



• Therefore, the overall series expansion is given by

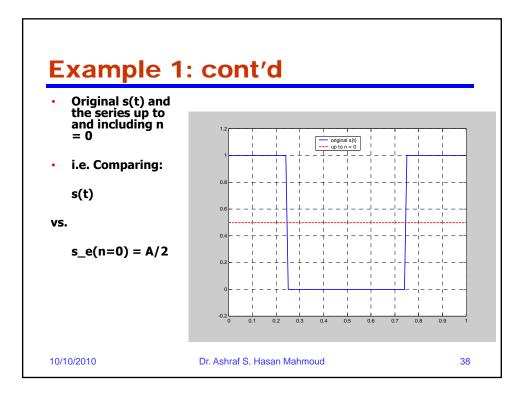
$$s(t) = \frac{A}{2} + \frac{2A}{\pi} \sum_{n=1,3,5}^{\infty} \frac{(-1)^{(n-1)/2}}{n} \times \cos(2\pi n f_0 t)$$

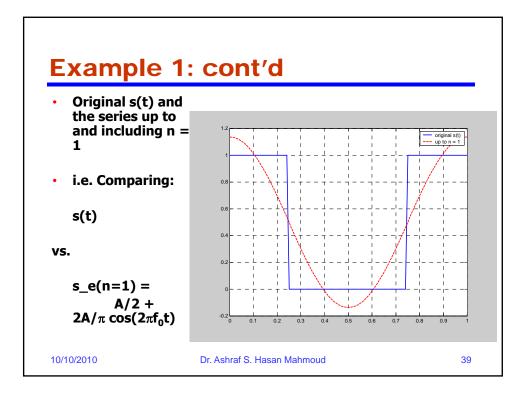
$$s(t) = \frac{A}{2} + \frac{2A}{\pi} \times \cos(2\pi f_0 t) - \frac{2A}{3\pi} \cos(2\pi \times 3f_0 t) + \frac{2A}{5\pi} \times \cos(2\pi \times 5f_0 t) - \frac{2A}{7\pi} \cos(2\pi \times 7f_0 t) + \dots$$

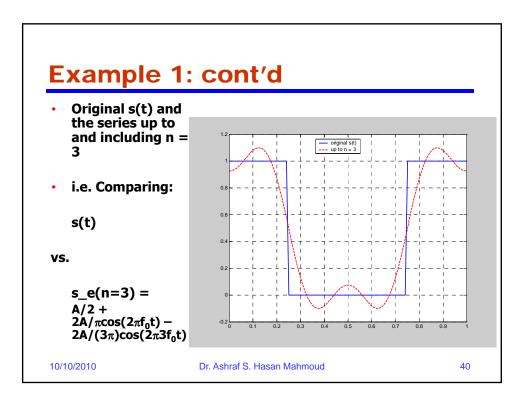
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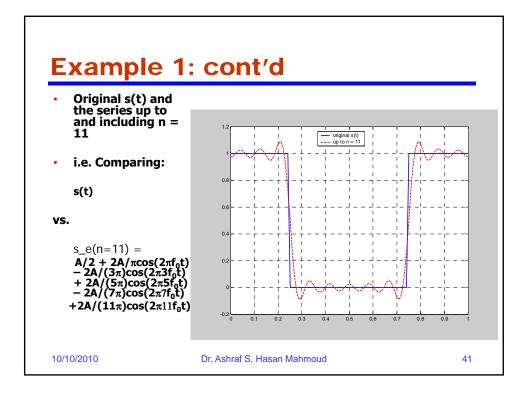
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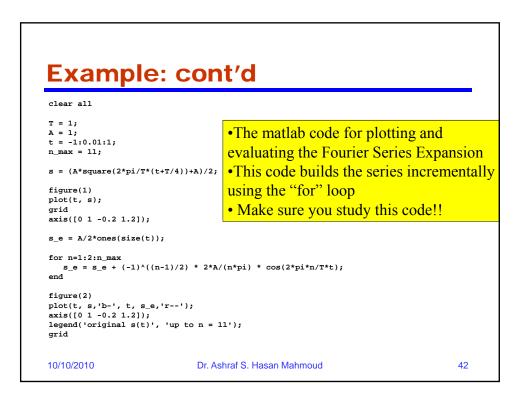
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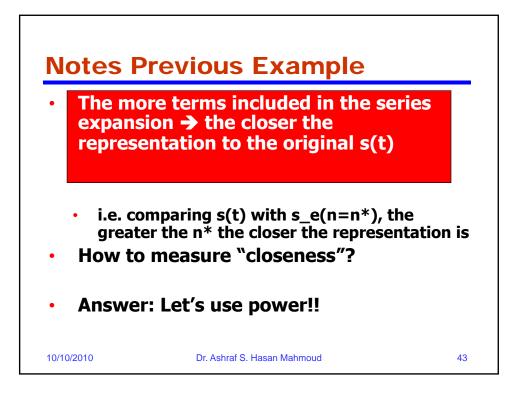


