

Q3) (40 points) A simple machine uses 3 hex digits to represent numbers. Let the used format be $A = A_1A_0.A_{-1}$.

$R = 16, n = 2, m = 1$

For unsigned system:

Maximum unsigned number = $R^n - R^{-m} = (100)_{16} - (0.1)_{16} = (FF.F)_{16} = (255.9375)_{10}$

For R's complement:

(1) Minimum -ve is $(80.0)_{16}$

– The value in decimal = $-R/2 \times R^{n-1} = -8 \times 16^1 = -128.0000$

Since this number is -ve, we CAN NOT find its value using $8 \times 16^1 + 0 \times 16^0 + 0 \times 16^{-1}$

However, $(80.0)_{16}$ is the -ve of $M - (80.0)_{16}$ or $-((100)_{16} - (80)_{16}) = -(80)_{16} = -128.0000$

(2) Maximum +ve is $(7F.F)_{16}$ (i.e. the number just before the minimum -ve)

– The value in decimal = $R/2 \times R^{n-1} - R^{-m} = 8 \times 16^1 - 16^{-1} = 127.9375$

Since this number is +ve

→ we can find its value using $7 \times 16^1 + 15 \times 16^0 + 15 \times 16^{-1} = 127.9375$

For R-1's complement:

(1) Minimum -ve is $(80.0)_{16}$

– The value in decimal = $-R/2 \times R^{n-1} = -8 \times 16^1 = -128.0000$

(2) Maximum +ve is $(7F.F)_{16}$ (i.e. the number just before the minimum -ve)

– The value in decimal = $R/2 \times R^{n-1} - R^{-m} = 8 \times 16^1 - 16^{-1} = 127.9375$

Q3) (40 points) A simple machine uses 3 hex digits to represent numbers. Let the used format be $A = A_1A_0.A_{-1}$.

List of all numbers of the form $A_1A_0.A_{-1}$ where A_i is a hex digit.

| | Unsigned | 15's Complement | 16's Complement |
|-------------|----------|-----------------|-----------------|
| 00.0 | 0.0000 | 0.0000 | 0.0000 |
| 00.1 | 0.0625 | 0.0625 | 0.0625 |
| | | | |
| 00.F | 0.9375 | 0.9375 | 0.9375 |
| 01.0 | 1.0000 | 1.0000 | 1.0000 |
| | ... | ... | ... |
| 7F.E | 127.8750 | 127.8750 | 127.8750 |
| 7F.F | 127.9375 | 127.9375 | 127.9375 |
| 80.0 | 128.0000 | - 127.9375 | - 128.0000 |
| 80.1 | 128.0625 | -127.8750 | -127.9375 |
| | | | |
| FF.E | 255.8750 | -0.0625 | -0.1250 |
| FF.F | 255.9375 | -0.0000 | -0.0625 |