King Fahd University of **Petroleum & Minerals Computer Engineering Dept**

COE 241 - Data and Computer Communications

Term 121

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Lecture Contents

- Fourier Analysis
 - a. Fourier Series Expansion
 - b. Fourier Transform
 - c. Ideal Low/band/high pass filters
- Data/Signals
 - a. Audio/Voice
 - b. c. Video
 - Text
- Transmission
 - a. Analog Transmission
 - b. Digital Transmission
- 4. Transmission Impairments
 - a. Attenuation and Attenuation Distortion
 - b. Delay Distortion
 - Noise C.
- 5. Channel Capacity

 - a. Nyquist Formulab. Shannon Capacity Formula
 - c. Eb/No expression

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Analog and Digital Data Transmission

- The terms:
 - Analogue ~ continuous
 - Digital ~ discrete
- They apply to:
 - A) Data: the information to be delivered
 - B) Signaling: the electrical or electromagnetic wave that propagates carrying the data
 - C) Transmission: the mechanism of delivering the data by processing and propagation of signal

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Examples of Data/Signaling: (1) AUDIO

- Most familiar type of analogue data
- Human Ear (Receiver) bandwidth is ~10
 Hz to ~20KHz
 - You can not hear sounds with frequencies much higher than 20KHz or much lower than 10 Hz – Some other animals can do that (bats, whales, etc)
- Human speech (Data) is mostly between 100 Hz and 7K Hz – with most of the energy concentrated in the lower part of this range

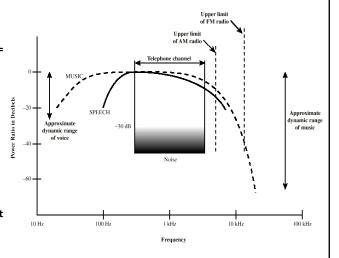
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Examples of Data/Signaling: (1) AUDIO – cont'd

- Typical Speech has a dynamic range of 25 dB – ratio of strongest speech signal to weakest speech signal is 25 dB or 10^{25/10} = 300 (in linear scale)
- The Telephone Channel has a bandwidth of about 3.1KHz (from 300 Hz to 3400 Hz)
- Note that Music has a much wider bandwidth than speech (~10 Hz to ~20 KHz) – Hence a good audio system (CD player, high end speakers, etc) should be able to reproduce these signals
- Music has also a higher dynamic range too – What is the dynamic range of your audio system?

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Examples of Data/Signalling: (2) VIDEO

- Another common example of analog data
- The original scene (source) is scanned and its image recorded by the camera – RASTER image
- In the TV: a moving electron beam scan the screen producing the picture
 - For black and white: the amount of illumination produced (on a scale from black (lowest) to white (highest) at any point is proportional to the beam intensity
- Hence the original brightness in REPRODUCED on the screen
- Video Image ←→ Time varying analog signal

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Examples of Data/Signalling: (3) VIDEO - cont'd

- Total of 525 horizontal lines (vertical resolution)
 - 483 visible lines (241.5 even and 241.5 odd)
 - Subjective vertical resolution is 70X483 = 338 lines
 - Hence, horizontal resolution is (4/3)X338 = 450 pixels per line
 - 42 blanked during vertical retrace
- Basic line duration = 63.5 μsec:
 - 52.5 μsec scanning horizontally
 - 11 µsec for horizontal retrace
- High number of scans per second → smoother picture but expensive hardware
- Low number of scans per second → jittery picture (flickering)
- Interlacing: scan odd lines first at 60 scan per second and then scan even lines at 60 scans per second → To the human eye, the screen is 60 refreshed 60 times per second, i.e. no flickering
 - Interlacing

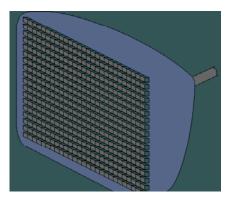
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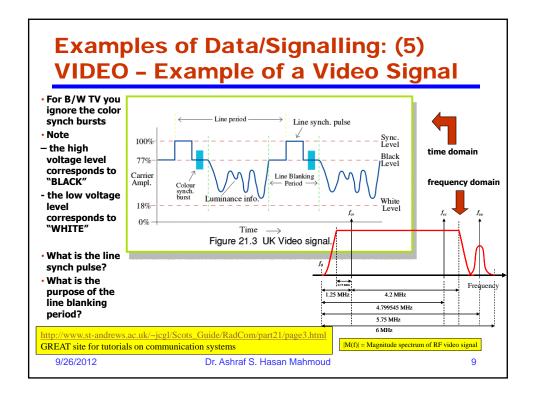
Examples of Data/Signalling: (4) VIDEO - cont'd

