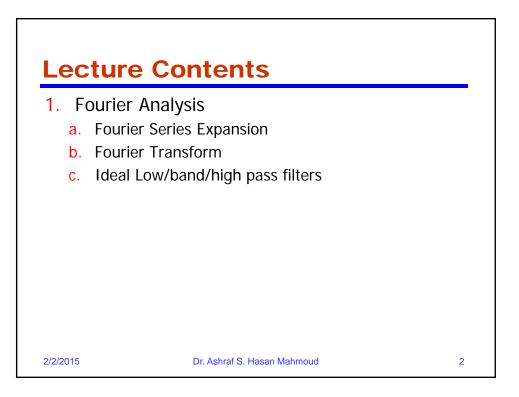
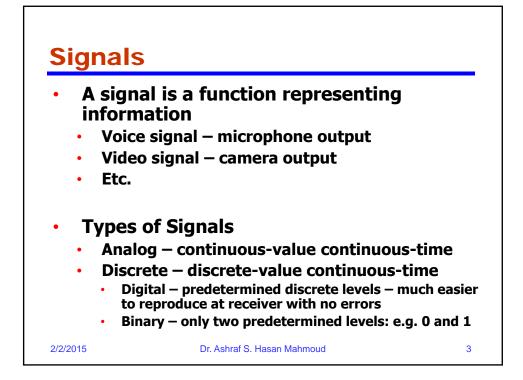
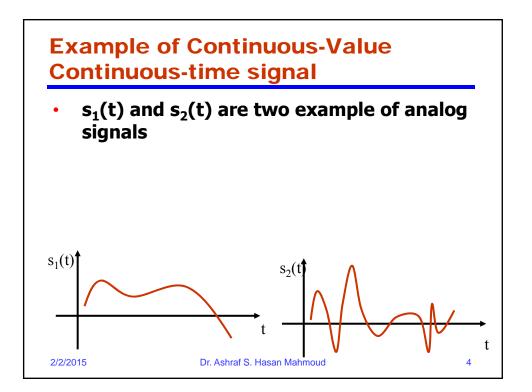
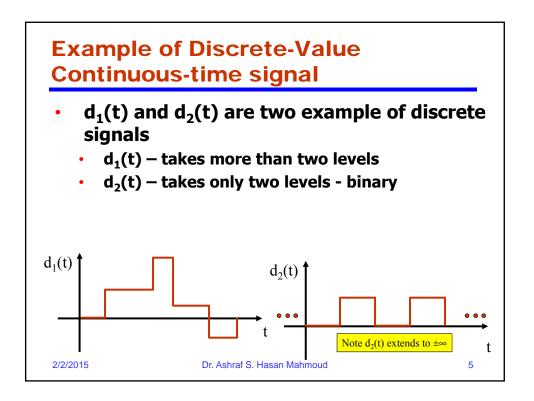
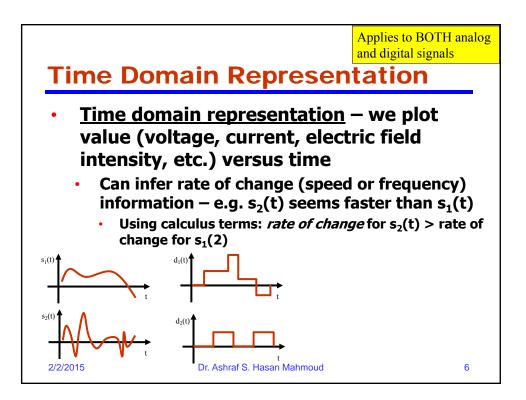
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Computer Engineering Dept			
COE 54 Term 1	0 –Computer Network 42	(S	
Dr. Ash	raf S. Hasan Mahmou	d	
Rm 22-4	420		
Ext. 17	24		
Email: a	ashraf@kfupm.edu.sa		
2/2/2015	Dr. Ashraf S. Hasan Mahmoud	1	

