# KING FAHD UNIVERSITY OF PETROLEUM \& MINERALS COLLEGE OF COMPUTER SCIENCES \& ENGINEERING COMPUTER ENGINEERING DEPARTMENT <br> COE-543 - Mobile and Wireless Networks November 17 ${ }^{\text {th }}, 2011$ - Midterm Exam 

## Student Name: <br> Student Number: <br> Exam Time: 90 mins

- Do not open the exam book until instructed
- The use of programmable and cell phone calculators is not allowed - only basic are permitted
- Answer ALL Questions
- All steps must be shown
- Any assumptions made must be clearly stated

| Question No. | Max Points |  |
| :---: | :---: | :---: |
| 1 | 50 |  |
| 2 | 50 |  |
| 3 | 50 |  |
| Total: | 150 |  |

## Q.1) On the subject of RF propagation

( 50 points) The modulation technique used in the existing AMPS is analog FM. The transmission bandwidth is 30 kHz per channel and the maximum transmitted power from a mobile use is 3 W . The acceptable quality of the input SNR is 18 dB , and the background noise in the bandwidth of the system is -120 dBm ( 120 dB below the 1 mW reference power). In the cellular operation we may assume the strength of the signal drops 30 dB for the first meter of distance from the transmitter antenna and 40 dB per decade of distance for distances beyond 1 meter.

1. What is the maximum distance between the mobile station and the base station at which we have an acceptable quality of signal?
2. Repeat (a) for digital cellular systems for which the acceptable SNR is 14 dB
3. For (2) - now assume shadowing is considered. What would be the distance such that $90 \%$ of the locations have SNR equal or greater than 14 dB ? Assume the shadowing process has a standard deviation of 8 dB .

Solution:

(1) Maximum distance for an SNR of 18 dB .

The transmitter power is $\mathrm{Pt}=10 \log (3 \mathrm{Watts} / 1 \mathrm{~mW})=34.8 \mathrm{dBm}$
The minimum acceptable received power is Prmin $=-120 \mathrm{dBm}+18 \mathrm{~dB}=-102 \mathrm{dBm}$
The maximum allowable path loss is Lpmax $=\operatorname{Pt}-\operatorname{Prmin}=34.8 \mathrm{dBm}-(-102 \mathrm{dBm})=136.8 \mathrm{~dB}$
The path loss model based on 30 dB in the first meter and 40 dB per decade of distance is
$L p=30+40^{\star} \log _{10}(d) \rightarrow d=10^{(L p-30) / 40}$ and $d m a x=10^{(L p m a x-30) / 40}=10^{(136.8-30) / 40}=468$ meters
(2) Maximum distance for an SNR of 14 dB .

The transmitter power is $\mathrm{Pt}=10 \log (3 \mathrm{Watts} / 1 \mathrm{~mW})=34.8 \mathrm{dBm}$
The minimum acceptable received power is $\operatorname{Prmin}=-120 \mathrm{dBm}+14 \mathrm{~dB}=-106 \mathrm{dBm}$
The maximum allowable path loss is Lpmax $=P t-\operatorname{Prmin}=34.8 \mathrm{dBm}-(-106 \mathrm{dBm})=140.8 \mathrm{~dB}$
The path loss model based on 30 dB in the first meter and 40 dB per decade of distance is
$L p=30+40^{\star} \log _{10}(d) \rightarrow d=10^{(L p-30) / 40}$ and dmax $=10^{(L \operatorname{pmax}-30) / 40}=10^{(140.8-30) / 40}=589$ meters
(3) Using the standard normal variable tables - $z p=1.282 \rightarrow X=8 * 1.282=10.26 \mathrm{~dB}$.