- Scanning Process:
 - Starts at the far left near top
 - Scans 241.5 lines
 - Ends at middle of screen – lowest part
 - Beam is repositioned at the top again
 - Scanning starts again for the other 241.5 lines (interlaced with the previous lines)



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Examples of Data/Signalling: (6) VIDEO - cont'd - Bandwidth Calculation

- 525 lines per scan at 30 scans per second → 15,750 lines/sec or 63.5 µsec per line
 - 52.5 µsec is the actual time spent in illuminating horizontal pixels
- There are 450 horizontal pixels per line
 - For maximum bandwidth calculation
 - Let illumination alternative from white to black and visa versa for consecutive pixels → 225 cycles / line
 - But line scanning is done in 52.5 µsec/line.
 - Hence, the beam does (225/52.5 µsec) = 4.2X10⁶ cycles per second
 - · For minimum bandwidth
 - Let all pixels has same illumination level (no change in picture) → DC component – fmin = 0 Hz
- Adding audio and color information does not increase bandwidth
- Hence NTSC video signal bandwidth is about 4 MHz

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Example:

 Problem 3.12: For a video signal, what increase in a) horizontal b) vertical resolution is possible if a bandwidth of 5 MHz is used?

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Example:

Solution:

For increase in horizontal resolution - keeping same vertical resolution (483 lines); each horizontal lines occupies 52.5 $\mu sec,$ therefore new horizontal resolution H is given by

5 MHz = (H/2) / 52.5 μ sec → H = 525 lines

For increase in vertical resolution – keeping same horizontal resolution of H = 450 lines, hence the new time for each horizontal line T is

 $5MHz = (450/2) / T \rightarrow T = 45 \mu sec$

The horizontal retrace still takes 11 μ sec, therefore total time for horizontal line is 56 μ sec.

(1/30 sec/scan) / V lines/scan = 56 µsec/line → V = 595 lines/scan

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Examples of Data/Signalling: (3) TEXT

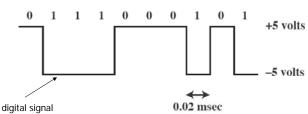
- Digital Data (pre-defined set of symbols)
 - Same as Morse Code
- IRA (or ASCII in the US) define 128 character using 7-bit words
- When transmitted or stored 1B or 8-bit words are used
 - A parity bit is added as a simple error detection technique
- The signal representing this data:
 - · One DC level for binary one
 - Another DC level for binary zero
- Bandwidth representing this signal:
 - Maximum bandwidth is required when bits alternate between 0 and 1 → This results in a periodic square waveform (see Figure 3.13 in text)
 - Theoretical BW is infinite, but most of the energy is located for f ≤ fundamental frequency
 - · Minimum frequency is zero (DC) when all bits are equal

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Examples of Data/Signalling: (4) TEXT

- Figure 3.13 (textbook) conversion of PC input digital signals.
- What is the minimum frequency for the shown signal?
- What is the maximum frequency for the shown signal?
- What is the APPROXIMATE bandwidth for the shown signal?





User input at a PC is converted into a stream of binary digits (1s and 0s). In this graph of a typical digital signal, binary one is represented by -5 volts and binary zero is represented by +5 volts. The signal for each bit has a duration of 0.02 msec, giving a data rate of 50,000 bits per second (50 kbps).