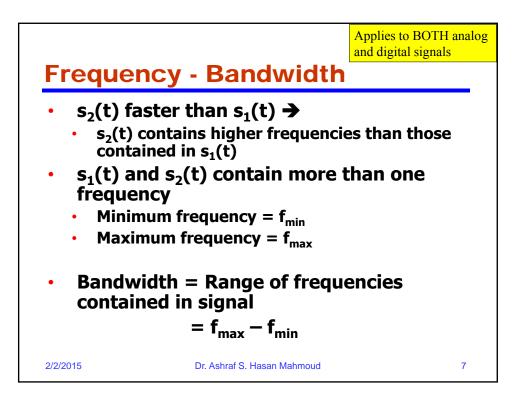


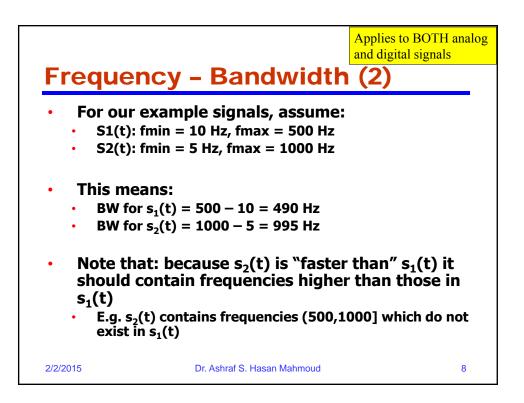


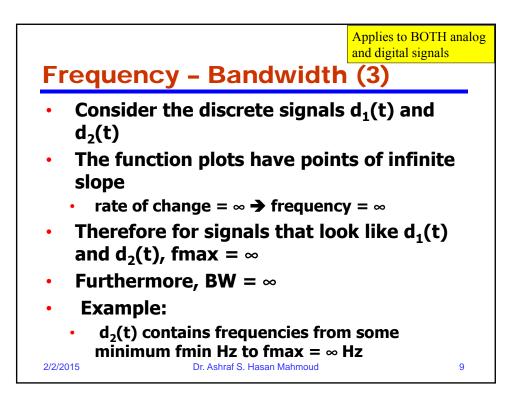


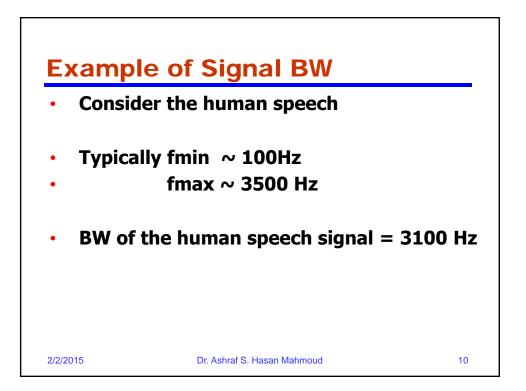


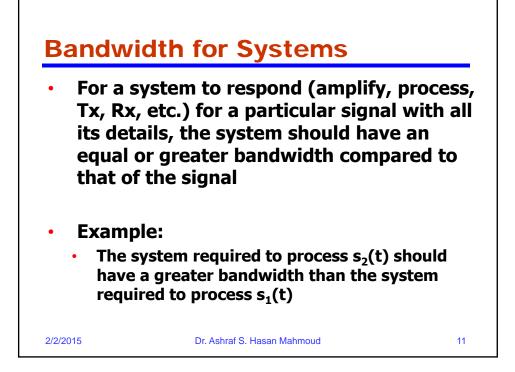


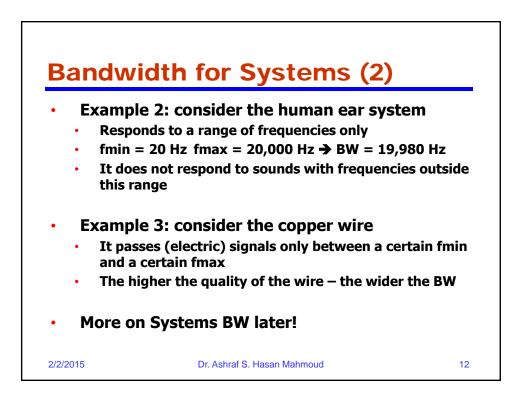


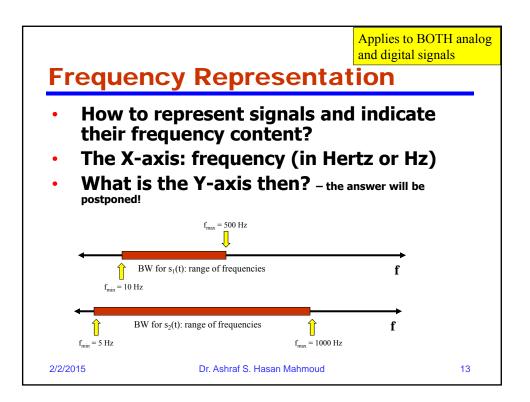


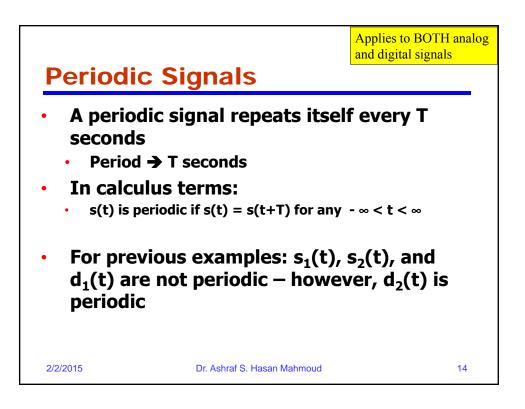


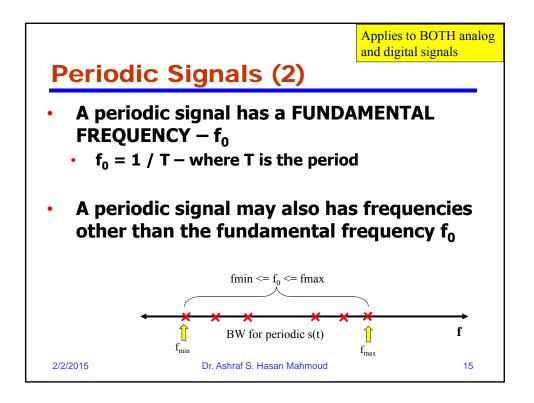


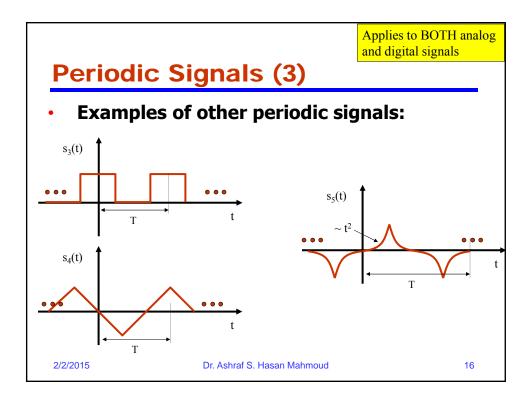


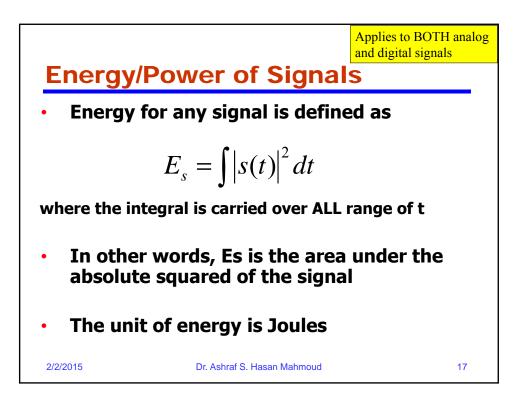


