outside Diameter (mm)	Inside Diameter (mm)	Wall Thickness (mm)	Flow Area (m <sup>2</sup> )
$\frac{1}{8}$	10.3	6.8	1.73	$3.660 \times 10^{-5}$
$\frac{1}{4}$	13.7	9.2	2.24	$6.717 \times 10^{-5}$
$\frac{3}{8}$	17.1	12.5	2.31	$1.236 \times 10^{-4}$
$\frac{1}{2}$	21.3	15.8	2.77	$1.960 \times 10^{-4}$
$\frac{3}{4}$	26.7	20.9	2.87	$3.437 \times 10^{-4}$
1	33.4	26.6	3.38	$5.574 \times 10^{-4}$
$1\frac{1}{4}$	42.2	35.1	3.56	$9.653 \times 10^{-4}$
$1\frac{1}{2}$	48.3	40.9	3.68	$1.314 \times 10^{-3}$
2	60.3	52.5	3.91	$2.168 \times 10^{-3}$
$2\frac{1}{2}$	73.0	62.7	5.16	$3.090 \times 10^{-3}$
3	88.9	77.9	5.49	$4.768 \times 10^{-3}$
$3\frac{1}{2}$	101.6	90.1	5.74	$6.381 \times 10^{-3}$
4	114.3	102.3	6.02	$8.213 \times 10^{-3}$
5	141.3	128.2	6.55	$1.291 \times 10^{-2}$
6	168.3	154.1	7.11	$1.864 \times 10^{-2}$
8	219.1	202.7	8.18	$3.226 \times 10^{-2}$
10	273.1	254.5	9.27	$5.090 \times 10^{-2}$
12	323.9	303.2	10.31	$7.219 \times 10^{-2}$
14	355.6	333.4	11.10	$8.729 \times 10^{-2}$
16	406.4	381.0	12.70	0.1140
18	457.2	428.7	14.27	0.1443
20	508.0	477.9	15.06	0.1794
24	609.6	574.7	17.45	0.2594



## ELECTRICITY

### Ohm's Law

$$I = \frac{E}{R}$$

or  $E = IR$

where  $I$  = current (amperes)  
 $E$  = electromotive force (volts)  
 $R$  = resistance (ohms)

### Conductor Resistivity

$$R = \rho \frac{L}{a}$$

where  $\rho$  = specific resistance (or resistivity) (ohm metres,  $\Omega \cdot m$ )  
 $L$  = length (metres)  
 $a$  = area of cross-section (square metres)

### Temperature correction

$$R_t = R_o (1 + \alpha t)$$

where  $R_o$  = resistance at  $0^\circ\text{C}$  ( $\Omega$ )  
 $R_t$  = resistance at  $t^\circ\text{C}$  ( $\Omega$ )  
 $\alpha$  = temperature coefficient which has an average value for copper of 0.004 28 ( $\Omega/\Omega^\circ\text{C}$ )

$$R_2 = R_1 \frac{(1 + \alpha t_2)}{(1 + \alpha t_1)}$$

where  $R_1$  = resistance at  $t_1$  ( $\Omega$ )  
 $R_2$  = resistance at  $t_2$  ( $\Omega$ )

$\alpha$ Values	$\Omega/\Omega^\circ\text{C}$
copper	0.00428
platinum	0.00385
nickel	0.00672
tungsten	0.0045
aluminum	0.0040

## Dynamo Formulae

$$\text{Average e.m.f. generated in each conductor} = \frac{2\Phi N p Z}{60c}$$

where  $Z$  = total number of armature conductors

$c$  = number of parallel paths through winding between positive and negative brushes

where  $c = 2$  (wave winding),  $c = 2p$  (lap winding)

$\Phi$  = useful flux per pole (webers), entering or leaving the armature

$p$  = number of pairs of poles

$N$  = speed (revolutions per minute)

$$\text{Generator Terminal volts} = E_G - I_a R_a$$

$$\text{Motor Terminal volts} = E_B + I_a R_a$$

where  $E_G$  = generated e.m.f.

$E_B$  = generated back e.m.f.

