## KFUPM - COMPUTER ENGINEERING DEPARTMENT <br> COE-540 - Computer Networks <br> Quiz 03 - Due March 11 ${ }^{\text {th }}, 2015$ - Take home quiz

## Student Name: <br> Student Number:

a) The transmitted frame is $T(X)=X^{13}+X^{12}+X^{10}+X^{8}+X^{7}+X^{6}+X^{5}+X^{4}+X$
b) The division is shown - Note that the division shown produce a ZERO remainder.


Division of $T(X)$ by $G(X)$ using binary representation


Division of $T(X)$ by $G(X)$ using polynomial representation
c) The error syndrome is given by 00100000000100 or $E(X)=X^{11}+X^{2}$

The received frame is $T_{R}(X)=T(X)+E(X)=X^{13}+X^{12}+X^{11}+X^{10}+X^{8}+X^{7}+X^{6}+X^{5}+X^{4}+$ $X^{2}+X$ or $11 \underline{1} 10111110 \underline{110}$. The underlined bits are the ones affected by the error.
d) The division of the received frame $T R(X)$ by $G(X)$ is as shown. Note the division produces a remainder and therefore, the


Division of $T R(X)$ by $G(X)$ using binary representation

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Note that the division process may be done in binary as shown or using the polynomial representation (easier to follow!) - Division in ONE representation form is required ONLY.

Note that the remainder of the division is $X^{\wedge} 3+X$ which is the bit pattern 1010

March $10^{\text {th }}, 2015$

|  |  |  |  |  |  |  | x^9 | x^8 | X^7 |  |  | x^4 |  | x^2 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| x^4 | $\times$ | 1 | $\times^{\wedge 13}$ | $\mathrm{x}^{\wedge} 12$ | $\chi^{\wedge} 11$ | $\mathrm{x}^{\wedge 10}$ |  | ${ }^{\times \wedge}$ | $\times^{\wedge} 7$ | ${ }^{\times n} 6$ | x^5 | $\times^{\wedge} 4$ |  | $\mathrm{x}^{2}$ | $\times$ |
|  |  |  | $\times^{\wedge 13}$ |  |  | x^10 | x^9 |  |  |  |  |  |  |  |  |
|  |  |  |  | x^12 | x^11 |  | x^9 | x^8 | X^7 | ${ }^{\times \times 6}$ | ${ }^{\times 5}$ | x^4 |  | ${ }^{\text {^2 }}$ | x |
|  |  |  |  | $\mathrm{x}^{\wedge} 12$ |  |  | x^9 | x^8 |  |  |  |  |  |  |  |
|  |  |  |  |  | $\chi^{\wedge 11}$ |  |  |  | x^7 | ${ }^{\times \times 6}$ | $\times \times 5$ | $\times^{\wedge 4}$ |  | $\times^{\wedge}$ | $\times$ |
|  |  |  |  |  | $\chi^{\wedge 11}$ |  |  | x^8 | x^7 |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  | x^8 |  | ${ }^{\times \times 6}$ | $\times^{\wedge 5}$ | $\times^{\wedge 4}$ |  | ${ }^{\times \wedge}$ | $x$ |
|  |  |  |  |  |  |  |  | x^8 |  |  | ${ }^{\times 5}$ | x^4 |  |  |  |
|  |  |  |  |  |  |  |  |  |  | ${ }^{\times \wedge}$ |  |  |  | x^2 | $\times$ |
|  |  |  |  |  |  |  |  |  |  | ${ }^{\times \times 6}$ |  |  | $\mathrm{x}^{\wedge}$ | ${ }^{\wedge}{ }^{2}$ |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  | $x^{\wedge} 3$ |  | $\times$ |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

Division of $T R(X)$ by $G(X)$ using polynomial representation