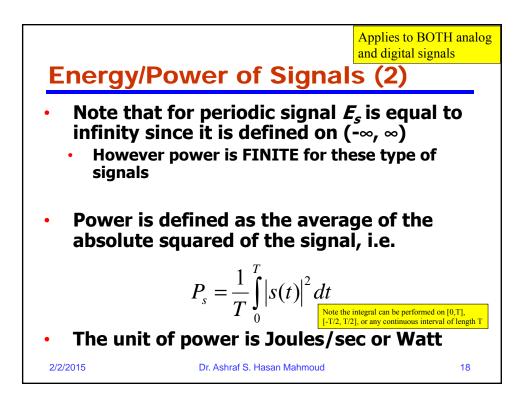


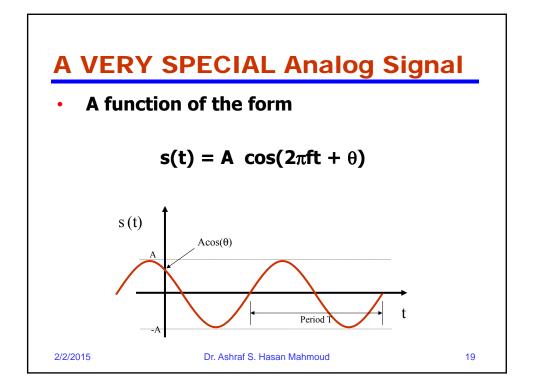


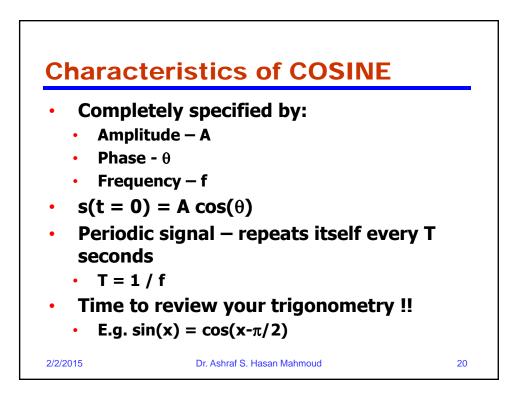


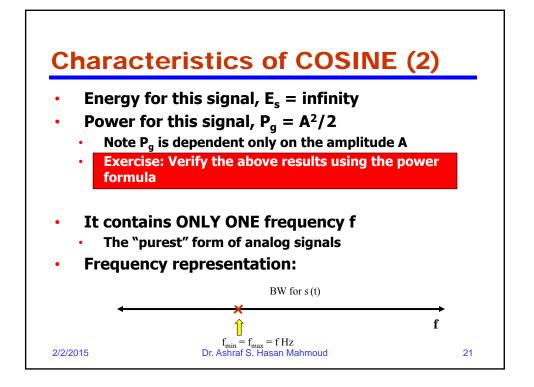




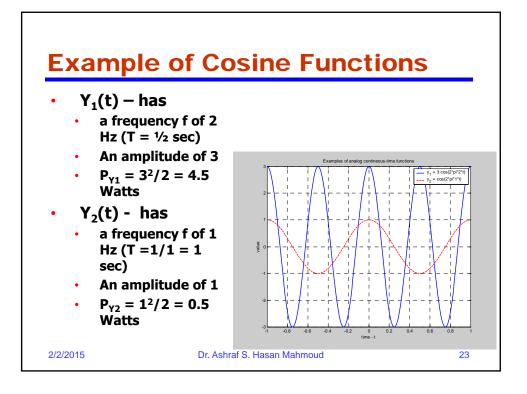


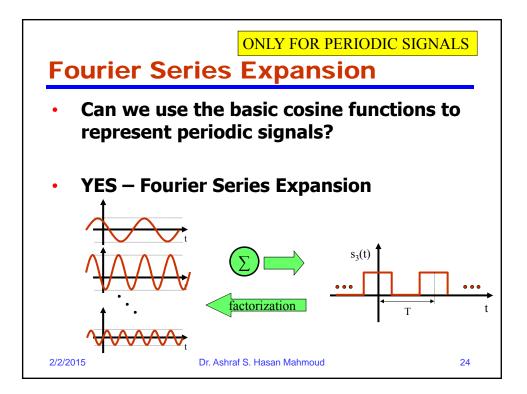


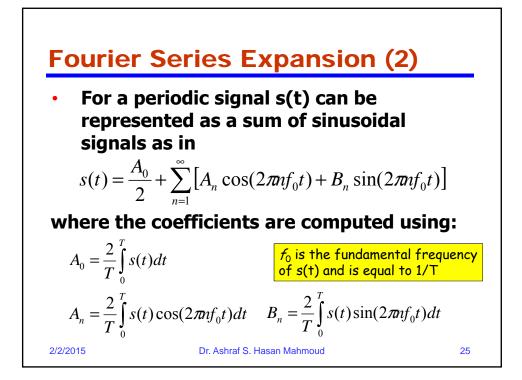


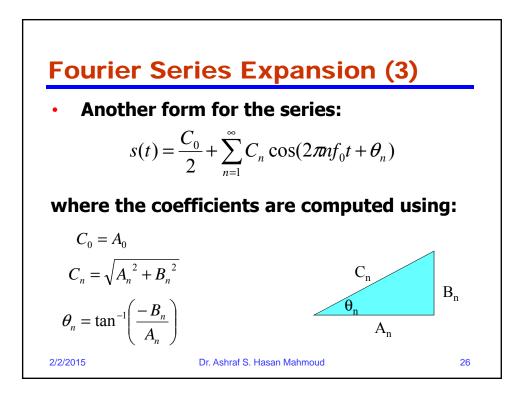


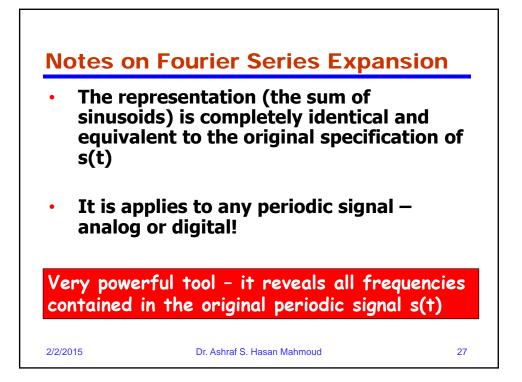
$$\begin{aligned}
\textbf{Characteristics of COSINE (3)}\\
\textbf{J} = (1 + 1)^{T} \\
\textbf{J} = (1 +$$

