

Example 2:

 Problem: What is the power of the signal s(t) used in previous example? And find n* such that the power contained in s_e(n=n*) is 95% of that existing in s(t)?

• Solution: Let the power of s(t) be given by P_s $P = \frac{1}{2} \int_{0}^{T} |s(t)|^2 dt = \frac{1}{2} \times A^2 \times \frac{T}{2} = \frac{A^2}{2} = 0.5A^2$

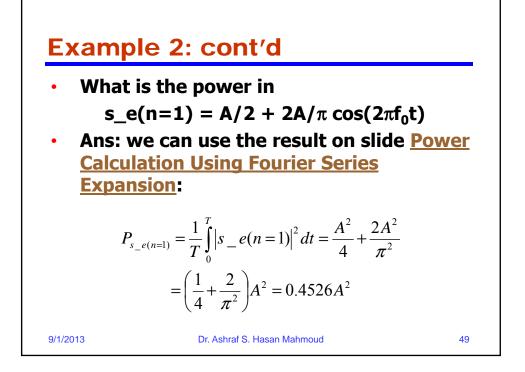
$$P_{s} = \frac{1}{T} \int_{0} |s(t)|^{2} dt = \frac{1}{T} \times A^{2} \times \frac{1}{2} = \frac{1}{2} = 0$$

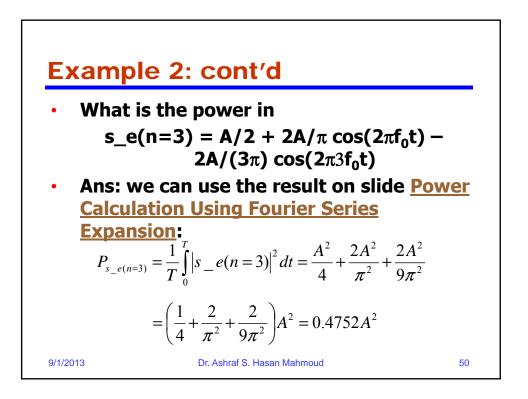
Dr. Ashraf S. Hasan Mahmoud

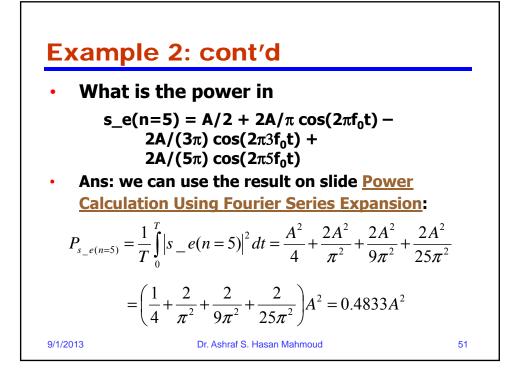
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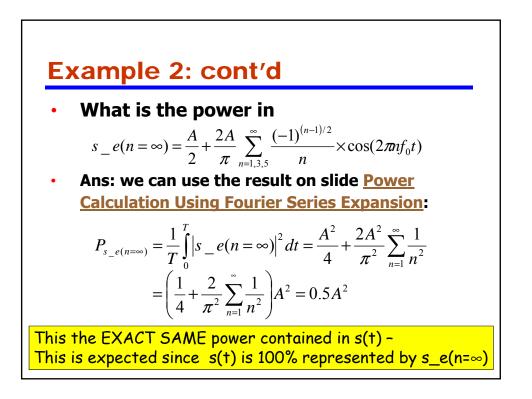
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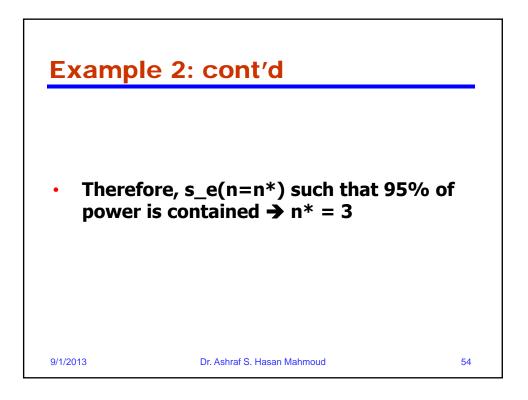