$I_a$  = armature current

$R_a$  = armature resistance

## Alternating Current

R.M.S. value of sine curve = 0.707 maximum value

Mean value of sine curve = 0.637 maximum value

$$\text{Form factor of sinusoidal} = \frac{\text{R.M.S. value}}{\text{Mean value}} = \frac{0.707}{0.637} = 1.11$$

$$\text{Frequency of alternator} = \frac{pN}{60} \text{ cycles per second}$$

Where  $p$  = number of pairs of poles

$N$  = rotational speed in r/min

### Slip of Induction Motor

$$\frac{\text{Slip speed of field - speed of rotor}}{\text{Speed of field}} \times 100$$

### Inductive Reactance

$$\text{Reactance of AC circuit (X)} = 2\pi fL \text{ ohms}$$

where L = inductance of circuit (henries)

$$\text{Inductance of an iron cored solenoid} = \frac{1.256T^2\mu A}{L \times 10^8} \text{ henries}$$

where T = turns on coil

$\mu$  = magnetic permeability of core

A = area of core (square centimetres)

L = length (centimetres)

### Capacitance Reactance

$$\text{Capacitance reactance of AC circuit} = \frac{1}{2\pi fC} \text{ ohms}$$

where C = capacitance (farads)

$$\text{Total reactance} = \left( 2\pi fL - \frac{1}{2\pi fC} \right) \text{ ohms}$$

$$\begin{aligned} \text{Impedance (Z)} &= \sqrt{(\text{resistance})^2 + (\text{reactance})^2} \\ &= \sqrt{R^2 + \left( 2\pi fL - \frac{1}{2\pi fC} \right)^2} \text{ ohms} \end{aligned}$$