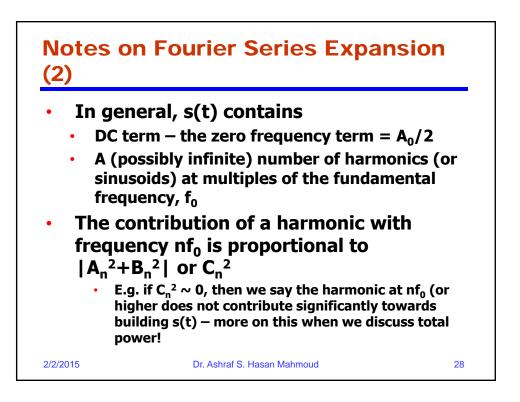


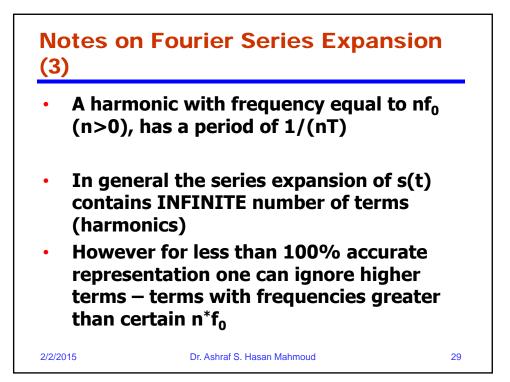


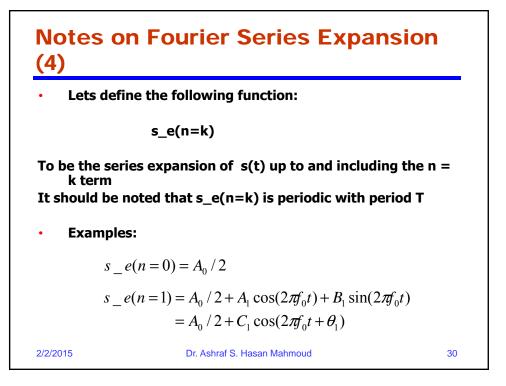


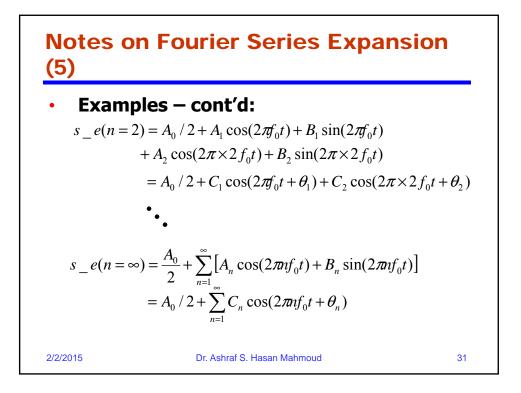


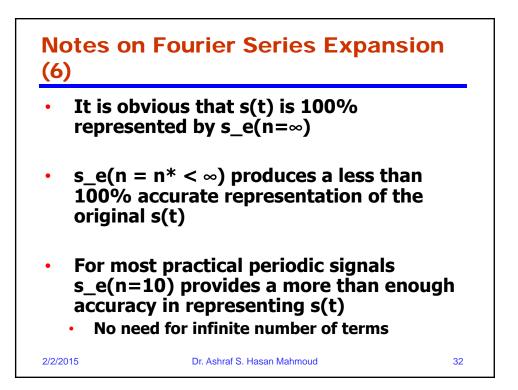


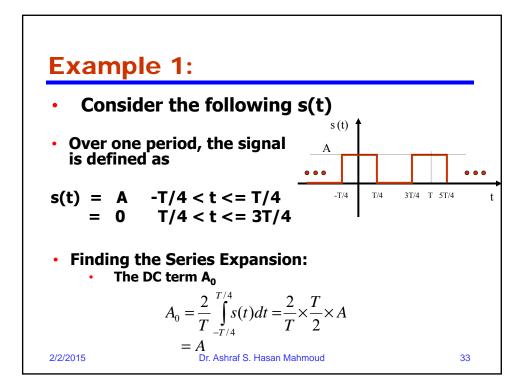


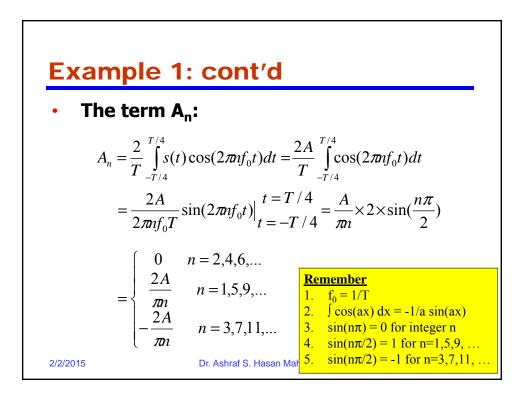


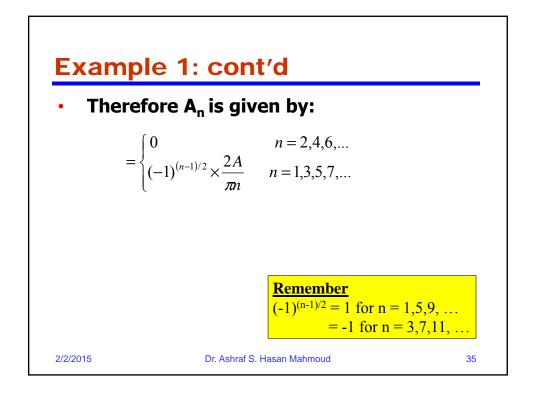


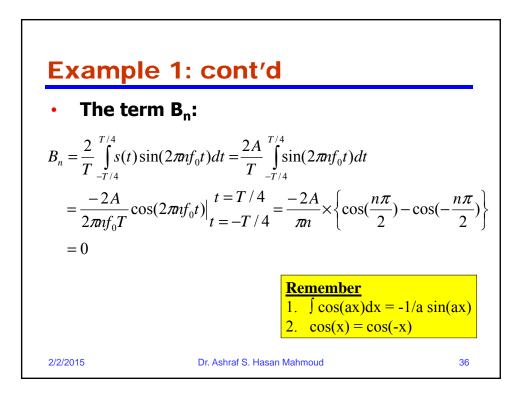














• Therefore, the overall series expansion is given by

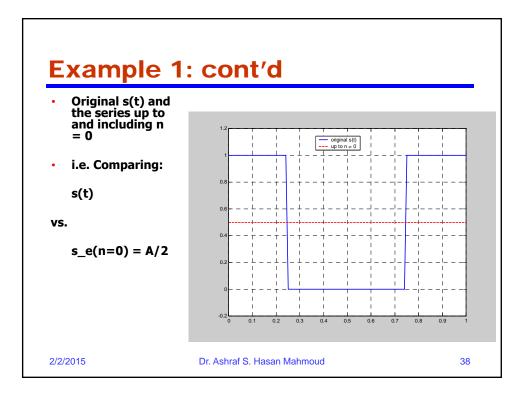
$$s(t) = \frac{A}{2} + \frac{2A}{\pi} \sum_{n=1,3,5}^{\infty} \frac{(-1)^{(n-1)/2}}{n} \times \cos(2\pi n f_0 t)$$

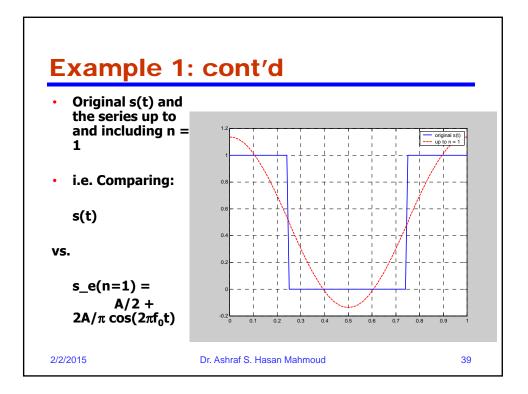
$$s(t) = \frac{A}{2} + \frac{2A}{\pi} \times \cos(2\pi f_0 t) - \frac{2A}{3\pi} \cos(2\pi \times 3f_0 t) + \frac{2A}{5\pi} \times \cos(2\pi \times 5f_0 t) - \frac{2A}{7\pi} \cos(2\pi \times 7f_0 t) + \dots$$

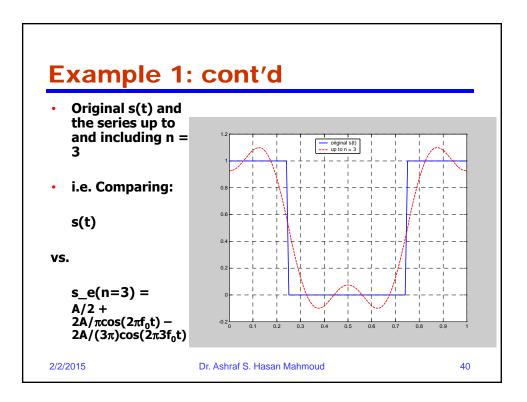
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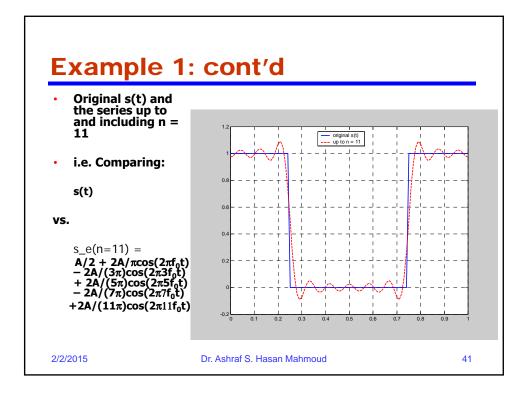
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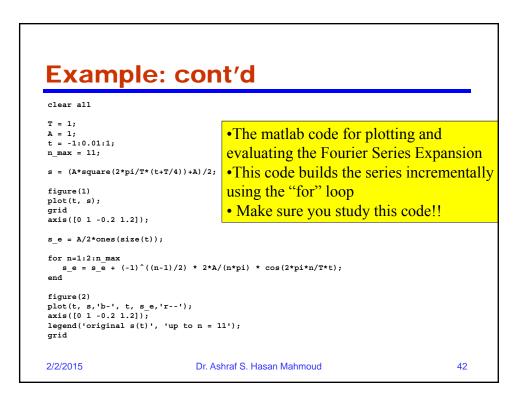
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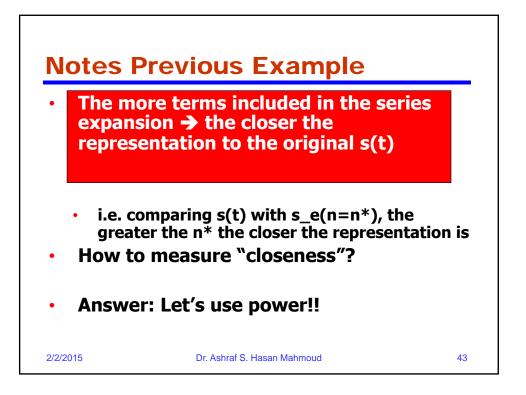


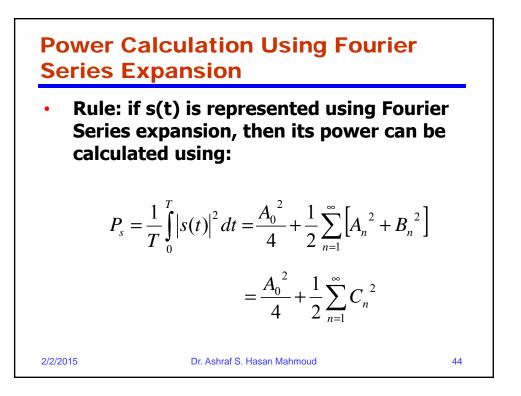


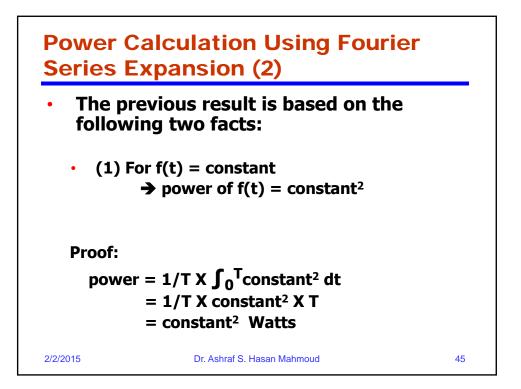


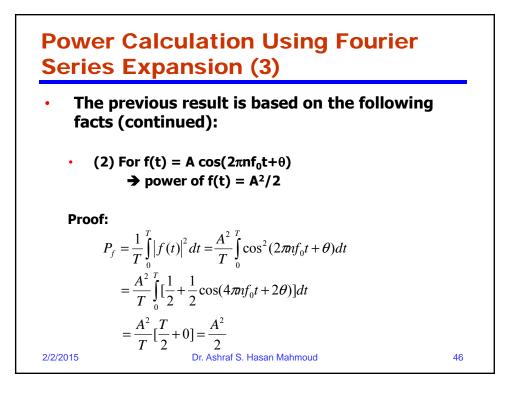












## Example 2:

 Problem: What is the power of the signal s(t) used in previous example? And find n\* such that the power contained in s\_e(n=n\*) is 95% of that existing in s(t)?

