King Fahd University of Petroleum and Minerals
College of Computer Sciences and Engineering
Department of Computer Engineering

COE 308 – Computer Architecture (T032)

Homework # 04 (SOLUTION)

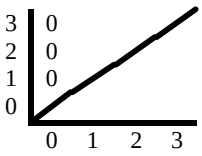
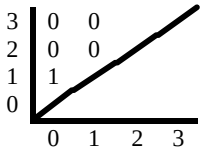
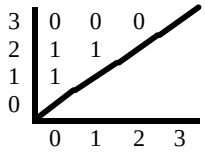
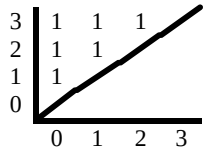
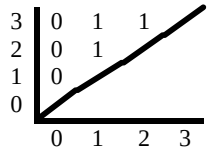
Problem # 1: Solve problem 3.14 from the textbook.

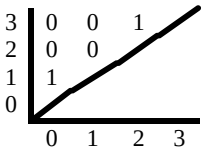
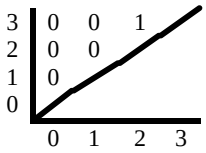
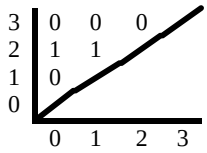
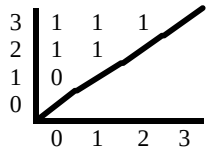
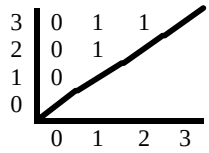
Solution:

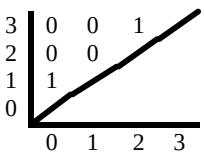
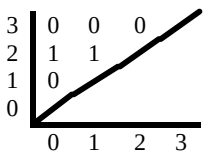
Address Tag	Hit/Miss	C_0	C_1	C_2	C_3	Subsequent actions
Initialization		0	0	0	0	
2	Miss	0	1	1	1	Block 0 filled
6	Miss	1	0	2	2	Block 1 filled
9	Miss	2	1	0	3	Block 2 filled
7	Miss	3	2	1	0	Block 3 filled
2	Hit	0	3	2	1	Block 0 accessed
3	Miss	1	0	3	2	Block 1 replaced
2	Hit	0	1	3	2	Block 0 accessed
9	Hit	1	2	0	3	Block 2 accessed
6	Miss	2	3	1	0	Block 3 replaced
2	Hit	0	3	2	1	Block 0 accessed
7	Miss	1	0	3	2	Block 1 replaced
4	Miss	2	1	0	3	Block 2 replaced

Problem # 2: Solve problem 3.15 from the textbook.

Solution: F = Fill, A = Access, R = Replace

TAG	**2**	**6**	**9**	**7**	**2**
Block	**0**	**1**	**2**	**3**	**0**
					
Comment	**F**	**F**	**F**	**F**	**A**
LRU Blk			**3**	**0**	**1**

TAG	**3**	**2**	**9**	**6**	**2**
Block	**1**	**0**	**2**	**3**	**0**
					
Comment	**R**	**A**	**A**	**R**	**A**
LRU Blk	**2**	**2**	**3**	**1**	**1**

TAG	**7**	**4**
Block	**1**	**2**
		
Comment	**R**	**R**
LRU Blk	**2**	**3**

Problem # 3: Consider a 4 × 8 array of numbers, A. Assume that each number in the array occupies one word in MM and that the array elements are stored **column-major** in MM starting from location 1008 to location 1039. The cache consists of 8 blocks each consisting of just two words. The cache is initially empty. Assume also that whenever needed, LRU replacement policy is used. Analyze the cache for the following segment of a program:

```
sum = 0;
For i = 0 to 1
        For j = 0 to 7
                sum = sum + A(i, j)
        EndFor
EndFor
```

Fill out the following assuming (i) direct mapping, then (ii) fully associative mapping. Also, calculate the hit ratio, the number of block replacements, and the percentage of cache utilization in each case.