### Current in AC Circuit

$$\text{Current} = \frac{\text{impressed volts}}{\text{impedance}}$$

## Power Factor

$$\text{p.f.} = \frac{\text{true watts}}{\text{volts} \times \text{amperes}}$$

also  $\text{p.f.} = \cos \Phi$ , where  $\Phi$  is the angle of lag or lead

## Three Phase Alternators

Star connected

$$\text{Line voltage} = \sqrt{3} \times \text{phase voltage}$$

$$\text{Line current} = \text{phase current}$$

Delta connected

$$\text{Line voltage} = \text{phase voltage}$$

$$\text{Line current} = \sqrt{3} \times \text{phase current}$$

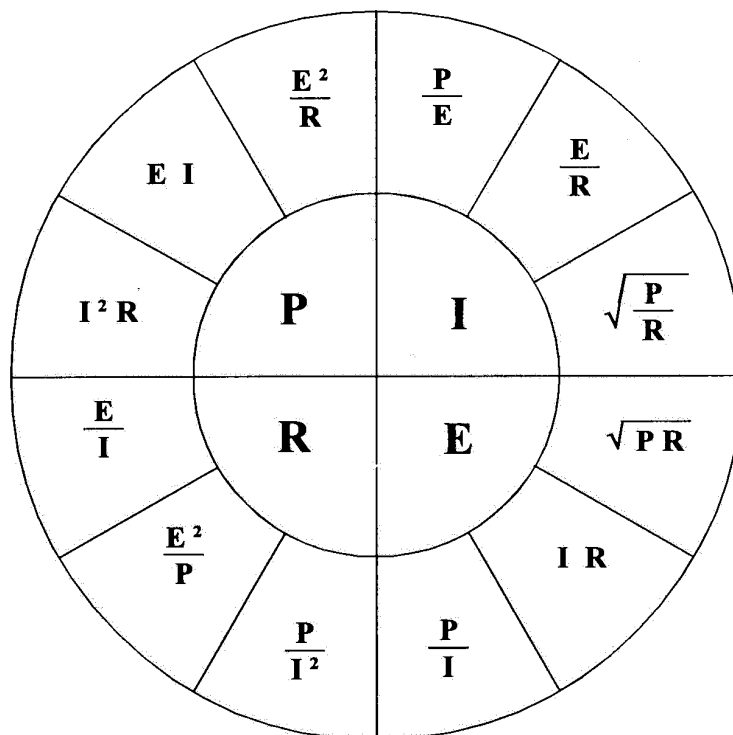
Three phase power

$$P = \sqrt{3} E_L I_L \cos \Phi$$

$$E_L = \text{line voltage}$$

$$I_L = \text{line current}$$

$$\cos \Phi = \text{power factor}$$



Noble Gases

**PERIODIC TABLE OF THE ELEMENTS**

Group	1 IA	2 IIA	3 IIIB	4 IVB	5 VB	6 VIB	7 VIIB	8 VIII B	9 VIII B	10 VIII B	11 IB	12 IIB	13 IIIA	14 IVA	15 VA	16 VIA	17 VIIA	18 VIIIA				
	1 H 1.008	Alkaline Earth Metals ↓ 2 He 4.003	Halogens ↓																			
	3 Li 6.941	4 Be 9.012	Transition Metals																			
	11 Na 22.99	12 Mg 24.31	Alkali Metals																			
	19 K 39.10	20 Ca 40.08	21 Sc 44.96	22 Ti 47.88	23 V 50.94	24 Cr 52.00	25 Mn 54.94	26 Fe 55.85	27 Co 58.93	28 Ni 58.69	29 Cu 63.55	30 Zn 65.38	31 Ga 69.72	32 Ge 72.59	33 As 74.92	34 Se 78.96	35 Br 79.90	36 Kr 83.80				
	37 Rb 85.47	38 Sr 87.62	39 Y 88.91	40 Zr 91.22	41 Nb 92.91	42 Mo 95.94	43 Tc (98)	44 Ru 101.1	45 Rh 102.9	46 Pd 106.4	47 Ag 107.9	48 Cd 112.4	49 In 114.8	50 Sn 118.7	51 Sb 121.8	52 Te 127.6	53 I 126.9	54 Xe 131.3				
	55 Cs 132.9	56 Ba 137.3	57 La* 138.9	72 Hf 178.5	73 Ta 180.9	74 W 183.9	75 Re 186.2	76 Os 190.2	77 Ir 192.2	78 Pt 195.1	79 Au 197.0	80 Hg 200.6	81 Tl 204.4	82 Pb 207.2	83 Bi 209.0	84 Po (209)	85 At (210)	86 Rn (222)				
	87 Fr (223)	88 Ra 226	89 Ac* (227)	104 Unq	105 Unp	106 Unh	107 Uns	108 Uno	109 Une	metals ←									→ nonmetals			
				58 Ce 140.1	59 Pr 140.9	60 Nd 144.2	61 Pm (145)	62 Sm 150.4	63 Eu 152.0	64 Gd 157.3	65 Tb 158.9	66 Dy 162.5	67 Ho 164.9	68 Er 167.3	69 Tm 168.9	70 Yb 173.0	71 Lu 175.0					
				90 Th 232.0	91 Pa (231)	92 U 238.0	93 Np (237)	94 Pu (244)	95 Am (243)	96 Cm (247)	97 Bk (247)	98 Cf (251)	99 Es (252)	100 Fm (257)	101 Md (258)	102 No (259)	103 Lr (260)					
				* Lanthanides			* Actinides															

## ION NAMES AND FORMULAE

### MONATOMIC

$\text{Ag}^+$	silver ion
$\text{Al}^{3+}$	aluminum ion
$\text{Au}^+$ and $\text{Au}^{2+}$	gold ion
$\text{Be}^{2+}$	beryllium ion
$\text{Ca}^{2+}$	calcium ion
$\text{Co}^{2+}$ and $\text{Co}^{3+}$	cobalt ion
$\text{Cr}^{2+}$ and $\text{Cr}^{3+}$	chromium ion
$\text{Cu}^+$ and $\text{Cu}^{2+}$	copper ion
$\text{Fe}^{2+}$ and $\text{Fe}^{3+}$	iron ion
$\text{K}^+$	potassium ion
$\text{Li}^+$	lithium ion
$\text{Mg}^{2+}$	magnesium ion
$\text{Na}^+$	sodium ion
$\text{Zn}^{2+}$	zinc ion

### POLYATOMIC

$\text{BO}_3^{3-}$	borate ion
$\text{C}_2\text{H}_3\text{O}_2^-$	acetate ion
$\text{ClO}^-$	hypochlorite ion
$\text{ClO}_2^-$	chlorite ion
$\text{ClO}_3^-$	chlorate ion
$\text{ClO}_4^-$	perchlorate ion
$\text{CN}^-$	cyanide ion
$\text{CO}_3^{2-}$	carbonate ion
$\text{C}_2\text{O}_4^{2-}$	oxalate ion
$\text{CrO}_4^{2-}$	chromate ion
$\text{Cr}_2\text{O}_7^{2-}$	dichromate ion
$\text{HCO}_3^-$	hydrogen carbonate or bicarbonate ion
$\text{H}_3\text{O}^+$	hydronium ion
$\text{HPO}_4^{2-}$	hydrogen phosphate ion
$\text{H}_2\text{PO}_4^-$	dihydrogen phosphate ion
$\text{HSO}_3^-$	hydrogen sulphite or bisulphite ion
$\text{HSO}_4^-$	hydrogen sulphate or bisulphate ion
$\text{MnO}_4^-$	permanganate ion
$\text{N}_3^-$	azide ion
$\text{NH}_4^+$	ammonium ion
$\text{NO}_2^-$	nitrite ion
$\text{NO}_3^-$	nitrate ion
$\text{O}_2^{2-}$	peroxide ion
$\text{OCN}^-$	cyanate ion
$\text{OH}^-$	hydroxide ion
$\text{PO}_3^{3-}$	phosphite ion
$\text{PO}_4^{3-}$	phosphate ion
$\text{SCN}^-$	thiocyanate ion
$\text{SO}_3^{2-}$	sulphite ion
$\text{SO}_4^{2-}$	sulphate ion
$\text{S}_2\text{O}_3^{2-}$	thiosulphate ion













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