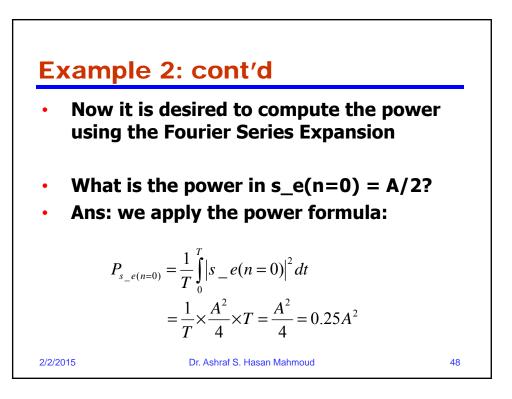
• Solution: Let the power of s(t) be given by  $P_s$ 

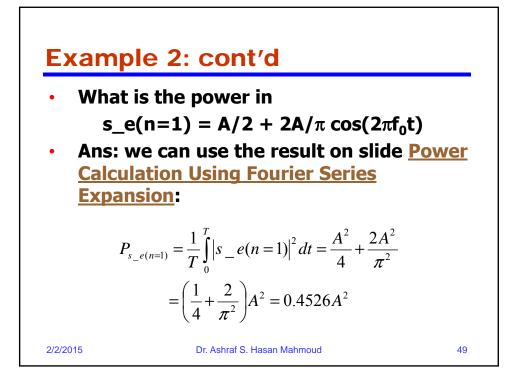
$$P_{s} = \frac{1}{T} \int_{0}^{T} |s(t)|^{2} dt = \frac{1}{T} \times A^{2} \times \frac{T}{2} = \frac{A^{2}}{2} = 0.5A^{2}$$

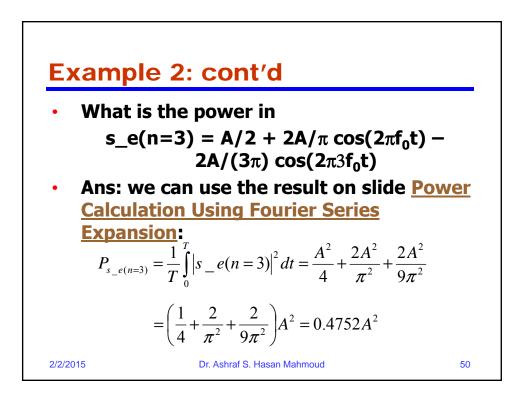
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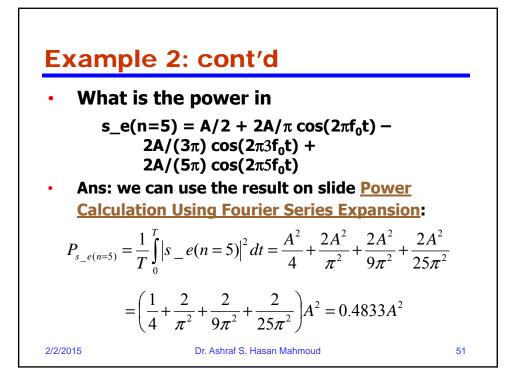
47

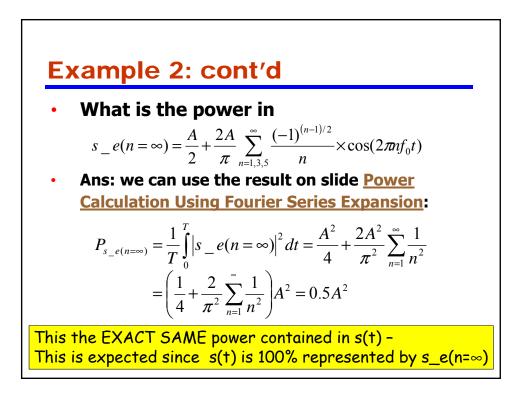
2/2/2015



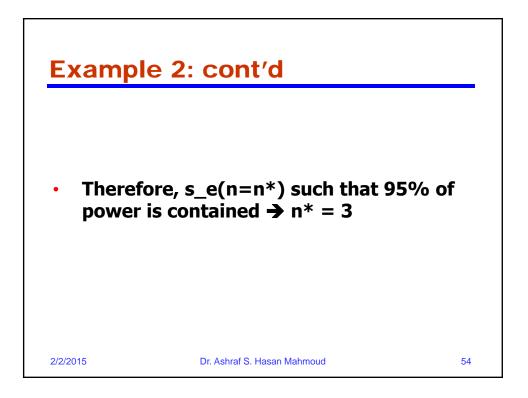


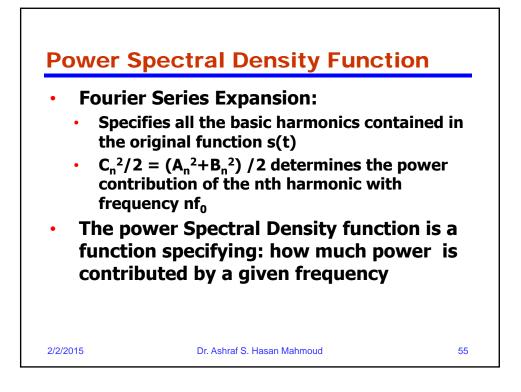


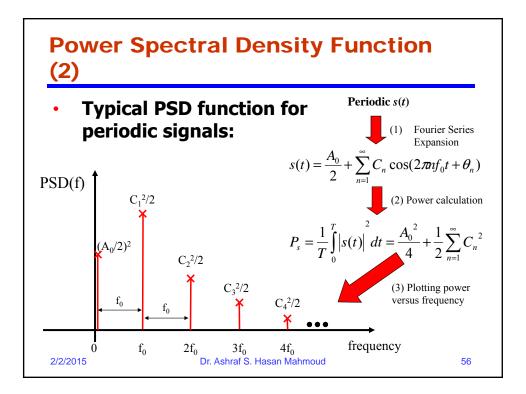


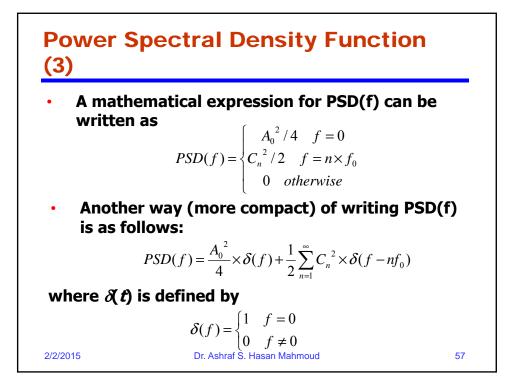


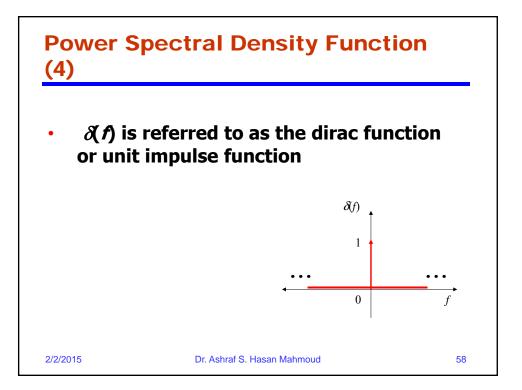
s_e(n=k)	Expression	Power	% Power+
k = 0	A/2	0.25 A <sup>2</sup>	$(0.25A^2)/(0.5A^2)$ = 50%
k = 1	$A/2 + 2A/\pi \cos(2\pi f_0 t)$	0.4526 A <sup>2</sup>	$(0.4526A^2)/(0.5A^2)$ = 90.5%
k = 2*	$A/2 + 2A/\pi \cos(2\pi f_0 t)$	0.4526 A <sup>2</sup>	90.5%
k = 3	$A/2 + 2A/\pi cos(2\pi f_0 t) - 2A/(3\pi) cos(2\pi 3f_0 t)$	0.4752 A <sup>2</sup>	95.0%
k = 5	$A/2 + 2A/\pi cos(2\pi f_0 t) - 2A/(3\pi)cos(2\pi 3f_0 t) + 2A/(5\pi)cos(2\pi 5f_0 t)$	0.4833 A <sup>2</sup>	96.7%