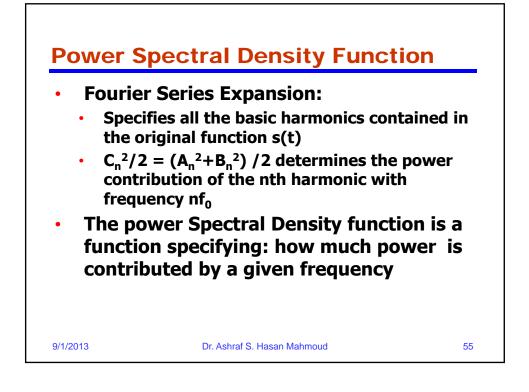


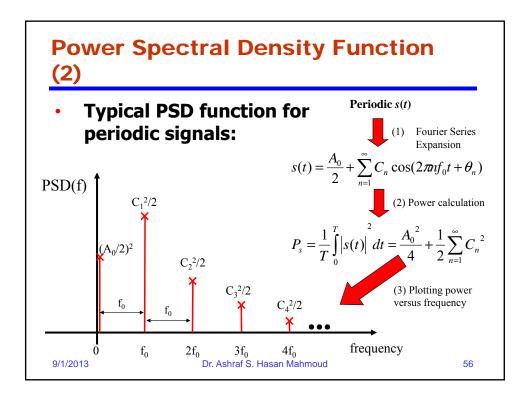


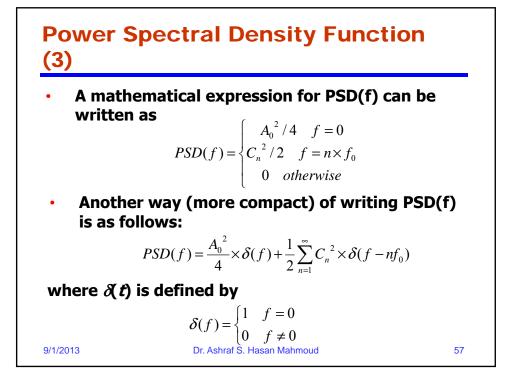


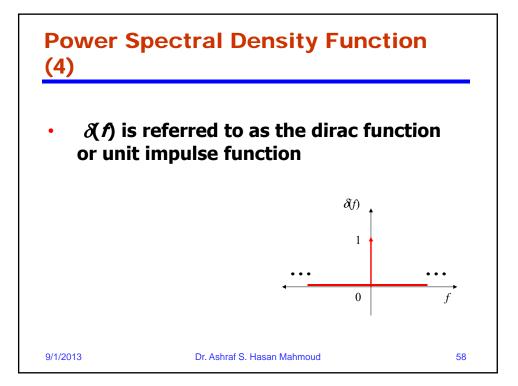
s_e(n=k)	Expression	Power	% Power+
k = 0	A/2	0.25 A ²	$(0.25A^2)/(0.5A^2)$ = 50%
k = 1	$A/2 + 2A/\pi cos(2\pi f_0 t)$	0.4526 A ²	$(0.4526A^2)/(0.5A^2)$ = 90.5%
k = 2*	$A/2 + 2A/\pi \cos(2\pi f_0 t)$	0.4526 A ²	90.5%
k = 3	$\begin{array}{r} A/2 + 2A/\pi \mathrm{cos}(2\pi f_0 t) - \\ 2A/(3\pi)\mathrm{cos}(2\pi 3 f_0 t) \end{array}$	0.4752 A ²	95.0%
k = 5	$A/2 + 2A/\pi cos(2\pi f_0 t) - 2A/(3\pi)cos(2\pi 3 f_0 t) + 2A/(5\pi)cos(2\pi 3 f_0 t) +$	0.4833 A ²	96.7%