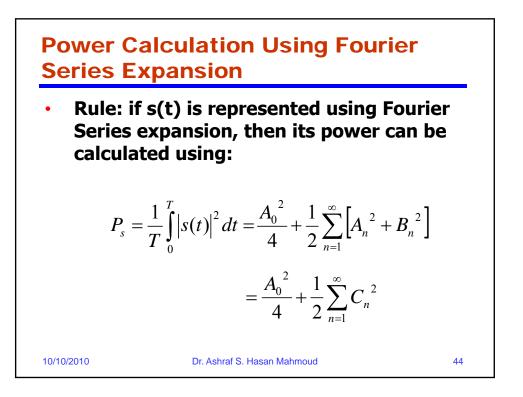


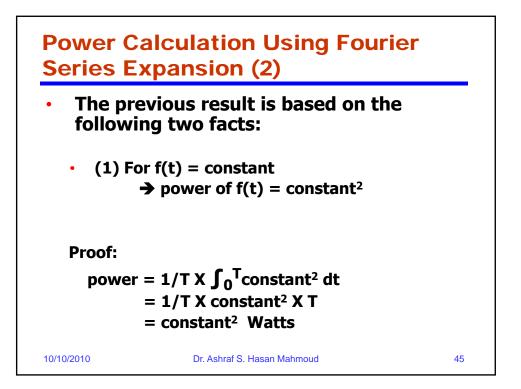


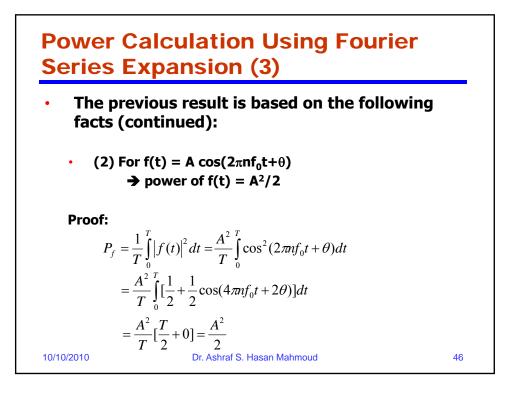












Example 2:

 Problem: What is the power of the signal s(t) used in previous example? And find n* such that the power contained in s_e(n=n*) is 95% of that existing in s(t)?

Solution:
 Let the power of s(t) be given by P_s

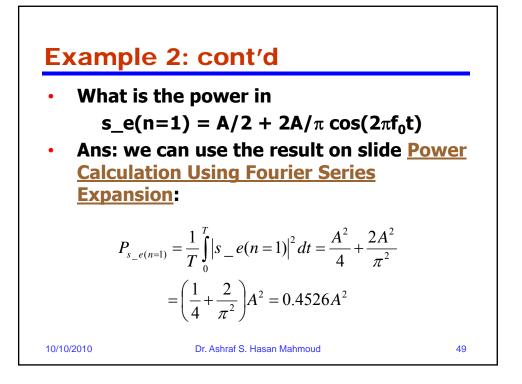
$$P_{s} = \frac{1}{T} \int_{0}^{T} |s(t)|^{2} dt = \frac{1}{T} \times A^{2} \times \frac{T}{2} = \frac{A^{2}}{2} = 0.5A^{2}$$