Therefore, the new minimum acceptable received power is $\operatorname{Prmin}=-120+14+10.26=-95.74 \mathrm{~dB}$
The maximum allowable path loss is Lpmax $=P t-\operatorname{Prmin}=34.8 \mathrm{dBm}-(-95.7)=130.5 \mathrm{~dB}$ $L p=30+40^{\star} \log _{10}(d) \rightarrow d=10^{(L p-30) / 40}$ and dmax $=10^{(\text {Lpmax-30)/40 }}=10^{(130.5-30) / 40}=325.5$ meters

## Q.2) On the subject of cellular concept and traffic engineering

(50 points) Consider a cellular system with 395 total allocated voice channels of 30 kHz each. The total available bandwidth in each direction is 12.5 MHz . The traffic is uniform with average call holding time of 120 seconds, and call blocking during the system busy hour is $2 \%$. Assume a cell reuse factor of 7,3 antenna sectors per cell site, and a slope for the pathloss of $40 \mathrm{~dB} /$ decade. Furthermore, assume the there are 10 mobiles $/ \mathrm{km} 2$ with each mobile generating traffic of 0.02 Erlangs.
a) ( 5 points) Calculate the calls per cell site per hour the network can support
b) (5 points) Calculate the maximum cell radius the network can support
c) (10 points) Calculate the mean SIR provided by setup
d) ( 20 points) Calculate the spectral efficiency in Erlangs $/ \mathrm{km} 2 / \mathrm{MHz}$
e) (10 points) How would an engineer utilize antenna sectorization to increase the capacity for the above system.

## Solution:

The traffic per cell site $=V X+X A c$
Where $\quad V=$ no of mobile per km2
$t=$ traffic in Erlangs per mobile
$A c=$ area of cell $=2.6 R^{2}$ ( $R$ is the cell radius)
Therefore, traffic per cell site $=10 \times 0.02 \times 2.6 R^{2}=0.52 R^{2}$ Erlangs
No of voice channels per sector $=395 /(7 \times 3)=19$ channel
Offered traffic per sector $=12.3$ Erlangs or $12.3 \times 3=36.9$ Erlangs per cell site
Carried traffic per cell site $=(1-0.02) \times 36.9=36.2$ Erlangs
a \& b) But carried traffic $=$ No of calls per cell site per hour $\times 3600 / 120$
$\rightarrow$ No of calls per cell site per hour $=1,086$
$\rightarrow$ Cell radius $\mathrm{R}=\operatorname{sqrt}(36.2 / 0.52)=8.3 \mathrm{~km}$
c) Mean SIR $=q^{\alpha} / m$, assuming $m$ co-channel interferers all at the reuse distance $D$ for $a=4$ (given), $N=7, q=5(3 N)=4.6, m=2$ (for 3 sectors) $\rightarrow$ SIR $=223.9$ or $23.5 d B$
d)

| Traffic carried per cell $\times$ Nc | Traffic carried per cell |
| :---: | :---: |

or

$$
=36.2 /\left(2.6 \mathrm{R}^{2} \times 12.5\right)=0.0162 \text { Erlangs } / \mathrm{km} 2 / \mathrm{MHz}
$$

e) To increase capacity utilizing sectorization, the engineer must increase number of sectors per site to say 4 or 6 and at the same time reduce the reuse factor to 4 or 3 . Without reducing the reuse factor there will be no capacity improvement.

## Q.3) (50 points) On the subject of physical layer for wireless networks

a) Frequency shift keying modulation (FSK)
a.1) (10 points) Explain the basic operation FSK modulation - Use drawing if possible.
a.2) (5 points) What is relation between Minimum shift keying (MSK) and FSK?
a.3) (10 points) How is MSK improved upon in Gaussian minimum shift keying? Draw the block diagram of the GMSK modulator.
b) Consider the spectral density functions of the MSK and GMSK shown in figure.
b.1) ( $\mathbf{1 0}$ points) What is referred to by $\mathrm{B}_{\mathrm{b}} \mathrm{T}$ ? Define the term and it implication.
b.2) ( $\mathbf{1 0}$ points) In terms of adjacent channel interference, which modulation scheme (MSK or GMSK) is better? And why?
b.3) (5 points) What is the disadvantage of a GMSK scheme of small $B_{b} T$ value (i.e. less than 0.25)?