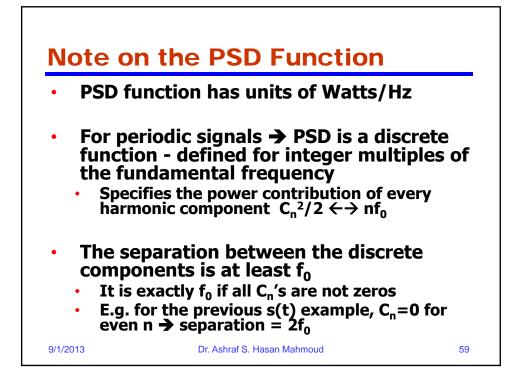


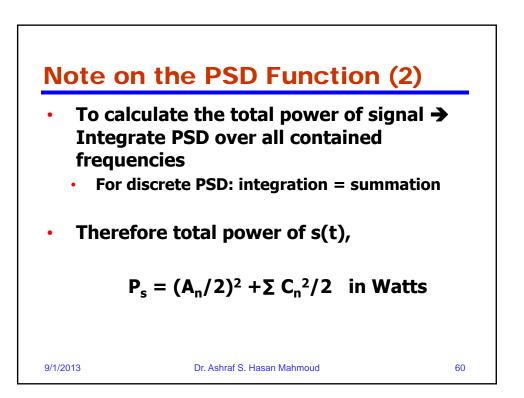


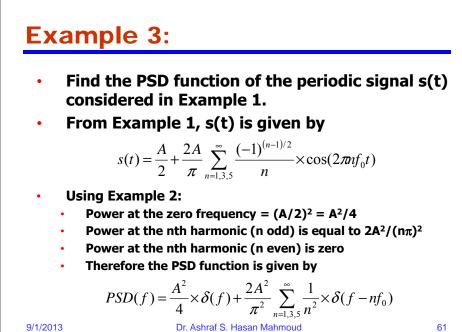




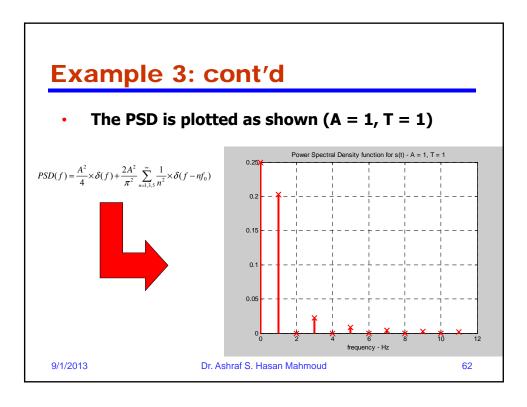


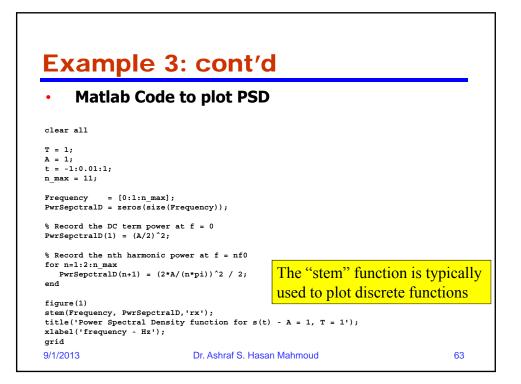


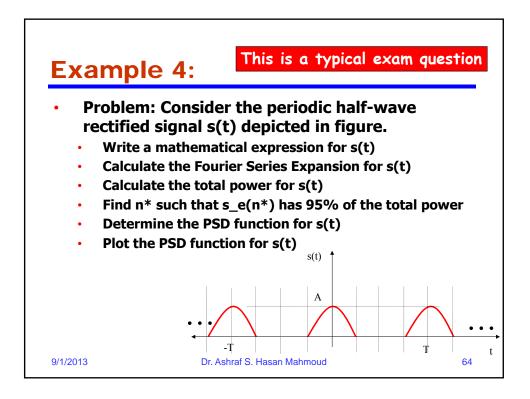