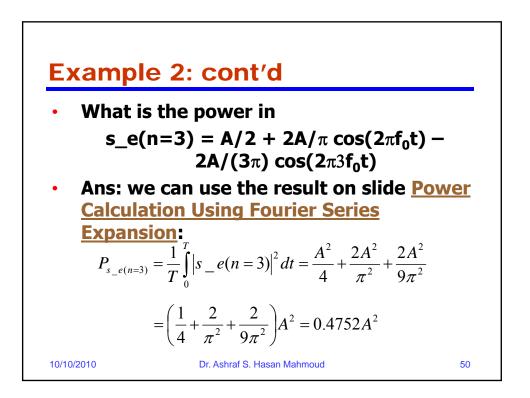
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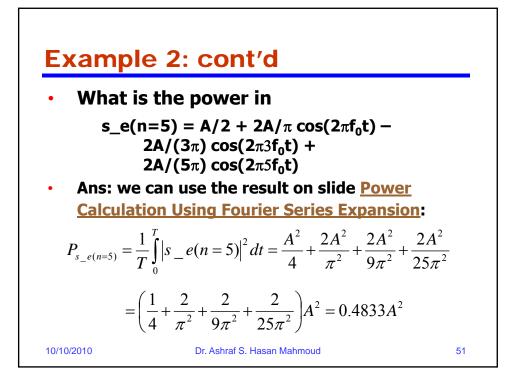
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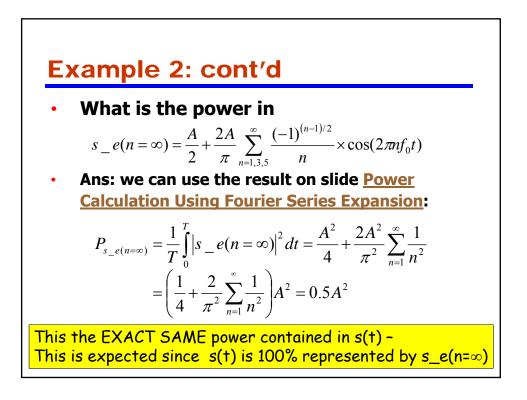
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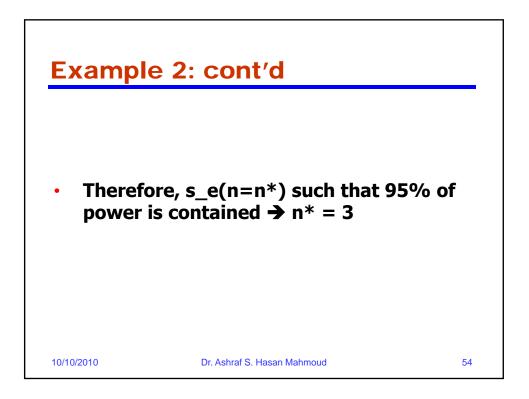