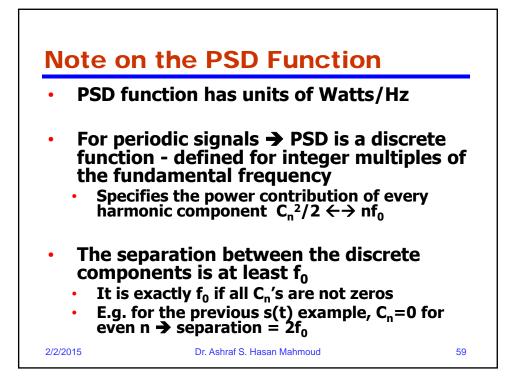


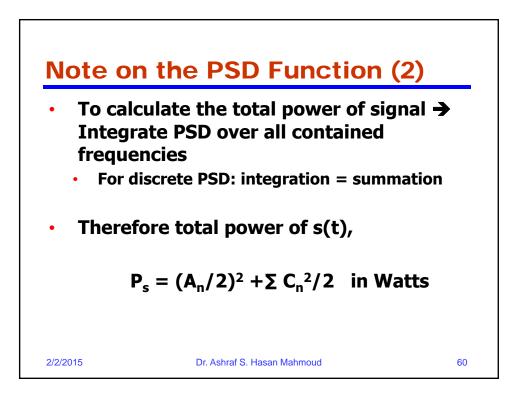


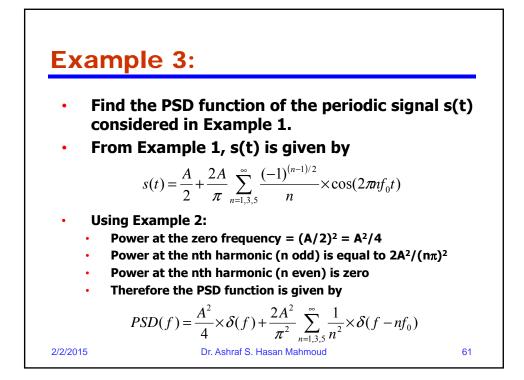


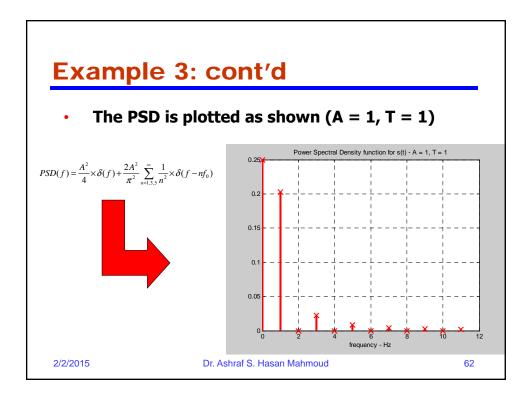


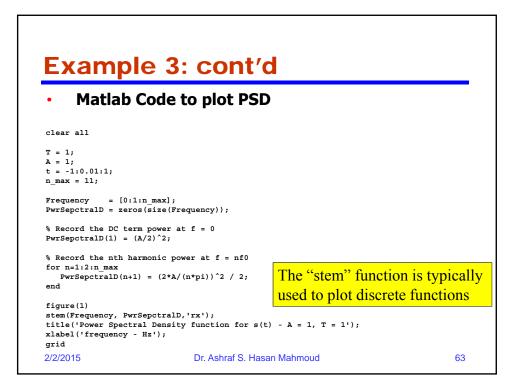


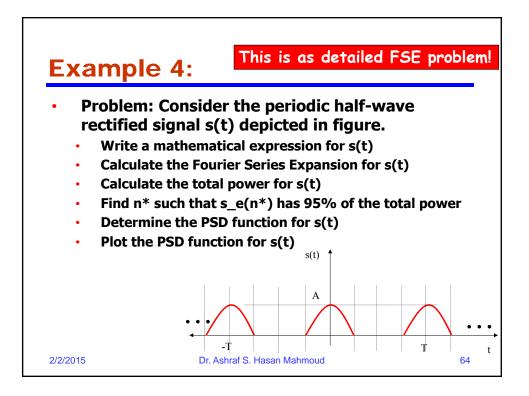


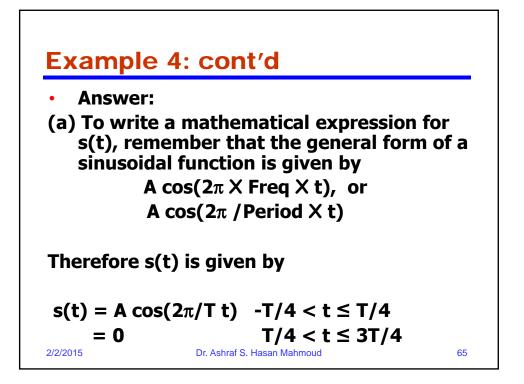


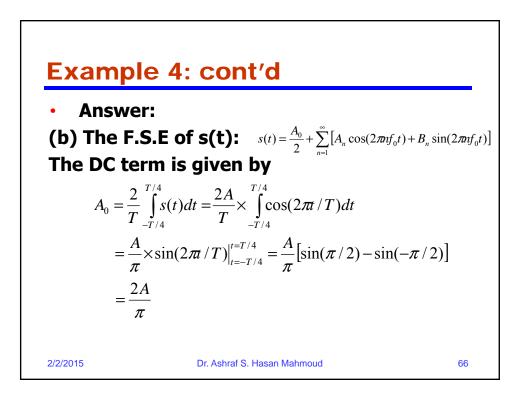


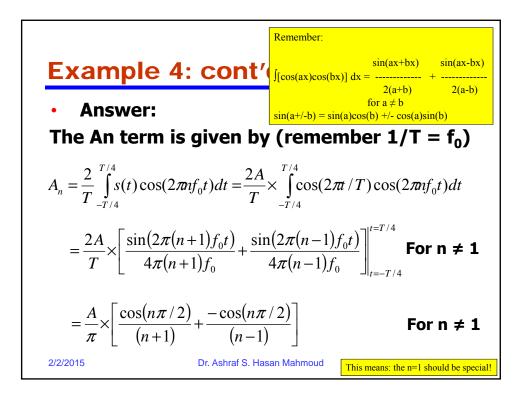


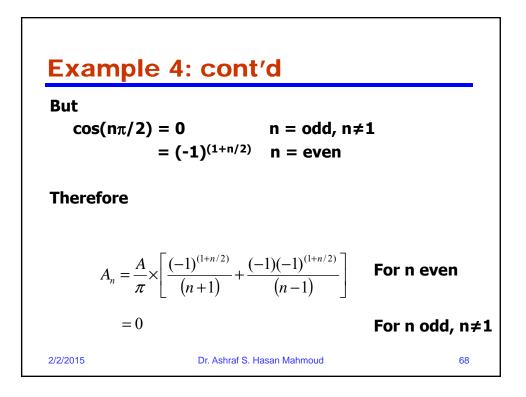


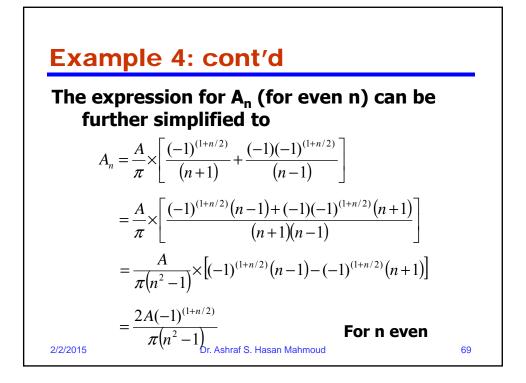


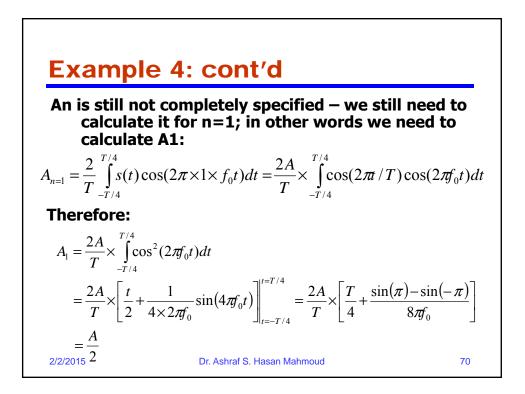


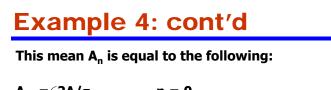


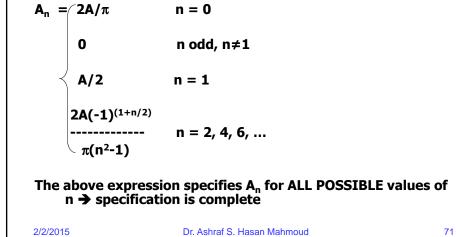


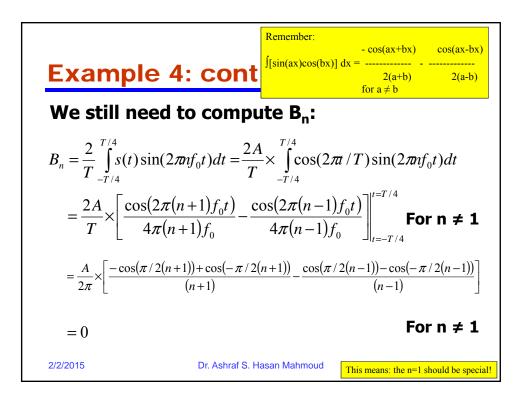


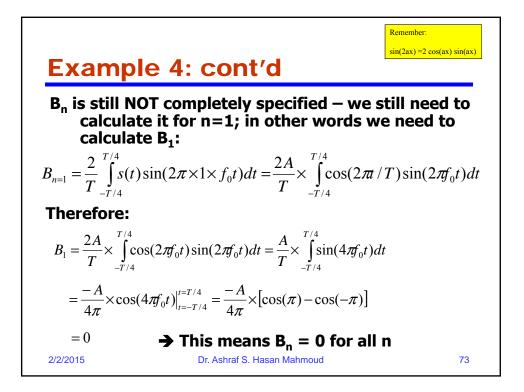


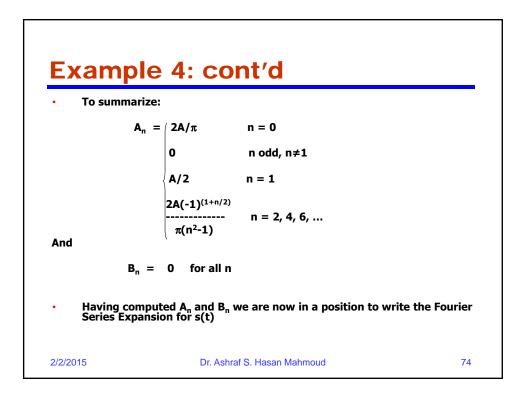


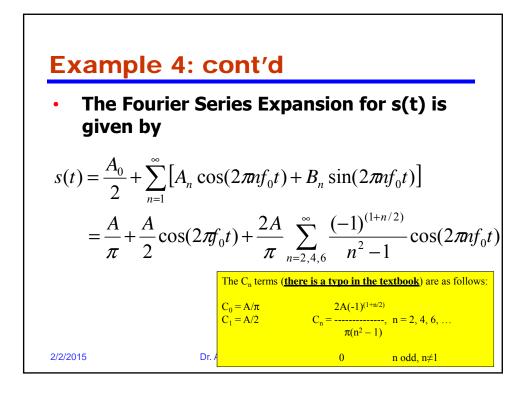