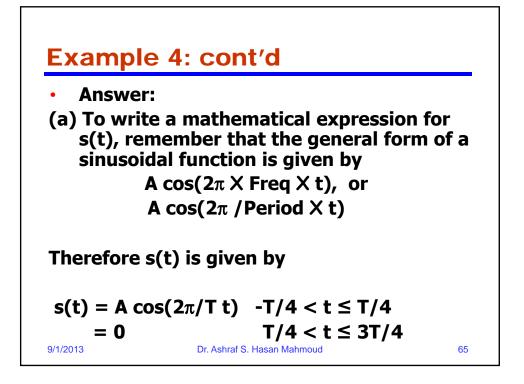


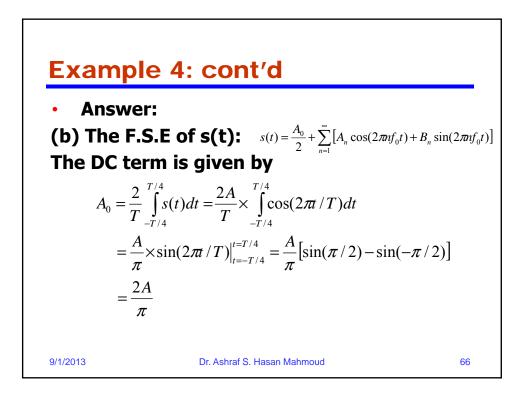


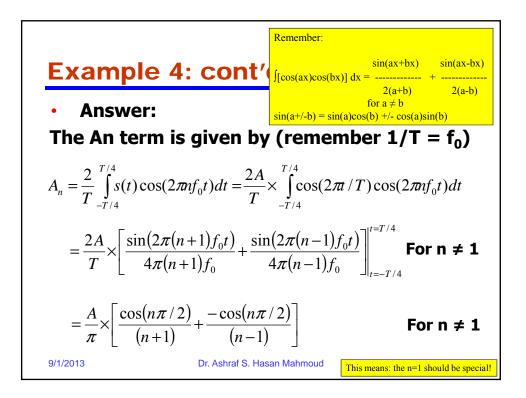


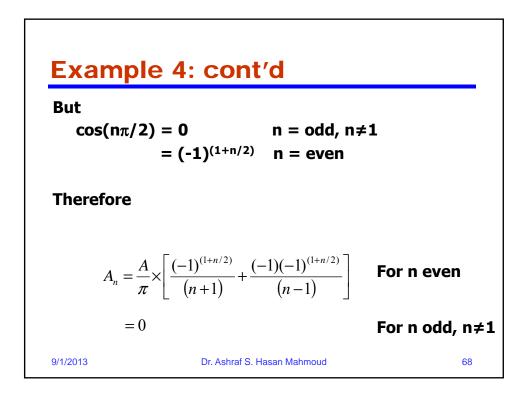


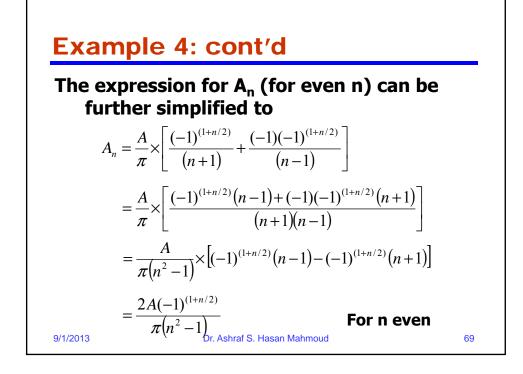


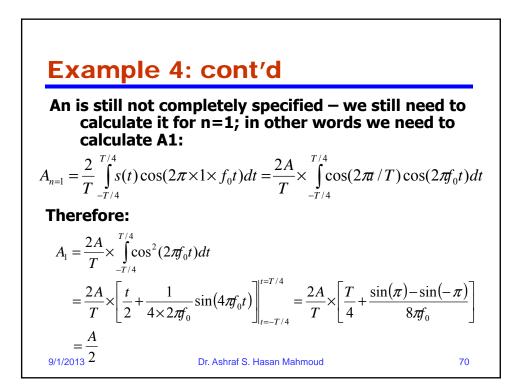