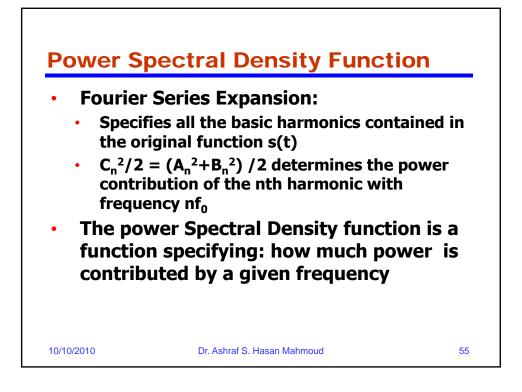


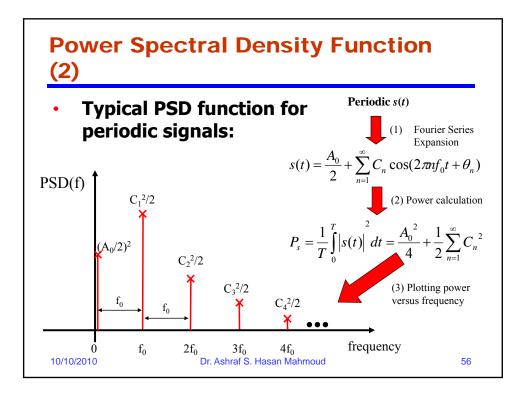


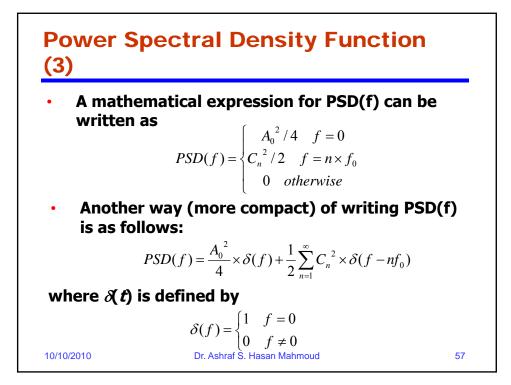


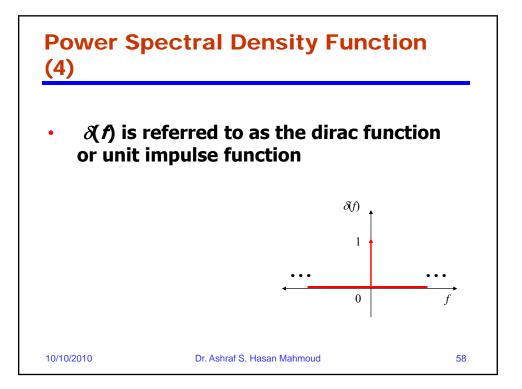
s_e(n=k)	Expression	Power	% Power+
k = 0	A/2	0.25 A ²	$(0.25A^2)/(0.5A^2)$ = 50%
k = 1	$A/2 + 2A/\pi cos(2\pi f_0 t)$	0.4526 A ²	$(0.4526A^2)/(0.5A^2)$ = 90.5%
k = 2*	$A/2 + 2A/\pi \cos(2\pi f_0 t)$	0.4526 A ²	90.5%
k = 3	$A/2 + 2A/\pi cos(2\pi f_0 t) - 2A/(3\pi) cos(2\pi 3f_0 t)$	0.4752 A ²	95.0%
k = 5	$\begin{array}{r} A/2 + 2A/\pi \cos(2\pi f_0 t) - \\ 2A/(3\pi)\cos(2\pi 3 f_0 t) + \\ 2A/(5\pi)\cos(2\pi 5 f_0 t) \end{array}$	0.4833 A ²	96.7%