Solution:
a.1) FSK: the following mapping is used: bit $0 \rightarrow \cos \left(2 \pi f_{1} t\right)$ while bit $1 \rightarrow \cos \left(2 \pi f_{2} t\right)$. The output is a constant envelope signal (refer to figure)
a.2) MSK is an FSK carrier modulation scheme where minimum frequency spacing is chosen such that the signal alphabets are orthogonal. This spacing is $1 /(2 \mathrm{~T})$ for coherent MSK And $1 / T$ for non coherent MSK. MSK is a constant-envelope continuous-phase modulation where abrupt phase changes at the bit transition times (characteristic of FSK in general) are eliminated.
a.3) To further reduce side lobes of an MSK signal power spectrum, a Gaussian filter is used in front of the MSK/FSK modulator - the resulting scheme is referred to by GMSK. The filter reduces side lobes and therefore reduces adjacent channel interference.
(a.1)

(a)

FSKMSK

(a.3)


Block diagram of GMSK modulator
b.1) BbT is the Time-bandwidth product for the Gaussian filter used in GMSK. where $B_{b}=3 \mathrm{~dB}$ bandwidth of the Gaussian filter, and T is the bit duration
Implication: an indication of how wide the filter bandwidth - when $\mathrm{Bb}=\infty \rightarrow$ all pass filter or no filter.

b.2) In terms of adjacent channel interference, MSK has the higher side lobes compared to GMSK. Further more, GMSK with lower $B_{b} T$ produces lower side lobes and therefore lower adjacent channel interference.
b.3) Low value of $B_{b} T$ (i.e. narrow low pass filter) produces good signal in terms of adjacent channel interference but a signal with very smooth transitions and therefore error-rate due to thermal noise increase.

Appendix A:
STATISTICAL TABLES

## A. 2 QUANTITIES OF THE UNIT NORMAL DISTRIBUTION

Table A. 2 lists $z_{p}$ for a given $p$. For example, for a two-sided confidence interval at $95 \%, \alpha=0.05$ and $p=1-\alpha / 2=0.975$. The entry in the row labeled 0.97 and column labeled 0.005 gives $z_{p}=1.960$.