Solution:

(i) Direct Mapping – locations 1008 & 1009 map to cache block number 0 (i.e. MM will be divided into blocks of 2 with 1008 & 1009 having block # 504 that maps to block (504 mod 8) = block 0 in cache)

Request	Cache Hit/ Miss	MM Address	Cache Block number	Cache Content													
				B0		B1		B2		B3		B4		B5		B6		B7	
A(0, 0)	Miss	1008	0	00	10														
A(0, 1)	Miss	1012	2	00	10			01	11										
A(0, 2)	Miss	1016	4	00	10			01	11			02	12						
A(0, 3)	Miss	1020	6	00	10			01	11			02	12			03	13		
A(0, 4)	Miss	1024	0	04	14			01	11			02	12			03	13		
A(0, 5)	Miss	1028	2	04	14			05	15			02	12			03	13		
A(0, 6)	Miss	1032	4	04	14			05	15			06	16			03	13		
A(0, 7)	Miss	1036	6	04	14			05	15			06	16			07	17		
A(1, 0)	Miss	1009	0	00	10			05	15			06	16			07	17		
A(1, 1)	Miss	1013	2	00	10			01	11			06	16			07	17		
A(1, 2)	Miss	1017	4	00	10			01	11			02	12			07	17		
A(1, 3)	Miss	1021	6	00	10			01	11			02	12			03	13		
A(1, 4)	Miss	1025	0	04	14			01	11			02	12			03	13		
A(1, 5)	Miss	1029	2	04	14			05	15			02	12			03	13		
A(1, 6)	Miss	1033	4	04	14			05	15			06	16			03	13		
A(1, 7)	Miss	1037	6	04	14			05	15			06	16			07	17		

Hit ratio = 0 / 16 = 0, **# block replacements** = 12 (shaded areas in the table), **Cache utilization%** = 4 / 8 = 50%

(ii) Fully Associative Mapping

Request	Cache Hit/ Miss	MM Addr.	Cache Block number	Cache Content															
				B0		B1		B2		B3		B4		B5		B6		B7	
A(0, 0)	Miss	1008	0	00	10														
A(0, 1)	Miss	1012	1	00	10	01	11												
A(0, 2)	Miss	1016	2	00	10	01	11	02	12										
A(0, 3)	Miss	1020	3	00	10	01	11	02	12	03	13								
A(0, 4)	Miss	1024	4	00	10	01	11	02	12	03	13	04	14						
A(0, 5)	Miss	1028	5	00	10	01	11	02	12	03	13	04	14	05	15				
A(0, 6)	Miss	1032	6	00	10	01	11	02	12	03	13	04	14	05	15	06	16		
A(0, 7)	Miss	1036	7	00	10	01	11	02	12	03	13	04	14	05	15	06	16	07	17
A(1, 0)	*Hit*	1009	0	00	10	01	11	02	12	03	13	04	14	05	15	06	16	07	17
A(1, 1)	*Hit*	1013	1	00	10	01	11	02	12	03	13	04	14	05	15	06	16	07	17
A(1, 2)	*Hit*	1017	2	00	10	01	11	02	12	03	13	04	14	05	15	06	16	07	17
A(1, 3)	*Hit*	1021	3	00	10	01	11	02	12	03	13	04	14	05	15	06	16	07	17
A(1, 4)	*Hit*	1025	4	00	10	01	11	02	12	03	13	04	14	05	15	06	16	07	17
A(1, 5)	*Hit*	1029	5	00	10	01	11	02	12	03	13	04	14	05	15	06	16	07	17
A(1, 6)	*Hit*	1033	6	00	10	01	11	02	12	03	13	04	14	05	15	06	16	07	17
A(1, 7)	*Hit*	1037	7	00	10	01	11	02	12	03	13	04	14	05	15	06	16	07	17

Hit ratio = 8 / 16 = 0.5, **# block replacements** = 0, **Cache utilization%** = 8 / 8 = 100%