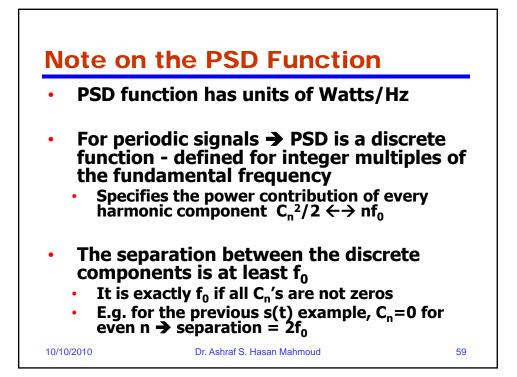


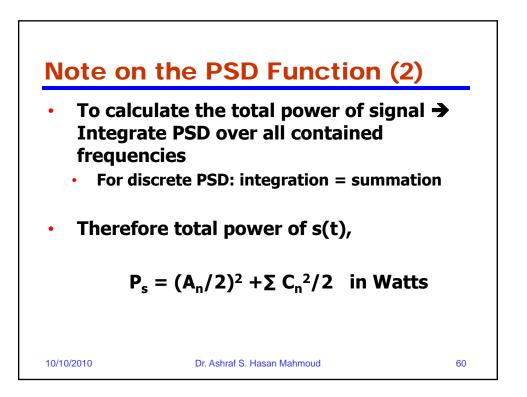


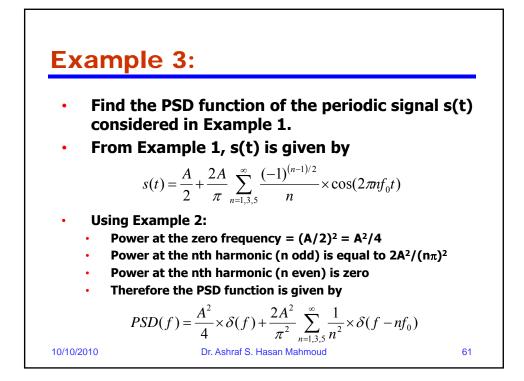


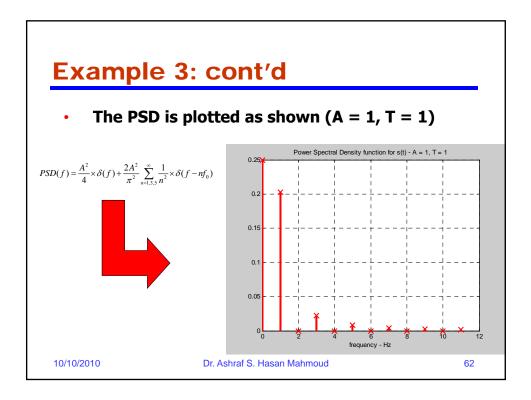


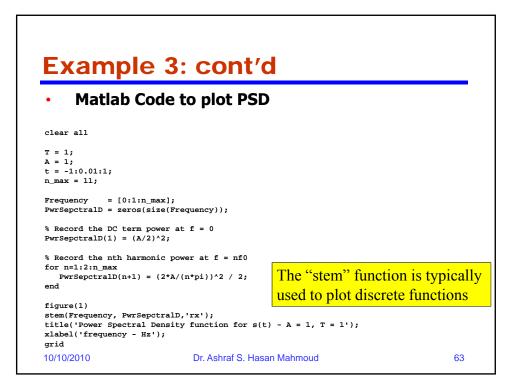


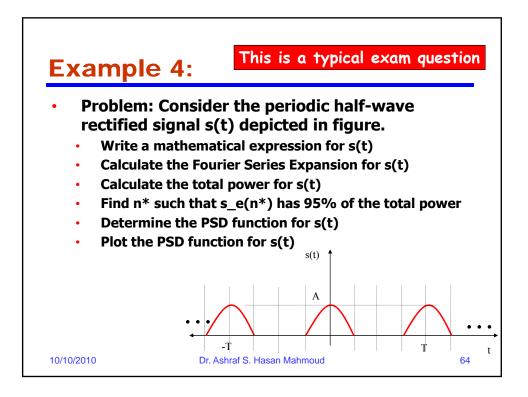


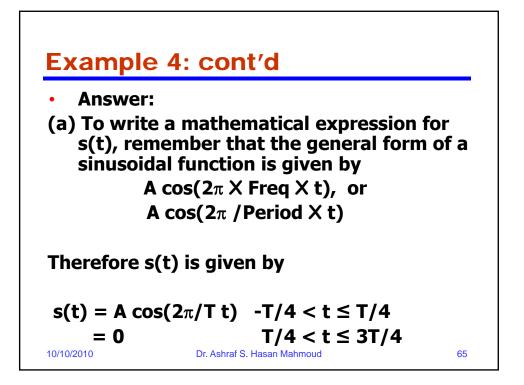


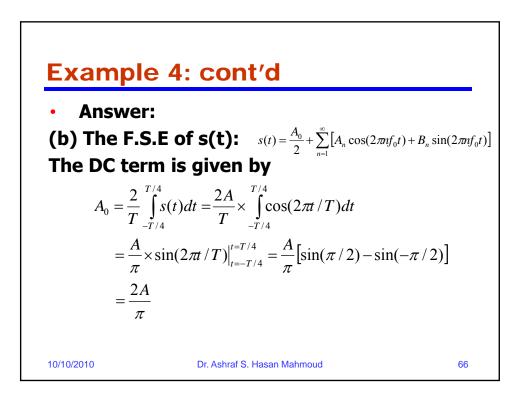


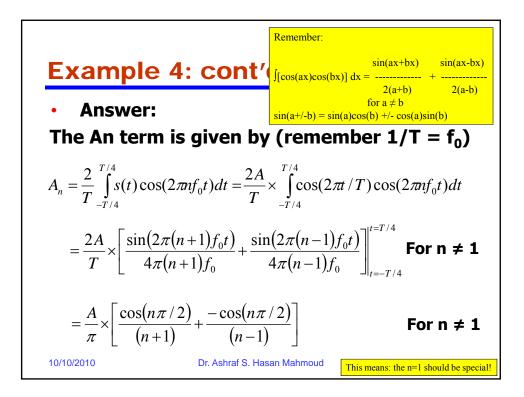


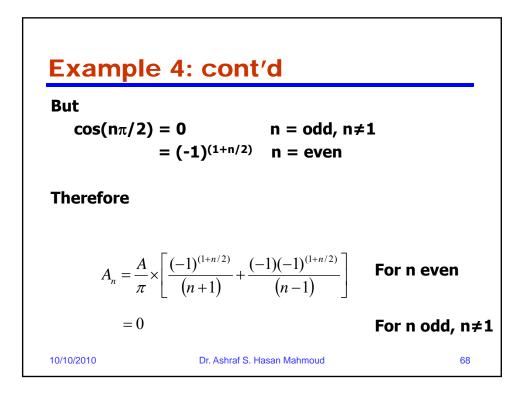


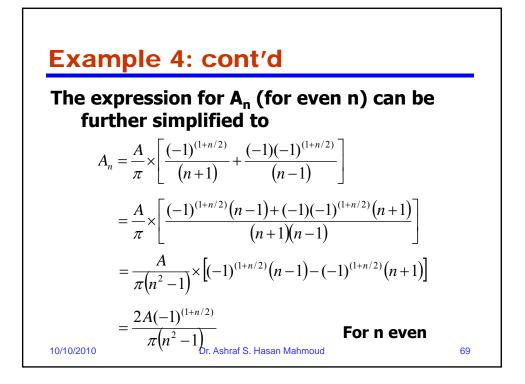