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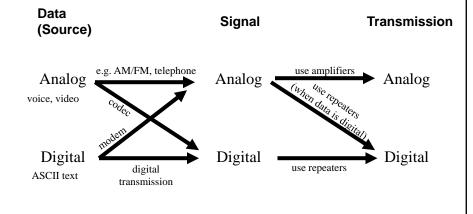
Transmission

- Analog Transmission:
 - Analog signal is propagated through amplifiers to compensate for attenuation and to achieve longer distance
 - Amplifiers:
 - · Boost signal and noise equally
 - May distort original signal
 - Can not be used indefinitely
- · Digital Transmission:
 - To overcome the higher attenuation, repeaters are used at appropriately spaced points
 - Repeaters:
 - Recover original digital data
 - Transmit new signal
 - · Can be used indefinitely

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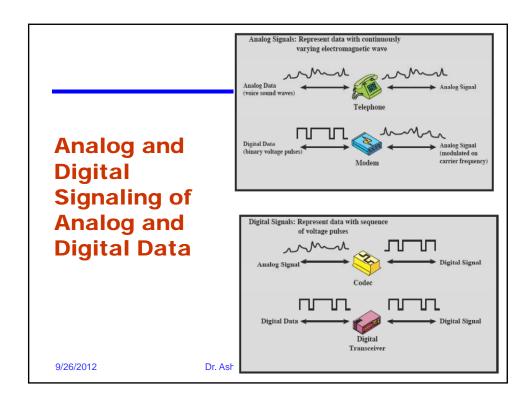
Transmission (2)

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Transmission (3)

- Digital Transmission is the prevailing technology:
 - Digital Technology: Capitalize on advances in digital circuitry
 - Data Integrity: With the use of repeaters, the effects of noise and other signal impairments are not cumulative
 - Capacity Utilization: It is easier to multiplex several digital signals (using TDM) on one high capacity link as opposed to multiplexing analog sources using FDM
 - · Security and Privacy: Use of encryption
 - Integration: Provides a uniform vehicle to transport both analog and digital data

very important reasons the popularity of digital transmission

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Transmission Impairments

- Impairments can degrade the quality of an analog signal or cause a bit (symbol) error for a digital signal
- **Types of Impairments:**
 - Attenuation and Attenuation Distortion
 - **Delay Distortion**
 - Noise

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Attenuation and Attenuation Distortion

- A received signal must have sufficient strength for proper detection at receiver
- For error-free communication signal strength relative to noise must
- frequency: Different components of signal are subject to different attenuation →
 - **Distortion in time domain**

Attenuation is an increasing function of Attenuation

- **Solution: Equalize transmission**
 - Results in almost equal attenuation qualized (gain) for all frequencies of . Attenuation interést function



- Frequencies of interest for a digital signal are centered around the fundamental frequency, f
- Attenuation function has to be flat around f only

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frequency

frequency

Increasing with frequency -

Causes attenuation distortion

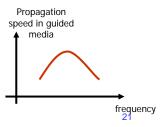
Roughly constant with frequency -

Does not cause attenuation distortion

Delay Distortion

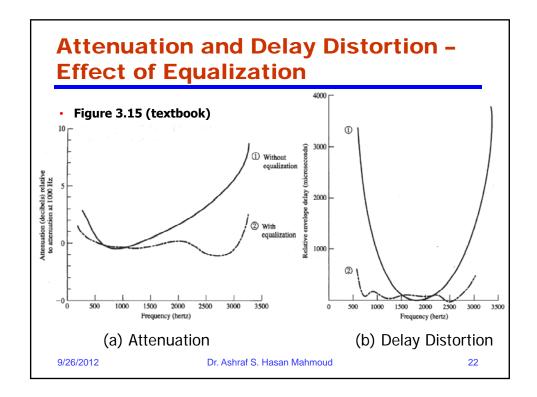
- For guided media different frequency components have different propagation speeds
- For unguided media multipath (signal being received through more than one path) causes delay distortion
- Received signal is distorted due to varying delays experienced at its constituent frequencies
- Critical for digital data: Causes Intersymbol interference a major limitation on maximum bit rate over a transmission channel

· Solution: Equalization



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Noise

- Major limiting factor in communication system performance
- Types of Noise:
 - Thermal Noise
 - · Intermodulation Noise
 - Crosstalk
 - · Impulse Noise

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Thermal Noise

- Due to agitation of electrons
- Function of temperature (energy of electrons)
- Can not be eliminated → limits communication system performance
- Noise power density (noise power found in 1 Hz) , N_{0} , is given by

$$No = kT$$
 (Watts/Hz)

Where k is Boltzman constant = $1.3803x10^{-23}$ J/degree Kelvin

T is the temperature in degrees Kelvin

· Hence, the thermal noise power in a bandwidth B Hz is given by

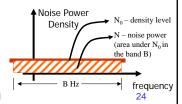
$$N = N_0 \times B = kT \times B$$
 (Watts)