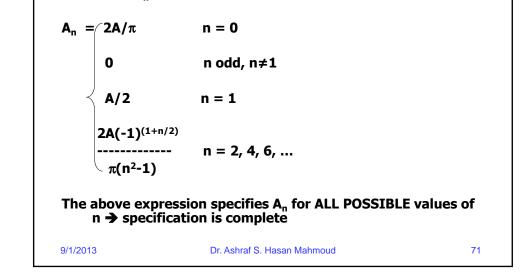


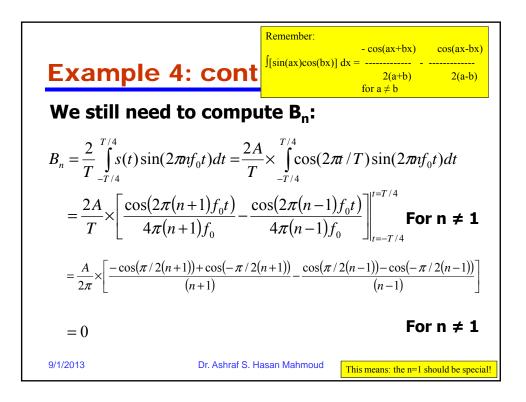


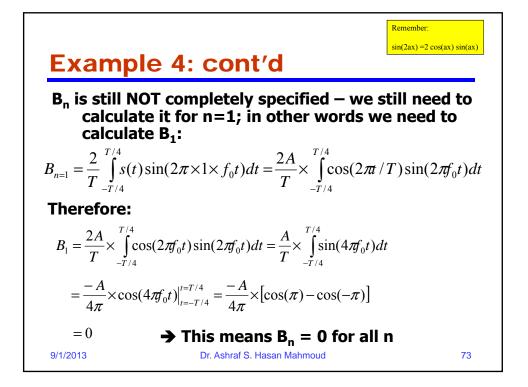


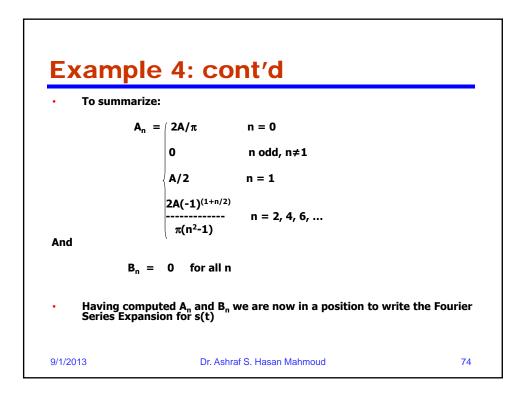


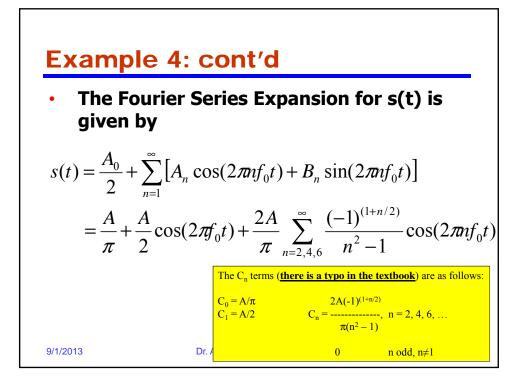
This mean A_n is equal to the following:

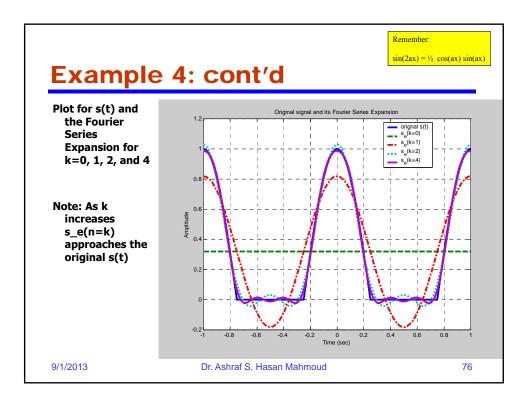


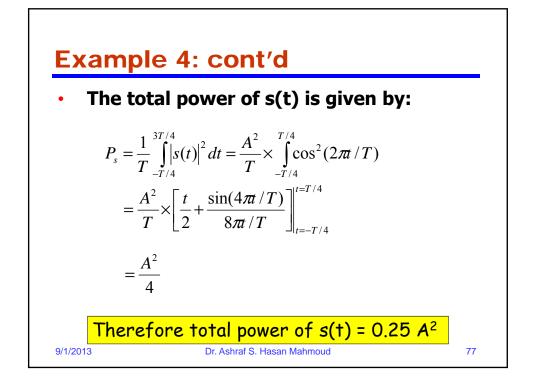




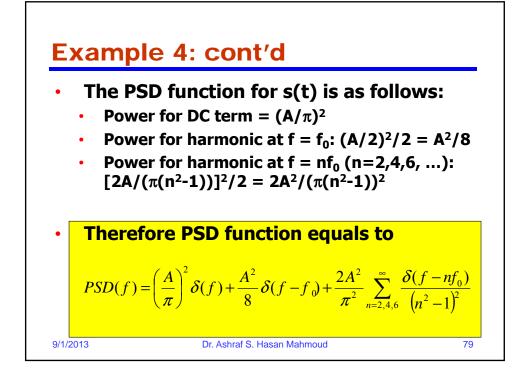


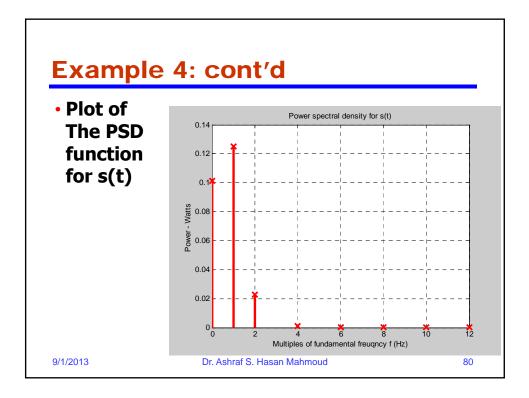


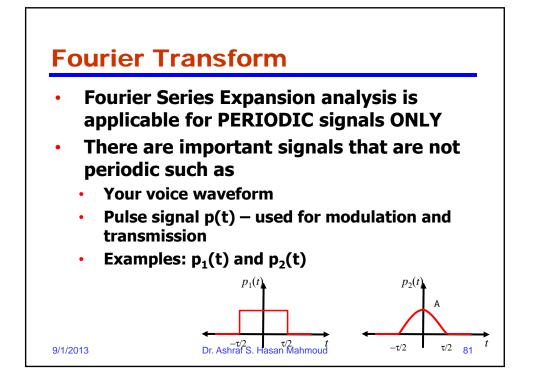


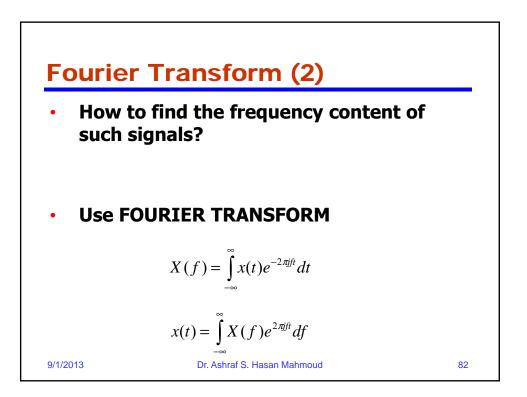


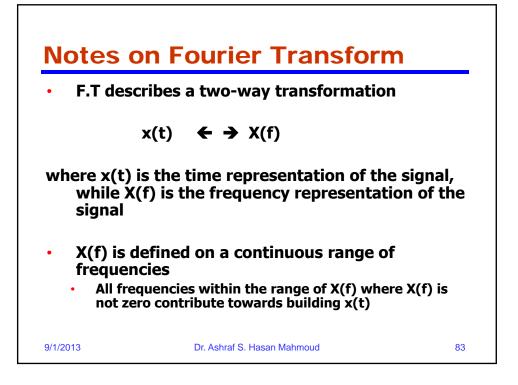
 To find n* such that power of s_e(n=n*) = 95% of total power: 			
s_e(n=k)	Expression	Power	% Power+
k = 0	Α/π	0.1013 A ²	$(0.1013A^2)/(0.25)$ $A^2) =$ 40.5%
k = 1	$A/\pi + A/2\cos(2\pi f_0 t)$	0.2263 A ²	$(0.2262A^2)/(0.25A^2)$ = 90.5%
k = 2	$A/\pi + A/2 \cos(2\pi f_0 t) + 2A/(3\pi) \cos(2\pi 2 f_0 t)$	0.2488 A ²	(0.2488A ²)/(0.25A ²) 99.5%