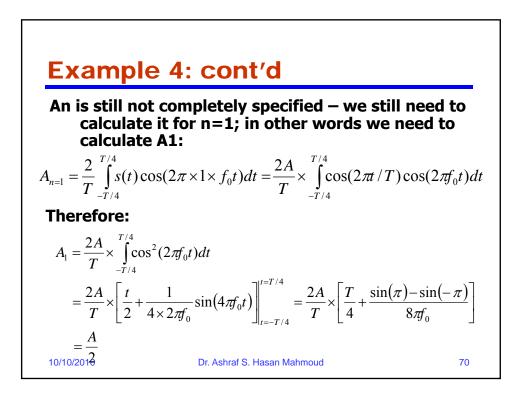








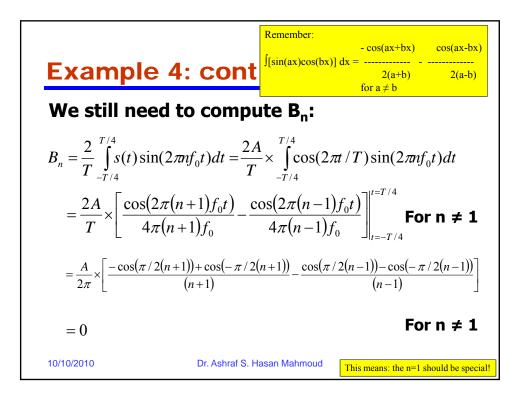




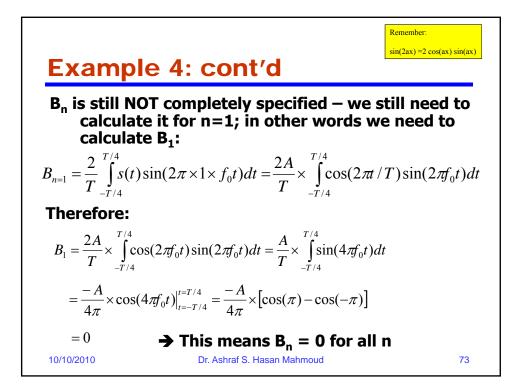


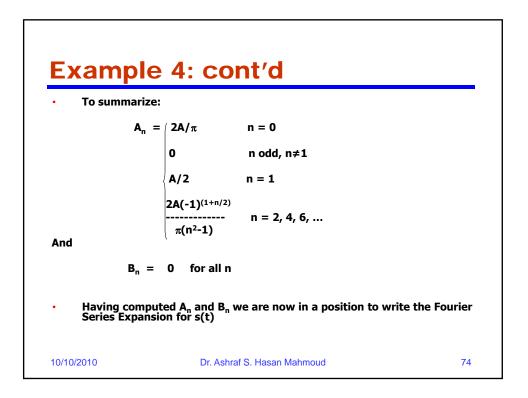
This mean A_n is equal to the following:

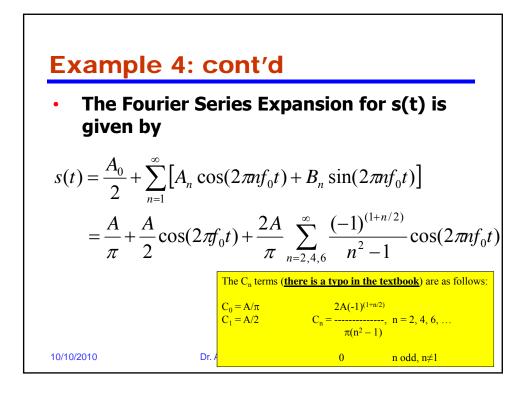
 $A_n = (2A)\pi$ n = 0 n odd, n≠1 0 A/2 n = 1 $2A(-1)^{(1+n/2)} = n = 2, 4, 6, ...$ $\pi(n^2-1)$ The above expression specifies A_n for ALL POSSIBLE values of n specification is complete 10/10/2010 Dr. Ashraf S. Hasan Mahmoud