• In decibels:

$$NdB = 10logk + 10logT + 10logB$$
$$= -228.6 dBW + 10logT + 10logB$$

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Examples:

 Problem 3.14: Given an amplifier with effective noise temperature of 10,000 degrees Kelvin, and a 10-MHz bandwidth, what thermal noise we expect at the output

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Examples:

Solution:

N = kT X B

 $k = 1.38x10^{-23}$ J/Kelvin, T = 10,000 degrees Kelvin, B = 10X10⁶ Hz,

N = 1.38X10⁻¹² Watts

 N_{dBW} = 10 log N = -118.6 dBW

In dBmW, one can write

NdBmW = 10 log N*1000 = -88.6 dBmW or simply, NdBmW = N_{dBW} + 30

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Intermodulation Noise

- Lineal System: H_L(S) = A₁xS + A₀
- E.g. Consider the input S_1+S_2 , where $S_1=\cos(2\pi^*f_1^*t)$ and $S_2=\cos(2\pi^*f_2^*t)$. The system output is

$$H_1(S_1+S_2) = A_1x \cos(2\pi^*f_1^*t) + A_1x \cos(2\pi^*f_2^*t) + A_0$$

Note the output signal has frequencies f_1 and f_2 ONLY.

• NonLinear System (example): $H_{NL}(S) = A_2xS^2 + A_1xS + A_0$ The output (for the same input) is

```
\mathsf{H}_{\mathsf{NL}}(\mathsf{S}_1 + \mathsf{S}_2) = \mathsf{A}_2 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right]^2 + \mathsf{A}_1 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t}) \right] + \mathsf{A}_0 x \left[ \cos(2\pi^* \mathsf{f}_1^* \mathsf{t}) + \cos(2\pi^* \mathsf{f}_2^* \mathsf{t})
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Note that $[\cos(2\pi^*f_i^*t)]^2 = \frac{1}{2} + \frac{1}{2}\cos(2\pi^*2f_i^*t)$, and

 $\cos(2\pi^*f_1^*t)\cos(2\pi^*f_2^*t) = \frac{1}{2}\cos(2\pi^*(f_1+f_2)^*t) + \frac{1}{2}\cos(2\pi^*(f_1-f_2)^*t)$

Output signal contain terms with multiples of (f1+f2) and (f1-f2)

- Intermodulation noise: undesired signals at the frequency that is multiples of sum or difference of the two original input frequencies
- Caused by nonlinearity

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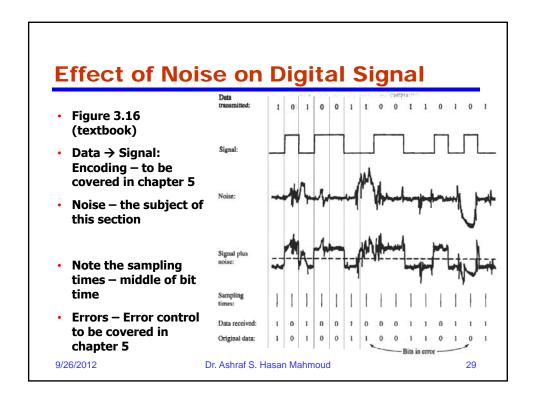
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Crosstalk/Impulse Noise

- Crosstalk:
 - · Unwanted coupling between signal paths
 - · E.g. electrical coupling between near by twisted pair wires
 - Coax cables are more immune to cross talk compared to twisted pairs
- Impulse Noise:
 - Unlike previous types of noise, this one is:
 - Noncontinuous irregular pulses or spikes for short duration and high amplitude
 - Causes:
 - Lightening
 - · Faults or flaws in communication systems
 - Major concern for digital data

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Channel Capacity

- · Terminology:
 - · Data Rate (R): bit rate of channel bits per second
 - Bandwidth (B): bandwidth of transmitted signal Hz
 - Noise power (N): average noise power level for communication channel – Watt/Hz for density or Watt for noise power
 - Error rate (Pe): rate at which an erroneous detection is made (detecting 0 for 1 and 1 for 0)





Bandwidth B

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Nyquist Bandwidth

- For a noise-free channel → data rate is limited by B of channel
- · A bandwidth of B Hz is enough to support 2B bits per second
- Example: B = 3100 Hz (telephone channel) → C = 6200 b/s
- · What if we use multilevel signaling:

$$C = 2B \log_2 M$$

Where M is the number of discrete levels used

- Example: for M = 8, same telephone channel can support C = 2X3100X log₂8 = 18.6 kb/s
- M = 2 receiver recognizes two signal levels 1s and 0s
- M > 2 receiver recognizes discrete levels other than 1 and 0
- In general, multilevel signaling requires more sophisticated receiver structure and perhaps more power for the same bandwidth

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Shannon Capacity Formula

· Capacity in the presence of noise

$$C = B \log_2(1 + SNR)$$

where SNR is the ratio of signal power to noise power – a measure of the signal quality

• Example: fmin = 3 MHz, fmax = 4 MHz, SNR = 24 dB, C = ?

$$B = 4 - 3 = 1 MHz$$

SNR =
$$10^{24/10}$$
 = 251 (on the linear scale)

$$C = 1X10^6 \log_2(1 + 251) \sim 8 \times 10^6 \text{ b/s or } 8 \text{ M b/s}$$

One can also calculate the required signaling levels, M, using Nyquist formula: $C = 2B \log_2(M) \rightarrow M = 2^{C/(2B)} = 16$

 Note the C (calculated by Shannon formula) is the theoretical (error-free) limit of the channel for the given B and SNR

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E_b/N₀ Expression

- An alternative representation of SNR
- Consider the bit stream shown in figure for bit of rate R, then each bit duration is equal to T_b = 1/R seconds
- Energy of signal for the bit duration is equal to A²X T_b , where its power is equal to bit energy / T_b or A².
- Noise power is equal to N₀ X B (refer to thermal noise section)
- · Hence, SNR is given by signal power / noise power or

$$SNR = \frac{signal power}{N_0 B} = \frac{E_b}{N_0} \times \frac{R}{B}$$

One can also write

$$\left(\frac{E_b}{N_0}\right)_{dB} = SignalPower(dBW) - 10\log R - 10\log k - 10\log T$$

Stream of bits

A $T_b = 1/R \text{ (sec)}$ 33

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Examples:

Problem 3.19: Given a channel with the intended capacity of 20 Mb/s, the bandwidth of the channel is 3 MHz. What signal to noise ratio is required to achieve this capacity?

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Examples:

• Solution:

```
Shannon Limit: C = B \log_2(1 + \text{SNR}), C = 20X10<sup>6</sup> b/s, B = 3X10<sup>6</sup> Hz \log_2(1 + \text{SNR}) = 6.67 \Rightarrow \text{SNR} = 101 = 20 \text{ dB}
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Examples:

 Problem 3.21: If the received signal level for a particular digital system is -151 dBW and the receiver system effective noise temperature is 1500 degrees Kelvin. What is the Eb/N0 for a link transmitting 2400 b/s

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Examples:

Solution:

```
Eb/No = (signal power / noise power) * (B/R)

Noise power = kT X B

Hence Eb/No = (signal power) / (kT R)

= 10<sup>-151/10</sup> / (1.38X10<sup>-23</sup>X1500X2400)

= 15.99

= 12 dB

Or (Eb/N0)dB = Signalpower_dBW - 10logk - 10logT - 10logR

= -151 -10log(1.3810<sup>-23</sup>) - 10log1500 -10log2400

= 12 dB
```

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Spectral Efficiency

- Spectral Efficiency = ratio of useful bits/sec (capacity, C) to channel bandwidth, B in Hz.
- Therefore, Spectral Efficiency = C/B
- Remember that

$$Eb/N0 = S/(No \times R) = S/N * B/C$$

• But using Shannon \rightarrow S/N = $2^{C/B} - 1$, or

Eb/No = B/C
$$(2^{C/B} - 1)$$

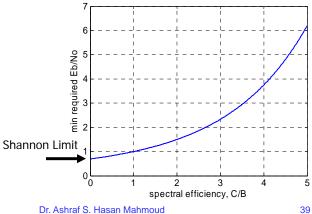
 Very useful formula relating the achievable spectral efficiency for a given Eb/No.

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Spectral Efficiency - cont'd

Note that the minimum required Eb/No for ANY communication system to work error-free is 0.6956 or -1.6 dB → This is known as the SHANNON LIMIT.



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