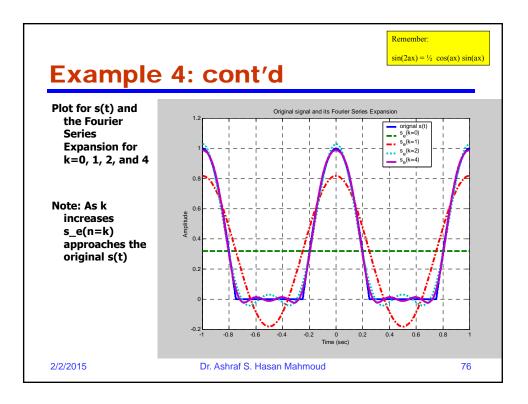


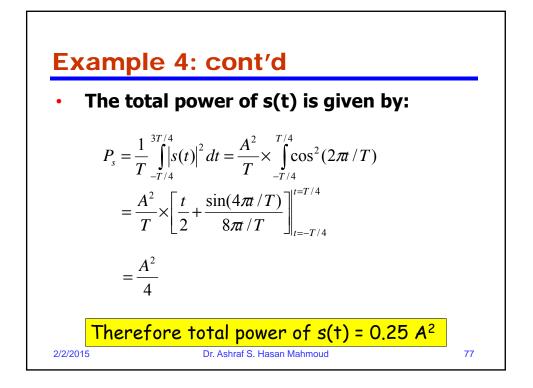




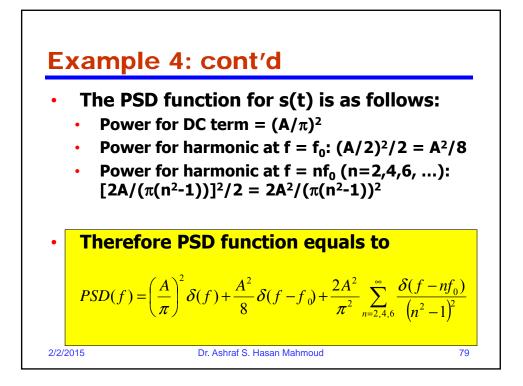


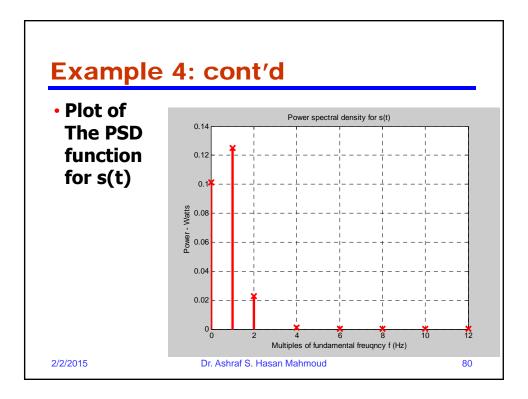


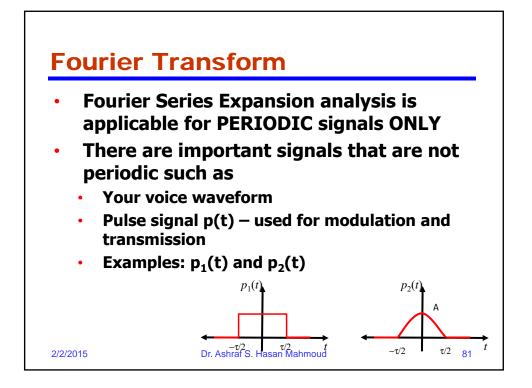


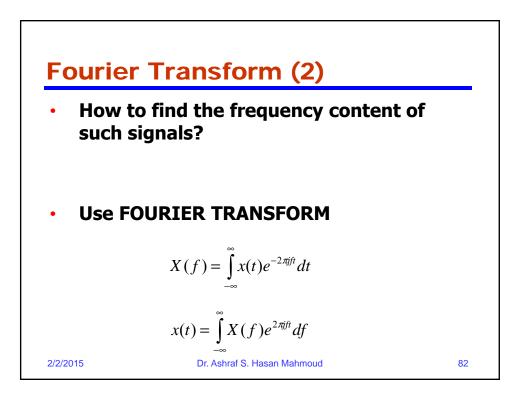


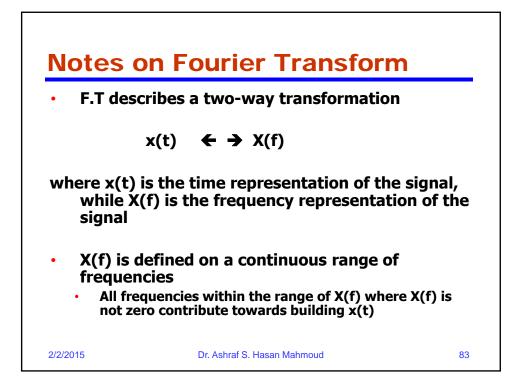
<ul> <li>To find n* such that power of s_e(n=n*) = 95% of total power:</li> </ul>			
s_e(n=k)	Expression	Power	% Power+
k = 0	Α/π	0.1013 A <sup>2</sup>	$\begin{array}{c} (0.1013A^2)/(0.25) \\ A^2) = \\ 40.5\% \end{array}$
k = 1	$A/\pi + A/2\cos(2\pi f_0 t)$	0.2263 A <sup>2</sup>	$(0.2262A^2)/(0.25A^2)$ = 90.5%
k = 2	$A/\pi + A/2 \cos(2\pi f_0 t) + 2A/(3\pi) \cos(2\pi 2f_0 t)$	0.2488 A <sup>2</sup>	(0.2488A <sup>2</sup> )/(0.25A <sup>2</sup> ) <b>99.5%</b>