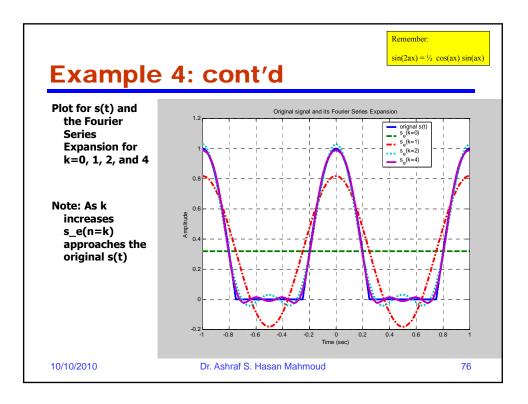


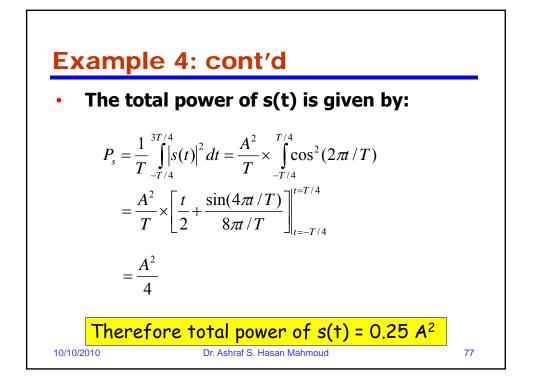
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 To find n* such that power of s_e(n=n*) = 95% of total power: 				
s_e(n=k)	Expression	Power	% Power+	
k = 0	Α/π	0.1013 A ²	$(0.1013A^2)/(0.25)$ $A^2) =$ 40.5%	
k = 1	$A/\pi + A/2\cos(2\pi f_0 t)$	0.2263 A ²	$(0.2262A^2)/(0.25A^2)$ = 90.5%	
k = 2	$A/\pi + A/2 \cos(2\pi f_0 t) + 2A/(3\pi) \cos(2\pi 2 f_0 t)$	0.2488 A ²	(0.2488A ²)/(0.25A ²) 99.5%	