TABLE A. 2 Quantilies of the Unit Normal Distribution

| $\boldsymbol{p}$ | 0.00 | 0.01 | 0.02 | 0.03 | 0.04 | 0.05 | 0.06 | 0.07 | 0.08 | 0.09 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.5 | 0.000 | 0.025 | 0.050 | 0.075 | 0.100 | 0.126 | 0.151 | 0.176 | 0.202 | 0.228 |
| 0.6 | 0.253 | 0.279 | 0.305 | 0.332 | 0.358 | 0.385 | 0.412 | 0.440 | 0.468 | 0.496 |
| 0.7 | 0.524 | 0.553 | 0.583 | 0.613 | 0.643 | 0.674 | 0.706 | 0.739 | 0.772 | 0.806 |
| 0.8 | 0.842 | 0.878 | 0.915 | 0.954 | 0.994 | 1.036 | 1.080 | 1.126 | 1.175 | 1.227 |
|  |  |  |  |  |  |  |  |  |  |  |
| $p$ | 0.000 | 0.001 | 0.002 | 0.003 | 0.004 | 0.005 | 0.006 | 0.007 | 0.008 | 0.009 |
| 0.90 | 1.282 | 1.287 | 1.293 | 1.299 | 1.305 | 1.311 | 1.317 | 1.323 | 1.329 | 1.335 |
| 0.91 | 1.341 | 1.347 | 1.353 | 1.359 | 1.366 | 1.372 | 1.379 | 1.385 | 1.392 | 1.398 |
| 0.92 | 1.405 | 1.412 | 1.419 | 1.426 | 1.433 | 1.4440 | 1.447 | 1.454 | 1.461 | 1.468 |
| 0.93 | 1.476 | 1.483 | 1.491 | 1.499 | 1.506 | 1.514 | 1.522 | 1.530 | 1.538 | 1.546 |
| 0.94 | 1.555 | 1.563 | 1.572 | 1.580 | 1.589 | 1.598 | 1.607 | 1.616 | 1.626 | 1.635 |
| 0.95 | 1.645 | 1.655 | 1.665 | 1.675 | 1.685 | 1.695 | 1.706 | 1.717 | 1.728 | 1.739 |
| 0.96 | 1.751 | 1.762 | 1.774 | 1.787 | 1.799 | 1.812 | 1.825 | 1.838 | 1.852 | 1.866 |
| 0.97 | 1.881 | 1.896 | 1.911 | 1.927 | 1.943 | 1.960 | 1.977 | 1.995 | 2.014 | 2.034 |
| 0.98 | 2.054 | 2.075 | 2.097 | 2.120 | 2.144 | 2.170 | 2.197 | 2.226 | 2.257 | 2.290 |
|  |  |  |  |  |  |  |  |  |  |  |
| $p$ | 0.0000 | 0.0001 | 0.0002 | 0.0003 | 0.0004 | 0.0005 | 0.0006 | 0.0007 | 0.0008 | 0.0009 |
| 0.990 | 2.326 | 2.330 | 2.334 | 2.338 | 2.342 | 2.346 | 2.349 | 2.353 | 2.357 | 2.362 |
| 0.991 | 2.366 | 2.370 | 2.374 | 2.378 | 2.382 | 2.387 | 2.391 | 2.395 | 2.400 | 2.404 |
| 0.992 | 2.409 | 2.414 | 2.418 | 2.423 | 2.428 | 2.432 | 2.437 | 2.442 | 2.447 | 2.452 |
| 0.993 | 2.457 | 2.462 | 2.468 | 2.473 | 2.478 | 2.484 | 2.489 | 2.495 | 2.501 | 2.506 |
| 0.994 | 2.512 | 2.518 | 2.524 | 2.530 | 2.536 | 2.543 | 2.549 | 2.556 | 2.562 | 2.569 |
| 0.995 | 2.576 | 2.583 | 2.590 | 2.597 | 2.605 | 2.612 | 2.620 | 2.628 | 2.636 | 2.644 |
| 0.996 | 2.652 | 2.661 | 2.669 | 2.678 | 2.687 | 2.697 | 2.706 | 2.716 | 2.727 | 2.737 |
| 0.997 | 2.748 | 2.759 | 2.770 | 2.782 | 2.794 | 2.807 | 2.820 | 2.834 | 2.848 | 2.863 |
| 0.998 | 2.878 | 2.894 | 2.911 | 2.929 | 2.948 | 2.968 | 2.989 | 3.011 | 3.036 | 3.062 |
| 0.999 | 3.090 | 3.121 | 3.156 | 3.195 | 3.239 | 3.291 | 3.353 | 3.432 | 3.540 | 3.719 |

Appendix B: Offered Loads (in Erlangs) for various Blocking Objectives - According to the Erlang-B model