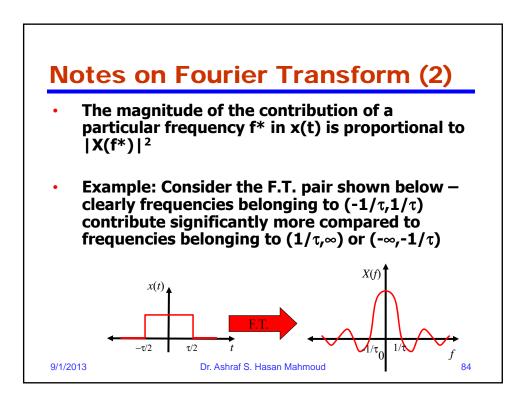


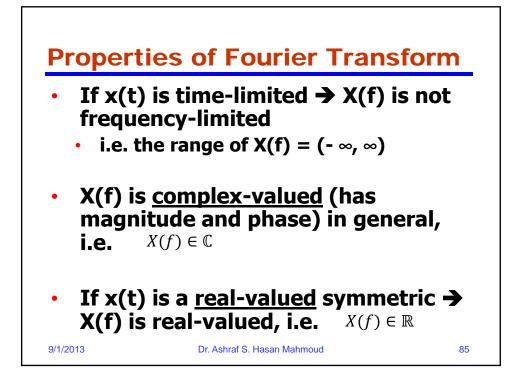


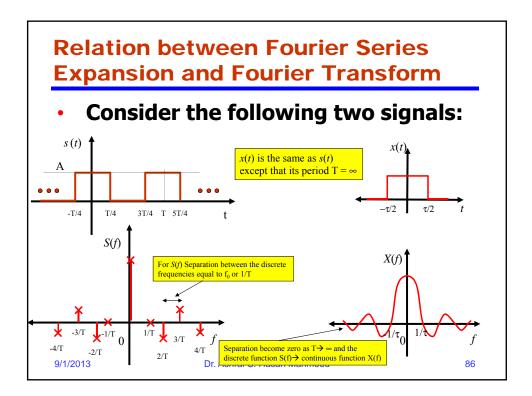


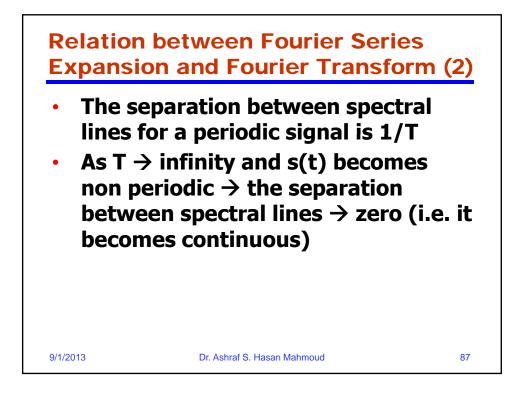


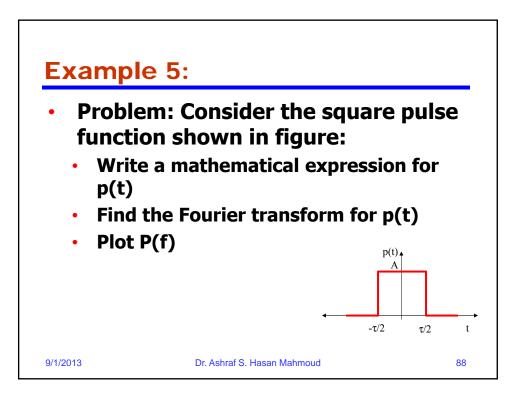


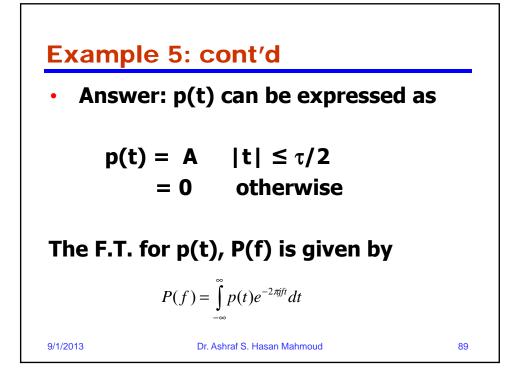


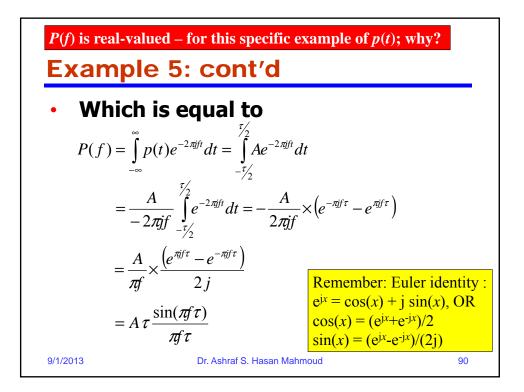


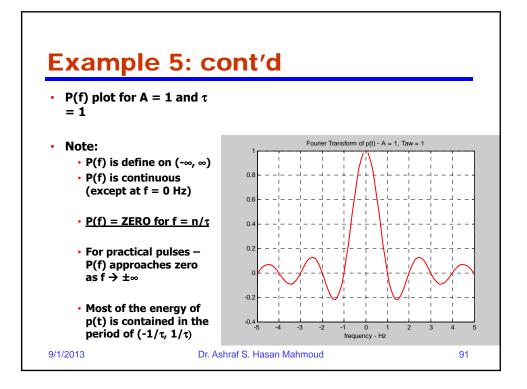


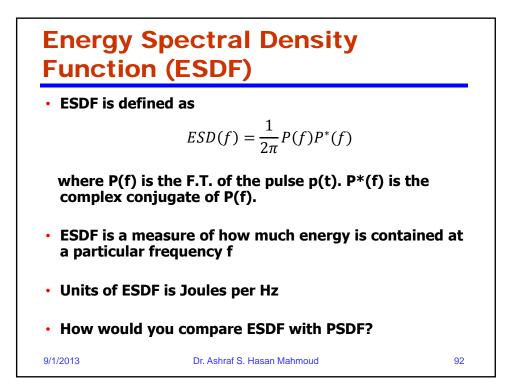


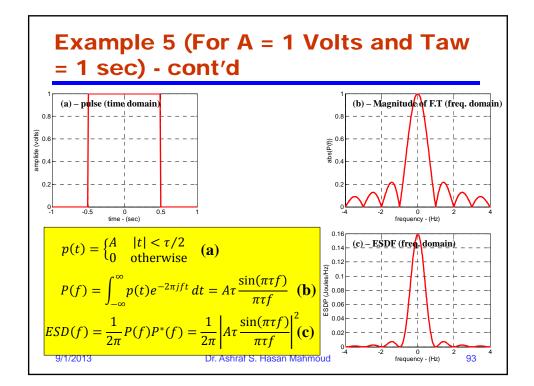












Example 5 (For A = 1 Volts and Taw = 1 sec) - Matlab Code Code for producing plots on previous slide clear all; LineWidth = 3; FontSize = 14; %Example of rectangular pulse A = 1; Taw = 1; % parameters for the rectangle pulse t_step = 0.01; f_step = 0.01; Nmax = 4; f = -Taw:t_step:Taw; % define the time axis f = -Nmax/Taw:f_step:Nmax/Taw; % define the frequency axis $ESDF_f = P_f.*conj(P_f)/(2*pi); % The ESDF$ figure(1); clf; set(gca, 'FontSize', FontSize); h = plot(t, p_t, '-r', 'LineWidth', LineWidth); xlabel('time - (sec)'); ylabel('amplide (volts)'); grid on; figure(2); clf; set(gca, 'FontSize', FontSize); $\begin{array}{l} h = \text{plot}(f, \text{ abs}(P, f), '-r', '\text{LineWidth'}, \text{LineWidth'}; \\ \text{xlabel}('\text{frequency} - (\text{Hz})'); \text{ ylabel}('\text{abs}(P(f))'); \text{ grid on}; \end{array}$ figure(3); clf; set(gca, 'FontSize', FontSize); h = plot(f, ESDF_f, '-r', 'LineWidth', LineWidth); xlabel('frequency - (Hz)'); ylabel('ESDP (Joules/Hz)'); grid on; 9/1/2013 Dr. Ashraf S. Hasan Mahmoud 94