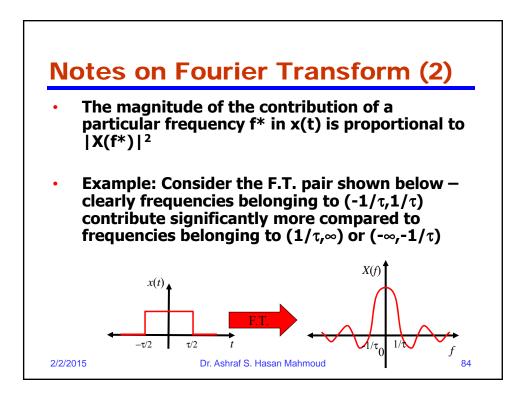


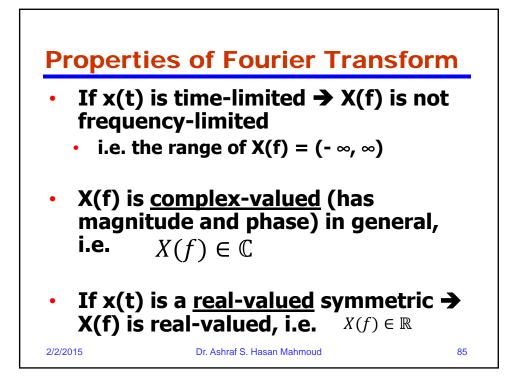


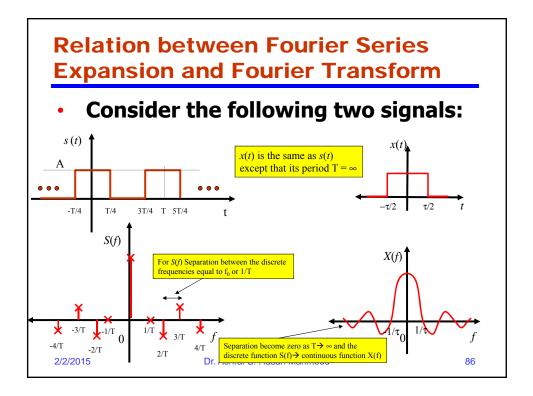


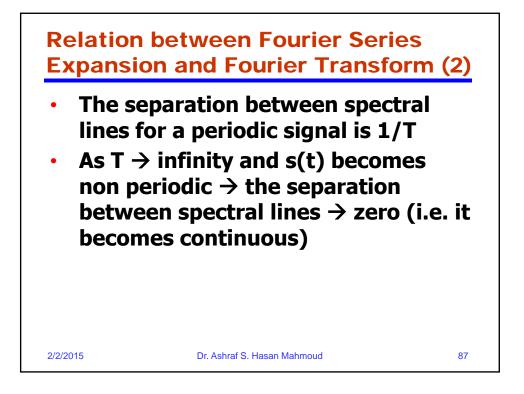


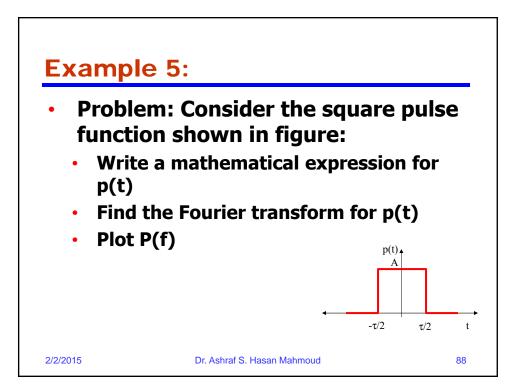


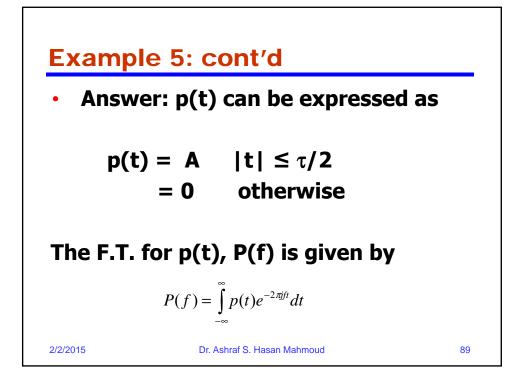


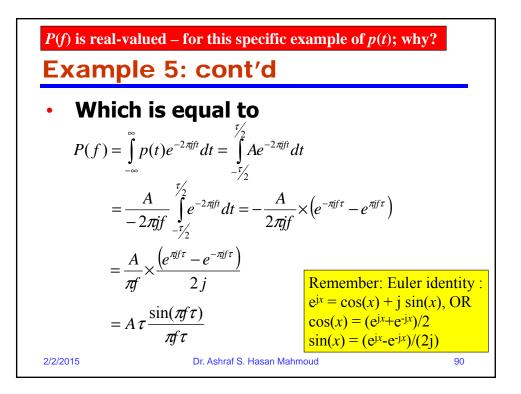


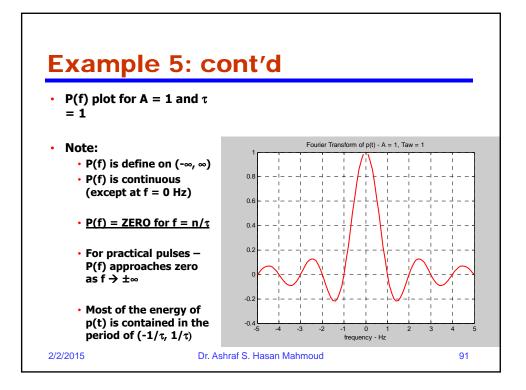












## **Energy Spectral Density Function (ESDF)**

• ESDF is defined as

$$ESD(f) = \frac{1}{2\pi} P(f) P^*(f)$$

where P(f) is the F.T. of the pulse p(t).  $P^*(f)$  is the complex conjugate of P(f).

- ESDF is a measure of how much energy is contained at a particular frequency f
- Units of ESDF is Joules per Hz
- How would you compare ESDF with PSDF?

2/2/2015

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