| $\mathbf{P}(\mathbf{B})=$ Trunks | 0.01 | 0.015 | 0.02 | 0.03 | 0.05 | 0.07 | 0.1 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I | 0.010 | 0.015 | 0.020 | 0.031 | 0.053 | 0.075 | 0.111 |
| 2 | 0.153 | 0.190 | 0.223 | 0.282 | 0.381 | 0.471 | 0.595 |
| 3 | 0.455 | 0.536 | 0.603 | 0.715 | 0.899 | 1.057 | 1.271 |
| 4 | 0.870 | 0.992 | 1.092 | 1.259 | 1.526 | 1.748 | 2.045 |
| 5 | 1.361 | 1.524 | 1.657 | 1.877 | 2.219 | 2.504 | 2.881 |
| 6 | 1.913 | 2.114 | 2.277 | 2.544 | 2.961 | 3.305 | 3.758 |
| 7 | 2.503 | 2.743 | 2.936 | 3.250 | 3.738 | 4.139 | 4.666 |
| 8 | 3.129 | 3.405 | 3.627 | 3.987 | 4.543 | 4.999 | 5.597 |
| 9 | 3.783 | 4.095 | 4.345 | 4.748 | 5.370 | 5.879 | 6.546 |
| 10 | 4.462 | 4.808 | 5.084 | 5.529 | 6.216 | 6.776 | 7.511 |
| 11 | 5.160 | 5.539 | 5.842 | 6.328 | 7.076 | 7.687 | 8.487 |
| 12 | 5.876 | 6.287 | 6.615 | 7.141 | 7.950 | 8.610 | 9.477 |
| 13 | 6.607 | 7.049 | 7.402 | 7.967 | 8.835 | 9.543 | 10.472 |
| 14 | 7.352 | 7.824 | 8.200 | 8.803 | 9.730 | 10.485 | 11.475 |
| 15 | 8.108 | 8.610 | 9.010 | 9.650 | 10.633 | 11.437 | 12.485 |
| 16 | 8.875 | 9.406 | 9.828 | 10.505 | 11.544 | 12.393 | 13.501 |
| 17 | 9.652 | 10.211 | 10.656 | 11.368 | 12.465 | 13.355 | 14.523 |
| 18 | 10.450 | 11.024 | 11.491 | 12.245 | 13.389 | 14.323 | 15.549 |
| 19 | 11.241 | 11.854 | 12.341 | 13.120 | 14.318 | 15.296 | 16.580 |
| 20 | 12.041 | 12.680 | 13.188 | 14.002 | 15.252 | 16.273 | 17.614 |
| 21 | 12.848 | 13.514 | 14.042 | 14.890 | 16.191 | 17.255 | 18.652 |
| 22 | 13.660 | 14.352 | 14.902 | 15.782 | 17.134 | 18.240 | 19.693 |
| 23 | 14.479 | 15.196 | 15.766 | 16.679 | 18.082 | 19.229 | 20.737 |
| 24 | 15.303 | 16.046 | 16.636 | 17.581 | 19.033 | 20.221 | 21.784 |
| 25 | 16.132 | 16.900 | 17.509 | 18.486 | 19.987 | 21.216 | 22.834 |
| 26 | 16.966 | 17.758 | 18.387 | 19.395 | 20.945 | 22.214 | 23.885 |
| 27 | 17.804 | 18.621 | 19.269 | 20.308 | 21.905 | 23.214 | 24.939 |
| 28 | 18.646 | 19.487 | 20.154 | 21.224 | 22.869 | 24.217 | 25.995 |
| 29 | 19.493 | 20.357 | 21.043 | 22.143 | 23.835 | 25.222 | 27.053 |
| 30 | 20.343 | 21.230 | 21.935 | 23.065 | 24.803 | 26.229 | 28.113 |
| 31 | 21.196 | 22.107 | 22.830 | 23.989 | 25.774 | 27.239 | 29.174 |
| 32 | 22.053 | 22.987 | 23.728 | 24.917 | 26.747 | 28.250 | 30.237 |
| 33 | 22.913 | 23.869 | 24.629 | 25.846 | 27.722 | 29.263 | 31.302 |
| 34 | 23.776 | 24.755 | 25.532 | 26.778 | 28.699 | 30.277 | 32.367 |
| 35 | 24.642 | 25.643 | 26.438 | 27.712 | 29.678 | 31.294 | 33.435 |
| 36 | 25.511 | 26.534 | 27.346 | 28.649 | 30.658 | 32.312 | 34.503 |
| 37 | 26.382 | 27.427 | 28.256 | 29.587 | 31.641 | 33.331 | 35.572 |
| 38 | 27.256 | 28.322 | 29.168 | 30.527 | 32.624 | 34.351 | 36.643 |
| 39 | 28.132 | 29.219 | 30.083 | 31.469 | 33.610 | 35.373 | 37.715 |

